## Patterns of Parallelism

- Decomposition views

Data (static) vs. recursive (dynamic) decomposition

- Exploratory decomposition vs. speculative decomposition

Exploratory - Parallel formulation may perform different amounts of work resulting in super or sub-linear speedup

- Speculative - Schedule tasks even when they may have dependencies

Data parallelism: all processors do the same thing on different data. Regular
Irregula

- Task parallelism: processors do different tasks or dynamically pick up data to compute on

Task queue

- Pipelines


## Pipeline

- Often occurs with image processing applications, where a number of images undergo a sequence of transformations.
- E.g., rendering, clipping, compression, etc.


## Task Parallelism

- Each process performs a different task.
- Two principal flavors:
- pipelines
- task queues
- Program Examples: PIPE (pipeline), TSP (task queue).


## Sequential Program

for( $\mathrm{i}=0 ; \mathrm{i}<$ num_pic, read(in_pic[i]); i++ ) \{
int_pic_1[i] = trans1 (in_pic[i] );
int_pic_2[i] = trans2( int_pic_1[i]);
int_pic_3[i] = trans3( int_pic_2[i]);
out_pic[i] = trans4( int_pic_3[i]);
\}

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## Parallelizing a Pipeline

- For simplicity, assume we have 4 processors (i.e., equal to the number of transformations).
- Furthermore, assume we have a very large number of pictures (>>4).

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Sequential vs. Parallel Execution

- Sequential
- Parallel

(Color -- picture; horizontal line -- processor).

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Parallelizing a Pipeline (part 2)
Processor 2:

```
for( i=0; i<num_pics; i++ ) {
    wait( event_1_2[i]);
        int_pic_2[i] = trans2(int_pic_1[i]);
        signal(event_2_3[i]);
    }
```

Same for processor 3

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## Parallelizing a Pipeline (part 3)

Processor 4:

```
for(i=0; i<num_pics; i++ ) {
    wait( event_3_4[i]);
    out_pic[i] = trans4(int_pic_3[i] );
}
```


## Another Sequential Program

```
for(i=0; i<num_pic, read(in_pic); i++ ) {
    int_pic_1 = trans1( in_pic );
    int_pic_2 = trans2( int_pic_1);
    int_pic_3 = trans3( int_pic_2);
    out_pic = trans4( int_pic_3);
}
```

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Can we use same parallelization?

- No, because of anti-dependence between stages, there is no parallelism
- Another example of privatization
- Costly in terms of memory


## In-between Solution

- Use $\mathrm{n}>1$ buffers between stages.
- Block when buffers are full or empty


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## Perfect Pipeline

- Sequential
- Parallel

(Color -- picture; horizontal line -- processor).


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## Patterns of Parallelism

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resulting in super or sub-linear speedup
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- Data parallelism: all processors do the same thing on different data. Regular
Irregular
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Task queue
Pipelines

## Exploratory Decomposition

Explore state space by creating independent tasks to follow each possible move from current state


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Exploratory Decomposition
Example: A 15-tile puzzle

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 9 | 8 |
| 9 | 10 | 7 | 11 |
| 13 | 14 | 15 | 12 |


| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | -11 |  |
| 13 | 14 | 15 | 12 |



(d)
(a)
(b)
(c)

Sequence of 3 moves leads from initial state (a) to final state (d)

In general: explore all possible moves to arrive at solution

## Exploratory Decomposition Speedup

- Parallel formulation may perform more or less work depending on when solution is found
- Superlinear or sublinear speedup


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## TSP (Traveling Salesman)

- Goal:
- given a list of cities, a matrix of distances between them, and a starting city,
- find the shortest tour in which all cities are visited exactly once.
- Example of an NP-hard search problem.
- Algorithm: branch-and-bound.


## Finding the Solution

- Eventually, a complete path will be found.
- Remember its length as the current shortest path.
- Every time a complete path is found, check if we need to update current best path.
- When priority queue becomes empty, best path is found.


## Branching

- Initialization:
- go from starting city to each of remaining cities - put resulting partial path into priority queue, ordered by its current length.
- Further (repeatedly):
- take head element out of priority queue,
- expand by each one of remaining cities,
- put resulting partial path into priority queue.

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## Using a Simple Bound

- Once a complete path is found, we have a lower bound on the length of shortest path
- No use in exploring partial path that is already longer than the current lower bound
- Better bounding methods exist ...


## Sequential TSP: Data Structures

- Priority queue of partial paths.
- Current best solution and its length.
- For simplicity, we will ignore bounding.


## Parallel TSP: Possibilities

- Have each process do one expansion
- Have each process do expansion of one partial path
- Have each process do expansion of multiple partial paths
- Issue of granularity/performance, not an issue of correctness.
- Assume: process expands one partial path.


## Sequential TSP: Code Outline

```
init_q(); init_best();
while( (p=de_queue()) != NULL ) {
    for each expansion by one city {
        q = add_city(p);
        if( complete(q) ) { update_best(q) };
        else { en_queue(q) };
    }
}
```

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## Parallel TSP: Synchronization

- True dependence between process that puts partial path in queue and the one that takes it out.
- Dependences arise dynamically.
- Required synchronization: need to make process wait if $q$ is empty.


## Parallel TSP: First Cut (part 1)

process i:
while( ( $\mathrm{p}=$ de_queue()) != NULL ) \{
for each expansion by one city \{
$\mathrm{q}=\operatorname{add} \_$city $(\mathrm{p})$;
if complete(q) \{ update_best(q) \};
else en_queue(q);
\}
\}


## Parallel TSP: First cut (part 2)

- In de_queue: wait if q is empty
- In en_queue: signal that q is no longer empty


## Parallel TSP: More synchronization

- All processes operate, potentially at the same time, on $q$ and best.
- This must not be allowed to happen.
- Critical section: only one process can execute in critical section at once.


## Parallel TSP: Critical Sections

- All shared data must be protected by critical section.
- Update_best must be protected by a critical section.
- En_queue and de_queue must be protected by the same critical section.


## Termination condition

- How do we know when we are done?
- All processes are waiting inside de_queue.
- Count the number of waiting processes before waiting.
- If equal to total number of processes, we are done.


## Parallel TSP

```
process i:
    while( (p=de_queue()) != NULL ) {
        for each expansion by one city {
            q = add_city(p);
            if complete(q) { update_best(q) };
            else en_queue(q)
        }
    }
```

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## Programming Models

- Standard models of parallelism
- shared memory (Pthreads)
- message passing (MPI)
- data parallel (Fortran 90 and HPF)
- shared memory + data parallel (OpenMP)
- Remote procedure call
- Global address space (UPC)

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## The Performance Transparency Modern multicore sysems hällenge <br> 10s to 100s of hardware contexts

- Shared hardware resource access
- Functional units, caches, on- and off-chip interconnects, memory
- Shared software resource access
- E.g., locks or shared data
- Non-uniform access latencies


## Shared Memory



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Impact of Thread Placement on Data Sharing Costs


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