Fault-Tolerant Consensus

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Consensus Problem

- Many distributed system problems are about reaching decisions consistently
  - Whether to commit a transaction in a distributed database?
  - How to order a series of updates in a replicated database?
  - Who gets the lock first in a distributed lock management?
  - Who should be the leader to perform a task on behalf of all of us?
  - ... ...

Fault Tolerance

- Fault tolerance in a distributed system
  - Nodes may fail, messages may disappear
  - Non-faulty nodes still want to get work done

- Fault-tolerant consensus:
  - Reach agreement on something, e.g., determine whether a bit should be 1 or 0
  - Consistency: all must agree on one value
  - Non-triviality: both 1 and 0 may appear as the agreed result, depending on the system semantics

Is it Difficult?

- Two-generals' problem
  - Two nodes with a faulty communication line
  - Try to reach agreement by proposing an idea and wait for acknowledgement

- Impossibility result for any deterministic protocol
  - Assume a minimal set of successful messages that convince both to attack
  - If the last message was lost, then the receiver would have doubt while the sender would attack

- Ideas:
  - If the leader makes a proposal and never wavers ...
  - But the proposal shouldn't go against the majority view
Paxos Algorithm (Lamport)

- Failure modes
  - Nodes fail-stop
  - Messages can be lost, but do not linger forever

- Paxos algorithm (Lamport)
  - Each leader can propose a value in a round
  - Multiple leaders can propose simultaneously; rounds have ordered IDs but they may happen in arbitrary order
  - A successful round lead to the acceptance of a value by some; all nodes must ever only accept one value

Paxos Algorithm

1. Initiate a round, the leader sends "Collect" to everyone.
2. A node, receiving the message, responds with "Last" message of any previously accepted value (if any); it responds with "OldRound" if it already accepted a value at a later round.
3. When the leader collects \( \frac{n}{2} \) "Last" messages (info-quorum), it proposes a value through a "Begin" message to everyone.
4. A node, receiving the message, accepts the proposed value and responds with "Accept"; it responds with "OldRound" if it already accepted a value at a later round.
5. The leader waits for \( \frac{n}{2} \) "Accept" messages (accept-quorum) to successfully conclude the round.

Byzantine Failures

- Can two rounds accept different values?
- Tolerate failures of fewer than half of the nodes

- Node failures:
  - Crash, or fail-stop
  - Byzantine: do arbitrary (maybe malicious) things

- Consensus with fail-stop failures:
  - Non-faulty nodes try to reach a decision
  - Then impose upon the whole system as a majority
  - For \( k \) failures, whole system size is at least \( 2k+1 \)

- Consensus with Byzantine failures:
  - How to guarantee the decision is the majority of non-faulty nodes?
  - For \( k \) failures, we need at least \( 2k+1 \) good nodes
  - \( n \)-node Byzantine system cannot tolerate \( k \) failures if \( n=3k \)
Consensus in Asynchronous Systems

- Synchronous systems
  - Messages take bounded delay (operate in steps)

- Asynchronous systems
  - Messages can take arbitrarily long
  - Impossible to distinguish message losses from slow messages

- Impossibility result
  - Not even a single machine failure can be tolerated

Consensus in Partially Asynchronous Systems

- In partially asynchronous system, message delays are bounded, but protocol designer doesn't know the bound

- Can't design things in steps, must deal with concurrent communication steps

- Paxos works for such systems