

Machine-Level Programming II: Arithmetic & Control

Kai Shen

1

Outline

- Arithmetic operations
- Control: Condition codes
- Conditional branches
- Loops
- Switch

2

Some Arithmetic Operations

- Two Operand Instructions:

Format	Computation	
<code>addl Src, Dest</code>	<code>Dest = Dest + Src</code>	
<code>subl Src, Dest</code>	<code>Dest = Dest - Src</code>	
<code>imull Src, Dest</code>	<code>Dest = Dest * Src</code>	
<code>sall Src, Dest</code>	<code>Dest = Dest << Src</code>	Also called <i>shll</i>
<code>sarl Src, Dest</code>	<code>Dest = Dest >> Src</code>	Arithmetic
<code>shrl Src, Dest</code>	<code>Dest = Dest >> Src</code>	Logical
<code>xorl Src, Dest</code>	<code>Dest = Dest ^ Src</code>	
<code>andl Src, Dest</code>	<code>Dest = Dest & Src</code>	
<code>orl Src, Dest</code>	<code>Dest = Dest Src</code>	

- One Operand Instructions

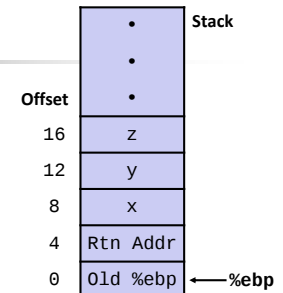
<code>incl Dest</code>	<code>Dest = Dest + 1</code>
<code>decl Dest</code>	<code>Dest = Dest - 1</code>
<code>negl Dest</code>	<code>Dest = - Dest</code>
<code>notl Dest</code>	<code>Dest = ~Dest</code>

3

Arithmetic Example

```
int arith(int x, int y, int z)
{
    int t1 = x+y;
    int t2 = z+t1;
    int t3 = x+4;
    int t4 = y * 48;
    int t5 = t3 + t4;
    int rval = t2 * t5;
    return rval;
}
```

```
movl 8(%ebp), %ecx    # ecx = x
movl 12(%ebp), %edx   # edx = y
leal (%edx,%edx,2), %eax # eax = y*3
sall $4, %eax         # eax *= 16 (t4)
leal 4(%ecx,%eax), %eax # eax = t4 +x+4 (t5)
addl %ecx, %edx       # edx = x+y (t1)
addl 16(%ebp), %edx   # edx += z (t2)
imull %edx, %eax      # eax = t2 * t5 (rval)
```



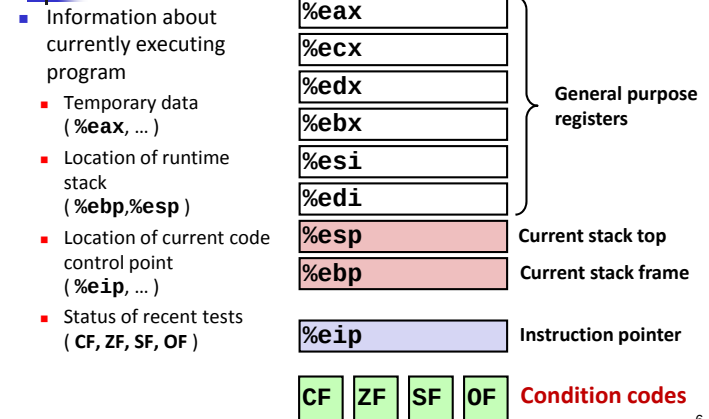
4

Outline

- Arithmetic operations
- Control: Condition codes
- Conditional branches
- Loops
- Switch

5

Processor State (IA32, Partial)



6

Condition Codes (Arithmetic Setting)

- Single bit registers
 - **CF** Carry Flag (for unsigned) **SF** Sign Flag (for signed)
 - **ZF** Zero Flag **OF** Overflow Flag (for signed)
- Set by arithmetic operations

Example: `addl/addq Src, Dest` $\leftrightarrow$ `t = a+b`

 - CF set** if carry out from most significant bit (unsigned overflow)
 - ZF set** if `t == 0`
 - SF set** if `t < 0` (as signed)
 - OF set** if two's-complement (signed) overflow
 $(a > 0 \ \&\& \ b > 0 \ \&\& \ t < 0) \ || \ (a < 0 \ \&\& \ b < 0 \ \&\& \ t >= 0)$
- Not set by `leal` instruction

7

Condition Codes (Setting by Compare)

- Setting by compare instruction
 - `cmpl Src2, Src1`
 - `cmpl b, a` like computing `a-b` without setting destination
- **CF set** if carry out from most significant bit (used for unsigned comparisons)
- **ZF set** if `a == b`
- **SF set** if `(a-b) < 0` (as signed)
- **OF set** if two's-complement (signed) overflow
 $(a > 0 \ \&\& \ b < 0 \ \&\& \ (a-b) < 0) \ || \ (a < 0 \ \&\& \ b > 0 \ \&\& \ (a-b) > 0)$

8

Condition Codes (Setting by Test)

- Setting by Test instruction
 - `testl Src2, Src1`
`testl b, a` like computing `a&b` without setting destination
 - Sets condition codes based on value of `Src1` & `Src2`
 - Useful to have one of the operands be a mask
 - ZF** set when `a&b == 0`
 - SF** set when `a&b < 0`

9

Reading Condition Codes

- SetX Instructions:
 - Set single byte based on combination of condition codes
- One of 8 addressable byte registers
 - Does not alter remaining 3 bytes
 - Typically use `movzbl` to finish job

```
int gt (int x, int y)
{
    return x > y;
}
```

```
movl 12(%ebp),%eax # eax = y
cmpl %eax,8(%ebp)  # Compare x : y
setg %al           # al = x > y
movzbl %al,%eax    # Zero rest of %eax
```

%eax %ah %al

%ecx %ch %cl

%edx %dh %dl

%ebx %bh %bl

%esi

%edi

%esp

%ebp

10

Reading Condition Codes

- SetX instructions
 - Set single byte based on combinations of condition codes

SetX	Condition	Description
<code>sete</code>	ZF	Equal / Zero
<code>setne</code>	~ZF	Not Equal / Not Zero
<code>sets</code>	SF	Negative
<code>setns</code>	~SF	Nonnegative
<code>setg</code>	~(SF^OF) & ~ZF	Greater (Signed)
<code>setge</code>	~(SF^OF)	Greater or Equal (Signed)
<code>setl</code>	(SF^OF)	Less (Signed)
<code>setle</code>	(SF^OF) ZF	Less or Equal (Signed)
<code>seta</code>	~CF & ~ZF	Above (unsigned)
<code>setb</code>	CF	Below (unsigned)

11

Outline

- Arithmetic operations
- Control: Condition codes
- Conditional branches & Moves
- Loops
- Switch

12

Jumping

- jX Instructions
 - Jump to different part of code depending on condition codes

jX	Condition	Description
jmp	1	Unconditional
je	ZF	Equal / Zero
jne	~ZF	Not Equal / Not Zero
js	SF	Negative
jns	~SF	Nonnegative
jg	~(SF^OF)&~ZF	Greater (Signed)
jge	~(SF^OF)	Greater or Equal (Signed)
jl	(SF^OF)	Less (Signed)
jle	(SF^OF) ZF	Less or Equal (Signed)
ja	~CF&~ZF	Above (unsigned)
jb	CF	Below (unsigned)

13

Conditional Control

- In assembly/machine code, jump is pretty much all we got
- But there are a variety of conditional control in high-level languages
 - if ... else ...
 - switch(...) {}
 - while loop
 - for loop
 -

14

Conditional Branch Example

```
int absdiff(int x, int y)
{
    int result;
    if (x > y) {
        result = x-y;
    } else {
        result = y-x;
    }
    return result;
}
```

```
absdiff:
    pushl %ebp
    movl %esp, %ebp
    movl 8(%ebp), %edx
    movl 12(%ebp), %eax
    cmpl %eax, %edx
    jle .L6
    subl %eax, %edx
    movl %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax
.L7:
    popl %ebp
    ret
```

Setup

Body1

Body2a

Body2b

Finish

15

Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
    int result;
    if (x <= y) goto Else;
    result = x-y;
    goto Exit;
Else:
    result = y-x;
Exit:
    return result;
}
```

```
absdiff:
    pushl %ebp
    movl %esp, %ebp
    movl 8(%ebp), %edx
    movl 12(%ebp), %eax
    cmpl %eax, %edx
    jle .L6
    subl %eax, %edx
    movl %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax
.L7:
    popl %ebp
    ret
```

Setup

Body1

Body2a

Body2b

Finish

- Better resemblance to “goto”-style C code
- Bad coding style, but that’s not our concern here

16

Using Conditional Moves

- Conditional move instructions
 - if (Test) Dest $\leftarrow$ Src
- Why?
 - Branches are very disruptive to instruction flow through pipelines
 - Cond-mov require no control transfer

C Code

```
val = Test
    ? Then_Expr
    : Else_Expr;
```

Cond-mov Version

```
tval = Then_Expr;
result = Else_Expr;
t = Test;
if (t) result = tval;
return result;
```

17

Outline

- Arithmetic operations
- Control: Condition codes
- Conditional branches and moves
- Loops
- Switch

18

Loop Control

- In assembly/machine code, jump is pretty much all we got for conditional control (similar to "goto" in C)
- Convert typical loop control into goto-based C code.
 - Familiarize with assembly/machine programming
 - Understand compiler transformation
 - Able to read/comprehend assembly/machine code

19

"Do-While" Loop Example

C Code

```
int pcount_do(unsigned x)
{
    int result = 0;
    do {
        result += x & 0x1;
        x >>= 1;
    } while (x);
    return result;
}
```

Goto Version

```
int pcount_do(unsigned x)
{
    int result = 0;
loop:
    result += x & 0x1;
    x >>= 1;
    if (x)
        goto loop;
    return result;
}
```

- Count number of 1's in argument x
- Use conditional branch to either continue looping or to exit loop

20

"Do-While" Loop Compilation

Goto Version

```

int pcount_do(unsigned x) {
    int result = 0;
loop:
    result += x & 0x1;
    x >>= 1;
    if (x)
        goto loop;
    return result;
}
  
```

Registers:
 %edx x
 %ecx result

```

movl $0, %ecx # result = 0
.L2: # loop:
movl %edx, %eax
andl $1, %eax # t = x & 1
addl %eax, %ecx # result += t
shrl %edx # x >>= 1
jne .L2 # If !0, goto loop
  
```

21

General "Do-While" Translation

C Code

```

do
    Body
while (Test);
  
```

Goto Version

```

loop:
    Body
    if (Test)
        goto loop
  
```

22

General "While" Translation

While version

```

while (Test)
    Body
  
```

Do-While Version

```

if (!Test)
    goto done;
do
    Body
while (Test);
done:
  
```

Goto Version

```

if (!Test)
    goto done;
loop:
    Body
    if (Test)
        goto loop;
done:
  
```

23

General "For" Translation

For Version

```

for (Init; Test; Update)
    Body
  
```

While Version

```

Init;
while (Test) {
    Body
    Update;
}
  
```

Do-While Version

```

Init;
if (!Test)
    goto done;
do
    Body
    Update
while (Test);
done:
  
```

Goto Version

```

Init;
if (!Test)
    goto done;
loop:
    Body
    Update
    if (Test)
        goto loop;
done:
  
```

24

"For" Loop Conversion Example

C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
    int i;
    int result = 0;
    for (i = 0; i < WSIZE; i++) {
        unsigned mask = 1 << i;
        result += (x & mask) != 0;
    }
    return result;
}
```

- Initial test can be optimized away

Goto Version

```
int pcount_for_gt(unsigned x) {
    int i;
    int result = 0;
    i = 0; Init
    if (i < WSIZE) !Test
    goto done;
loop: Body
    {
        unsigned mask = 1 << i;
        result += (x & mask) != 0;
    }
    i++; Update
    if (i < WSIZE) Test
        goto loop;
done:
    return result;
}
```

25

Outline

- Arithmetic operations
- Control: Condition codes
- Conditional branches and moves
- Loops
- Switch

26

Switch Statement

```
long switch_eg
(long x, long y, long z)
{
    long w = 1;
    switch(x) {
        case 1:
            w = y*z;
            break;
        case 2:
            w = y/z;
            /* Fall Through */
        case 3:
            w += z;
            break;
        case 5:
        case 6:
            w -= z;
            break;
        default:
            w = 2;
    }
    return w;
}
```

- An example
 - Multiple case labels (5 & 6)
 - Fall through case (2)
 - Missing case (4)
- How to implement switch statement in machine code?
 - Using jumps (or "goto")
- Jump table avoids sequencing through cases
 - constant time, rather than linear

27

Jump Table Structure

Switch Form

```
switch(x) {
    case val_0:
        Block 0
    case val_1:
        Block 1
    . . .
    case val_n-1:
        Block n-1
}
```

Jump Table

```
jtab: Targ0
      Targ1
      Targ2
      .
      .
      Targn-1
```

Jump Targets

Targ0: Code Block 0

Targ1: Code Block 1

Targ2: Code Block 2

...

Targn-1: Code Block n-1

Approximate Translation

```
target = JTab[x];
goto *target;
```

28

Switch Statement Example (IA32)

```
long switch_eg(long x, long y, long z)
{
    long w = 1;
    switch(x) {
        . . .
    }
    return w;
}
```

Jump table

```
.section .rodata
.align 4
.JT:
.long .L2 # x = 0
.long .L3 # x = 1
.long .L4 # x = 2
.long .L5 # x = 3
.long .L2 # x = 4
.long .L6 # x = 5
.long .L6 # x = 6
```

Setup:

```
switch_eg:
    pushl %ebp          # Setup
    movl %esp, %ebp     # Setup
    movl 8(%ebp), %eax   # eax = x
    cmpl $6, %eax       # Compare x:6
    ja .L2              # If unsigned > goto default
    jmp *.JT(, %eax, 4)  # Goto *JT[x]
```

Indirect
jump →

29

Jump Table

```
.section .rodata
.align 4
.JT:
.long .L2 # x = 0
.long .L3 # x = 1
.long .L4 # x = 2
.long .L5 # x = 3
.long .L2 # x = 4
.long .L6 # x = 5
.long .L6 # x = 6
```

```
switch(x) {
    case 1: // .L3
        w = y*z;
        break;
    case 2: // .L4
        w = y/z;
        /* Fall Through */
    case 3: // .L5
        w += z;
        break;
    case 5:
    case 6: // .L6
        w -= z;
        break;
    default: // .L2
        w = 2;
}
```

30

Discover Jump Table in Machine Code

- First, find the address of the jump table

Disassembled Object Code

```
08048410 <switch_eg>:
    . . .
8048419: 77 07          ja      8048422 <switch_eg+0x12>
804841b: ff 24 85 60 86 04 08 jmp     *0x8048660(, %eax, 4)
```

- Then read into the jump table
- But the table doesn't show up in disassembled code
- Can inspect using GDB: **x/7xw 0x8048660**
 - Examine **Z** hexadecimal format "words" (4-bytes each)
 - Use command "**help x**" to get format documentation

```
0x8048660: 0x08048422 0x08048432 0x0804843b 0x08048429
0x8048670: 0x08048422 0x0804844b 0x0804844b
```

31

Matching Disassembled Targets

Value	Disassembly
0x8048422	8048422: mov \$0x2,%eax
0x8048432	8048427: jmp 8048453 <switch_eg+0x43>
0x8048442	8048429: mov \$0x1,%eax
0x804844b	804842e: xchgb %ax,%ax
0x8048444	8048430: jmp 8048446 <switch_eg+0x36>
0x8048445	8048432: mov 0x10(%ebp),%eax
0x8048446	8048435: imul 0xc(%ebp),%eax
0x8048447	8048439: jmp 8048453 <switch_eg+0x43>
0x8048448	804843b: mov 0xc(%ebp),%edx
0x8048449	804843e: mov %edx,%eax
0x804844a	8048440: sar \$0x1f,%edx
0x804844b	8048443: idivl 0x10(%ebp)
0x804844c	8048446: add 0x10(%ebp),%eax
0x804844d	8048449: jmp 8048453 <switch_eg+0x43>
0x804844e	804844b: mov \$0x1,%eax
0x804844f	8048450: sub 0x10(%ebp),%eax
0x8048450	8048453: pop %ebp
0x8048451	8048454: ret

32



Summary on Execution Control

- Control in high-level language
 - if-then-else
 - do-while
 - while, for
 - switch
- Control in machine code
 - Conditional jump
 - Conditional move
 - Indirect jump
 - Compiler generates code sequence to implement more complex control
- Standard techniques
 - Loops converted to go-to form
 - Large switch statements use jump tables
 - Sparse switch statements may use decision trees

33



Disclaimer

These slides were adapted from the CMU course slides provided along with the textbook of "Computer Systems: A programmer's Perspective" by Bryant and O'Hallaron. The slides are intended for the sole purpose of teaching the computer organization course at the University of Rochester.

34