

CSC 172– Data Structures and Algorithms

Lecture #17

Spring 2018

Please put away all electronic devices



Announcement

- Project 3 is out
 - Due: 04/13/2018 (11:59 pm)

- Huffman tree
- Priority Queue
- HashMap
- Encoding
- Decoding

HUFFMAN CODING

Recall: Variable-Length Encoding: Idea

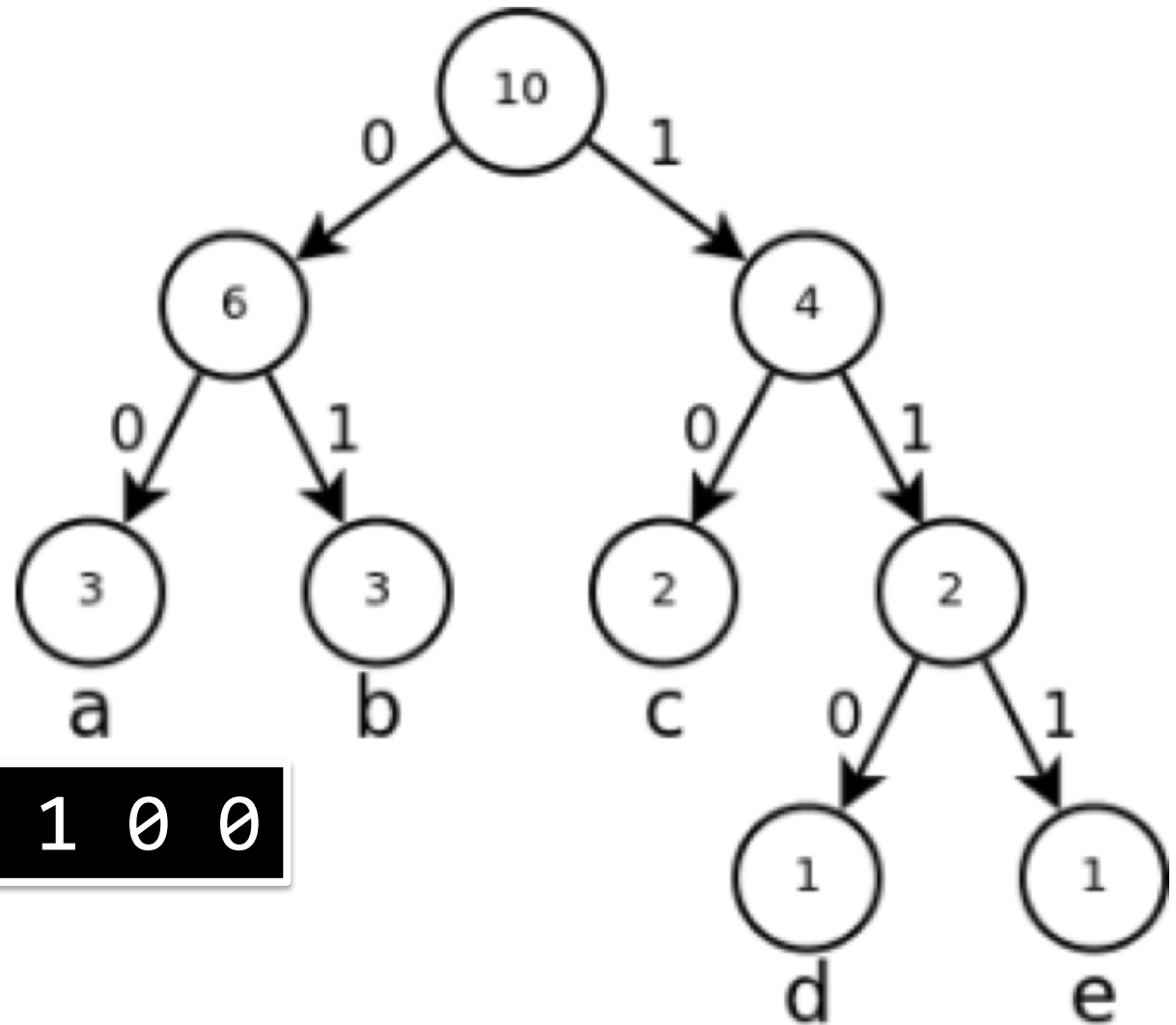
- Encode letter E with fewer bits, say b_E bits
- Letter J with many more bits, say b_J bits
- We gain space if

- $$b_E \cdot f_E + b_J \cdot f_J < 8f_E + 8f_J$$

where $\mathbf{f}$ is the frequency vector

- Problem: how to decode?

Recall: Solution --- Prefix-Free Codes



1 0 1 1 1 0 1 0 0

c e b a

Objectives

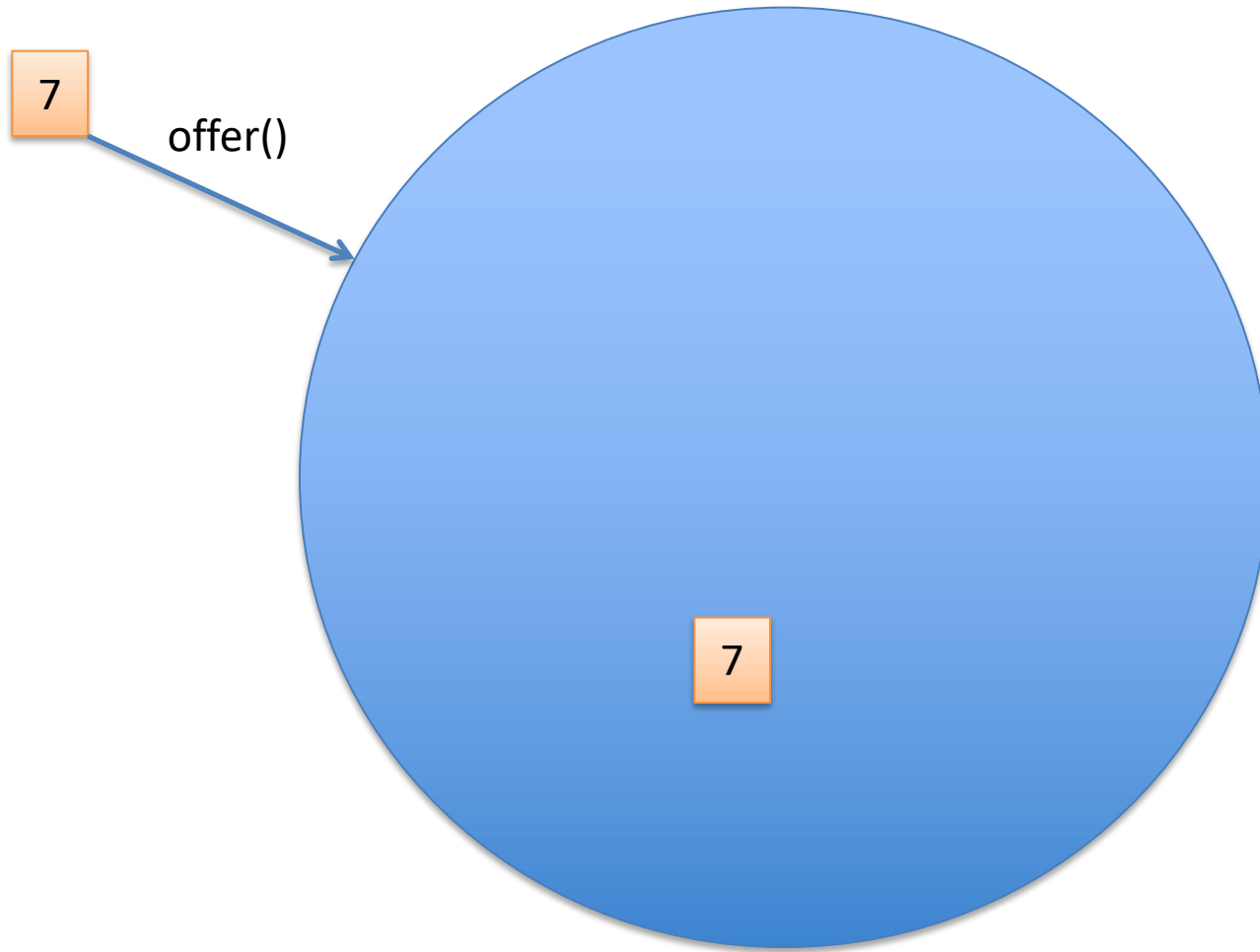
- Huffman tree
- Priority Queue
- HashMap
- Encoding
- Decoding

PRIORITY QUEUE

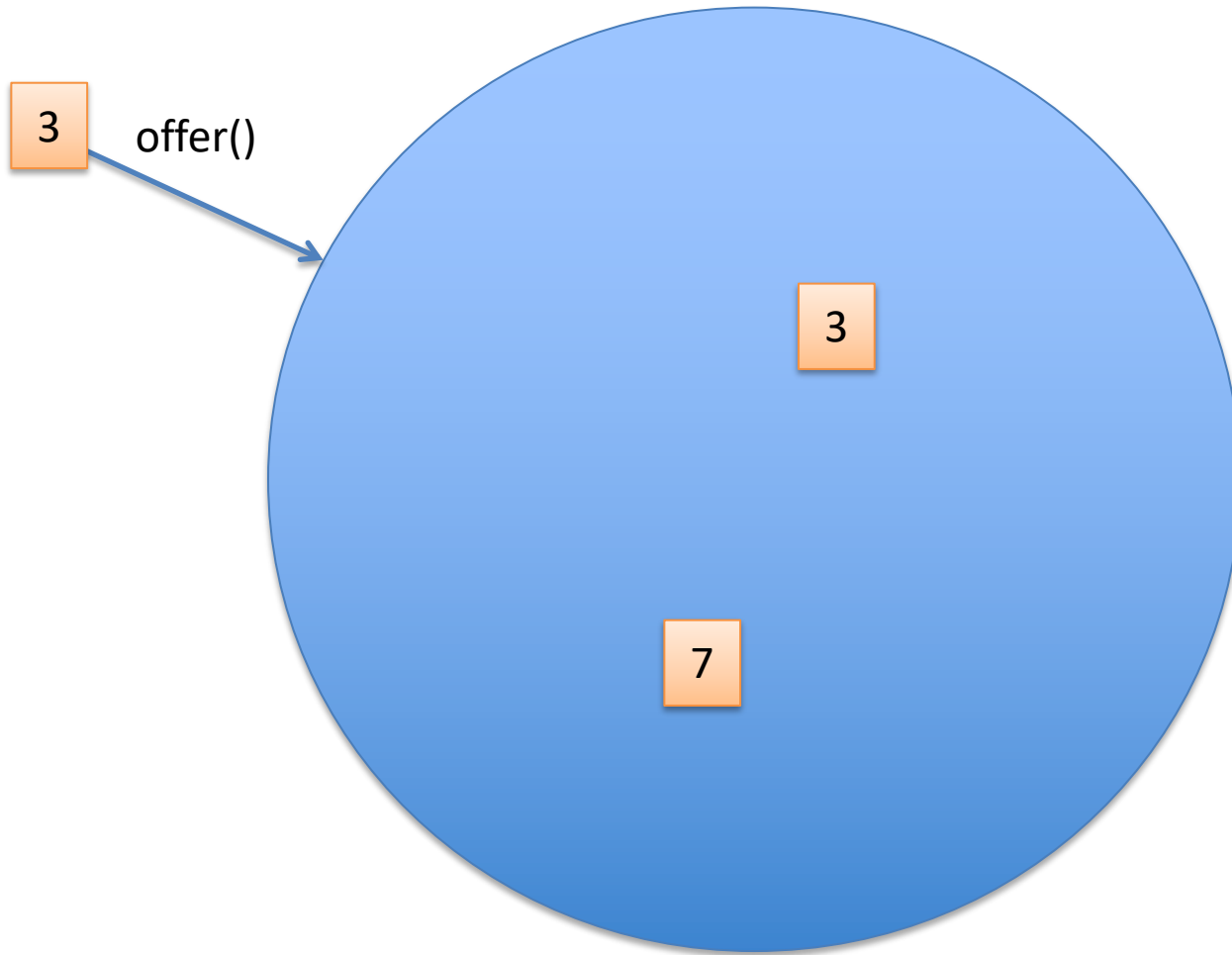
Priority Queues

- **Stack: FILO**
 - push(), pop(), peek()
- **Queue: FIFO**
 - offer(), poll(), peek()
- **Priority Queue:**
 - Is a Queue
 - Each element has a “priority”
 - offer() stores new element (with “priority”)
 - poll() removes element with highest/lowest priority
 - peek() shows that element but doesn’t remove

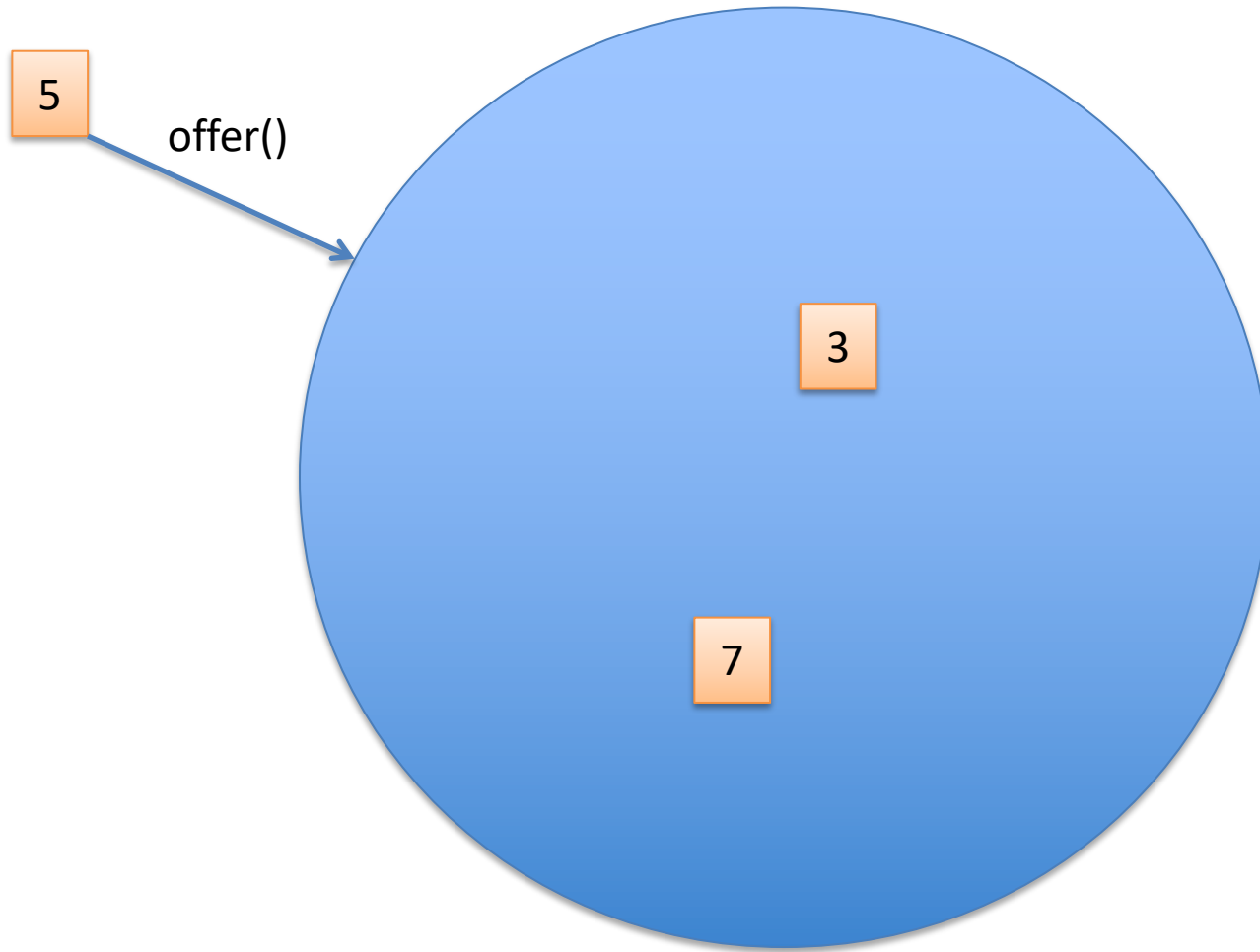
A Priority Queue in Picture



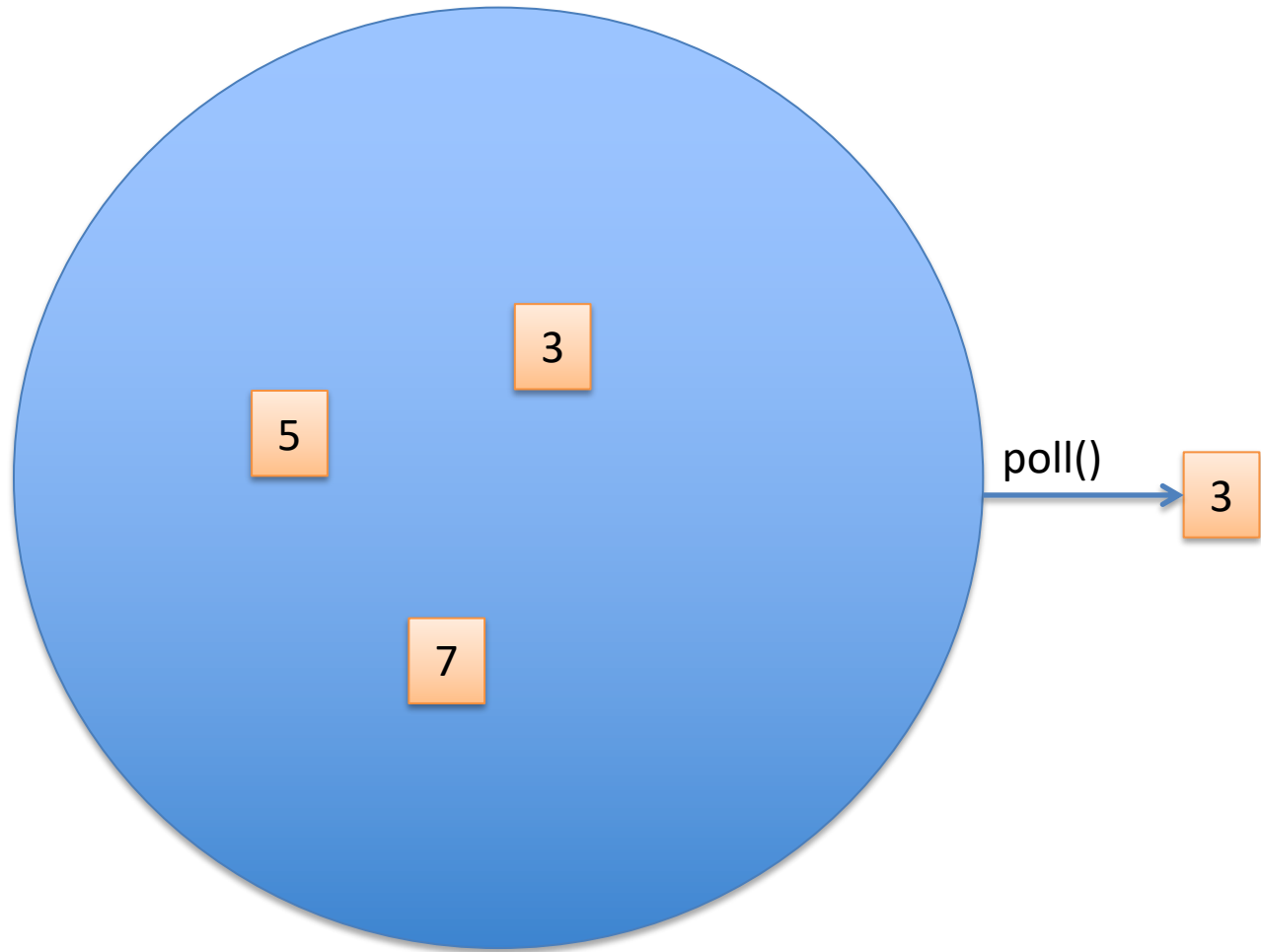
A Priority Queue in Picture



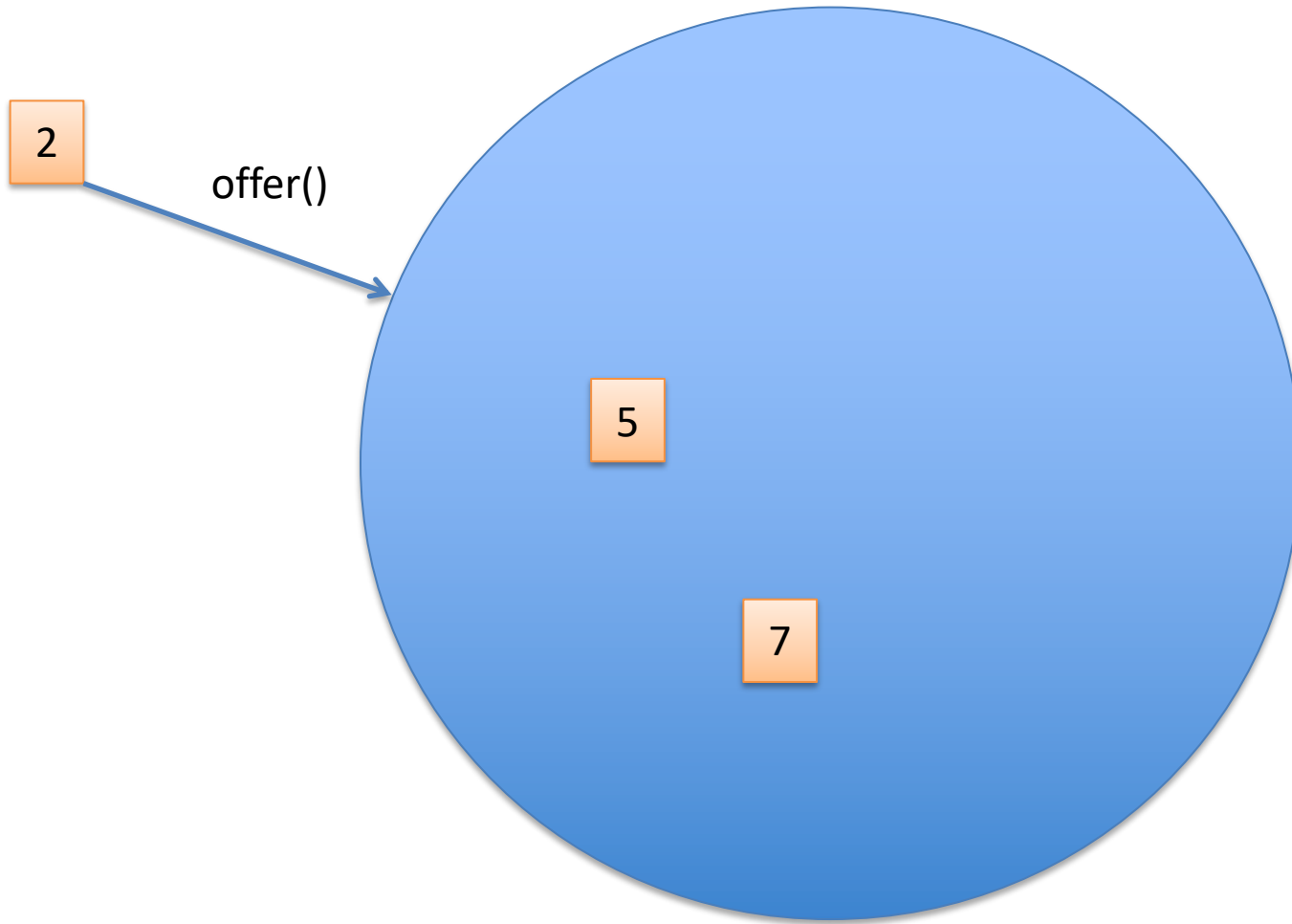
A Priority Queue in Picture



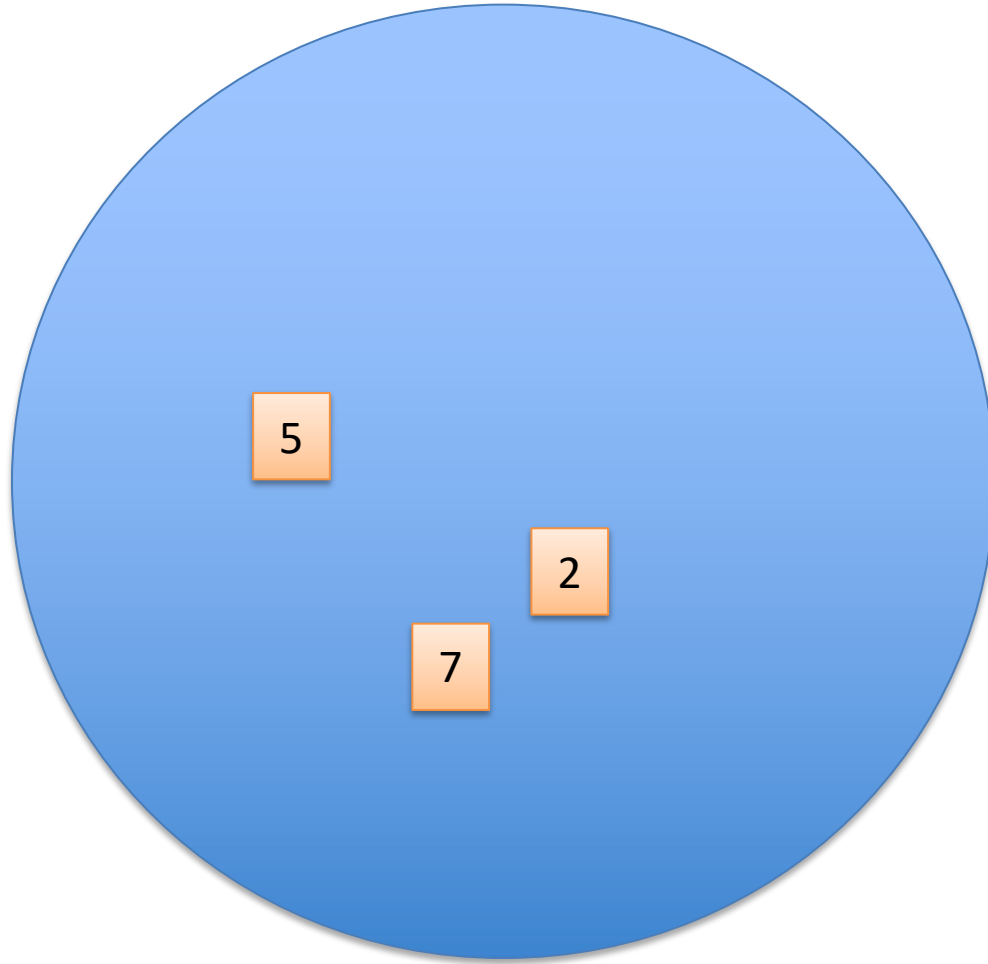
A Priority Queue in Picture



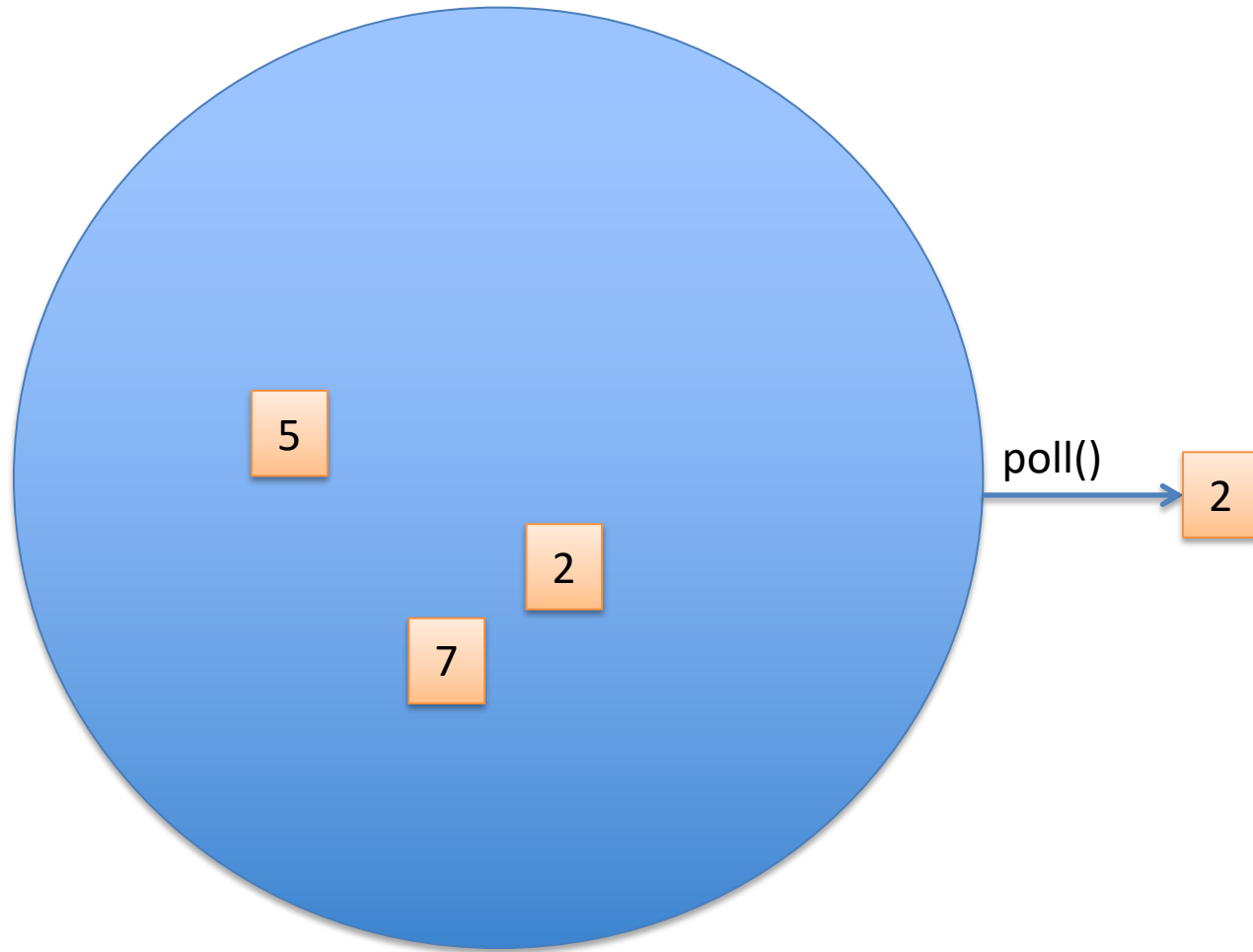
A Priority Queue in Picture



A Priority Queue in Picture



A Priority Queue in Picture



Code

```
public static void main(String args[])
{
    // Creating empty priority queue
    PriorityQueue<Integer> pq =
        new PriorityQueue<Integer>();

    // Adding items to the pq
    pq.offer(7);
    pq.offer(3);
    pq.offer(5);

    // Printing the highest priority element
    System.out.println("Head value :"+ pq.peek());

    // Printing all elements
    System.out.println("The pq elements:");
    Iterator itr = pq.iterator();
    while (itr.hasNext())
        System.out.println(itr.next());

    // Removing the top priority element (or head) and
    // printing the modified pQueue
    pq.poll();
    System.out.println("After removing an element");
    itr = pq.iterator();
    while (itr.hasNext())
        System.out.println(itr.next());

    pq.offer(2);
    System.out.println("After adding 2");
    itr = pq.iterator();
    while (itr.hasNext())
        System.out.println(itr.next());
}
```

Head value using peek function:3

The pq elements:

3

7

5

After removing an element

5

7

After adding 2

2

7

5

How does PriorityQueue compare elements?

Comparable Interface

But what about objects whose class does not implement Comparable Interface?

What about if I want to change the priority of order:
Ascending to Descending

Comparator Interface

Custom Comparator

```
public class Desc implements Comparator<Integer>
{
    // Used for sorting in ascending order of
    // roll name
    public int compare(Integer a, Integer b)
    {
        int i = 0;
        if (a < b) return 1;
        if ( a > b) return -1;
        return 0;
    }
}
```

Output

```
PriorityQueue<Integer> pq =
```

- ```
new PriorityQueue<Integer>(10, new Desc());
```

```
Head value using peek function:7
```

```
The pq elements:
```

```
7
```

```
3
```

```
5
```

```
After removing an element
```

```
5
```

```
3
```

```
After adding 2
```

```
5
```

```
3
```

```
2
```

# Comparable vs Comparator

- Comparable:
  - Compares itself
  - must implements the `java.lang.Comparable` interface
- Comparator:
  - Compares others
  - must implements `java.util.Comparator` interface
- [Ref: http://www.digizol.com/2008/07/java-sorting-comparator-vs-comparable.html](http://www.digizol.com/2008/07/java-sorting-comparator-vs-comparable.html)

**HASHMAP**

# Example

```
static void printFreq(int arr[])
{
 // Creates an empty HashMap
 HashMap<Integer, Integer> hmap =
 new HashMap<Integer, Integer>();

 // Traverse through the given array
 for (int i = 0; i < arr.length; i++)
 {
 Integer c = hmap.get(arr[i]);

 // If this is first occurrence of element
 if (hmap.get(arr[i]) == null)
 hmap.put(arr[i], 1);

 // If elements already exists in hash map
 else
 hmap.put(arr[i], ++c);
 }

 // Print result
 for (Map.Entry m:hmap.entrySet())
 System.out.println("Frequency of " + m.getKey() +
 " is " + m.getValue());
}
```

```
int arr[] = {2, 4, 5, 4, 3, 3, 4};
```

```
Frequency of 2 is 1
Frequency of 3 is 2
Frequency of 4 is 3
Frequency of 5 is 1
```

<http://www.geeksforgeeks.org/hashmap-treemap-java/>

# HUFFMAN CODING

# Start with Frequency Table

| Letters | Frequency | Code |
|---------|-----------|------|
| A       | 25        | ?    |
| B       | 20        | ?    |
| C       | 10        | ?    |
| D       | 15        | ?    |
| E       | 30        | ?    |

# Generate Codes

A 25

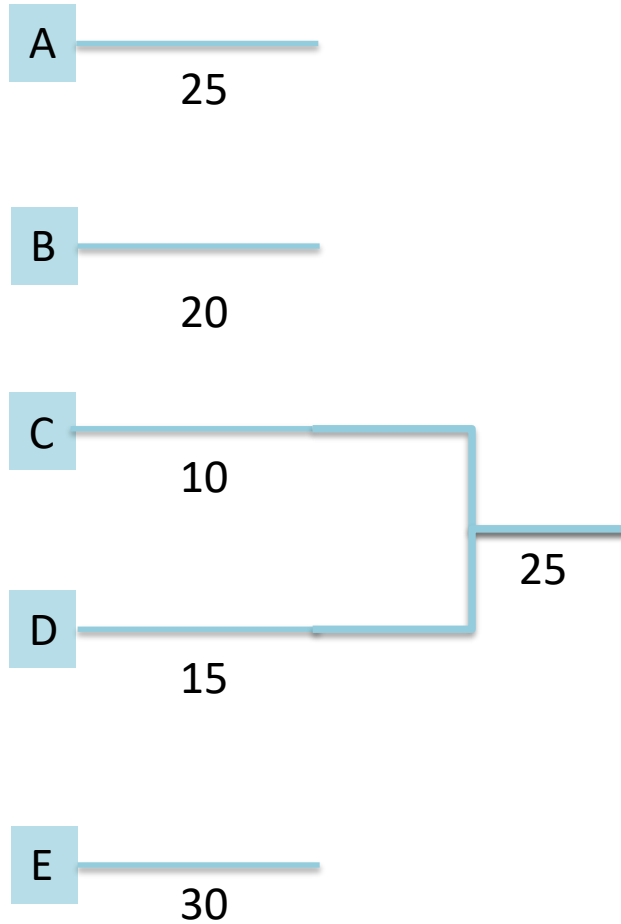
B 20

C 10

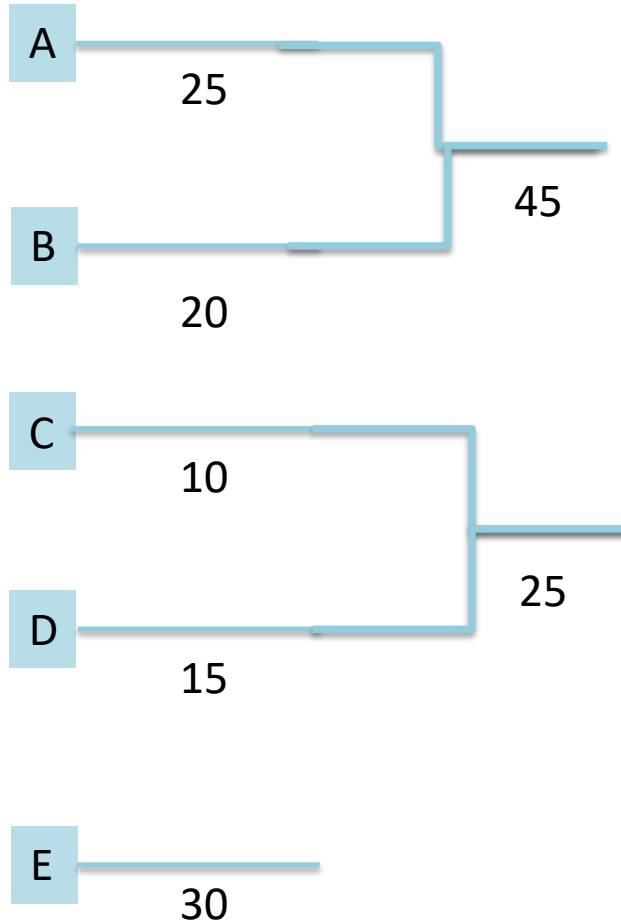
D 15

E 30

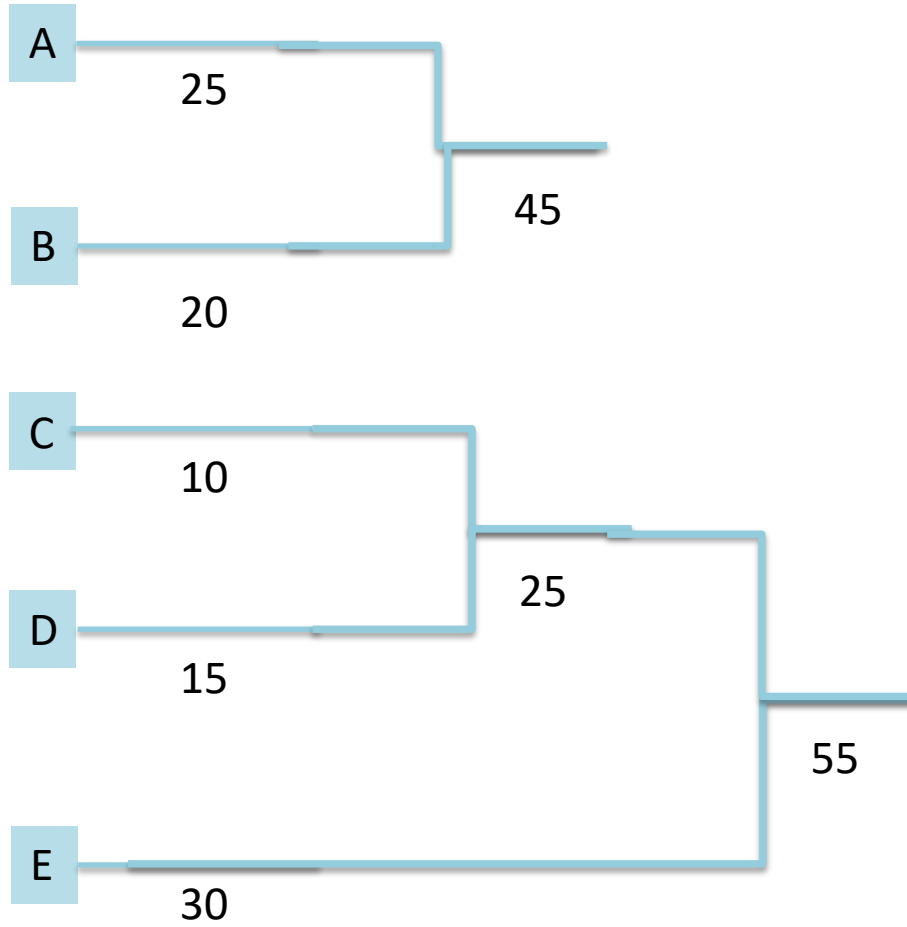
# Generate Codes



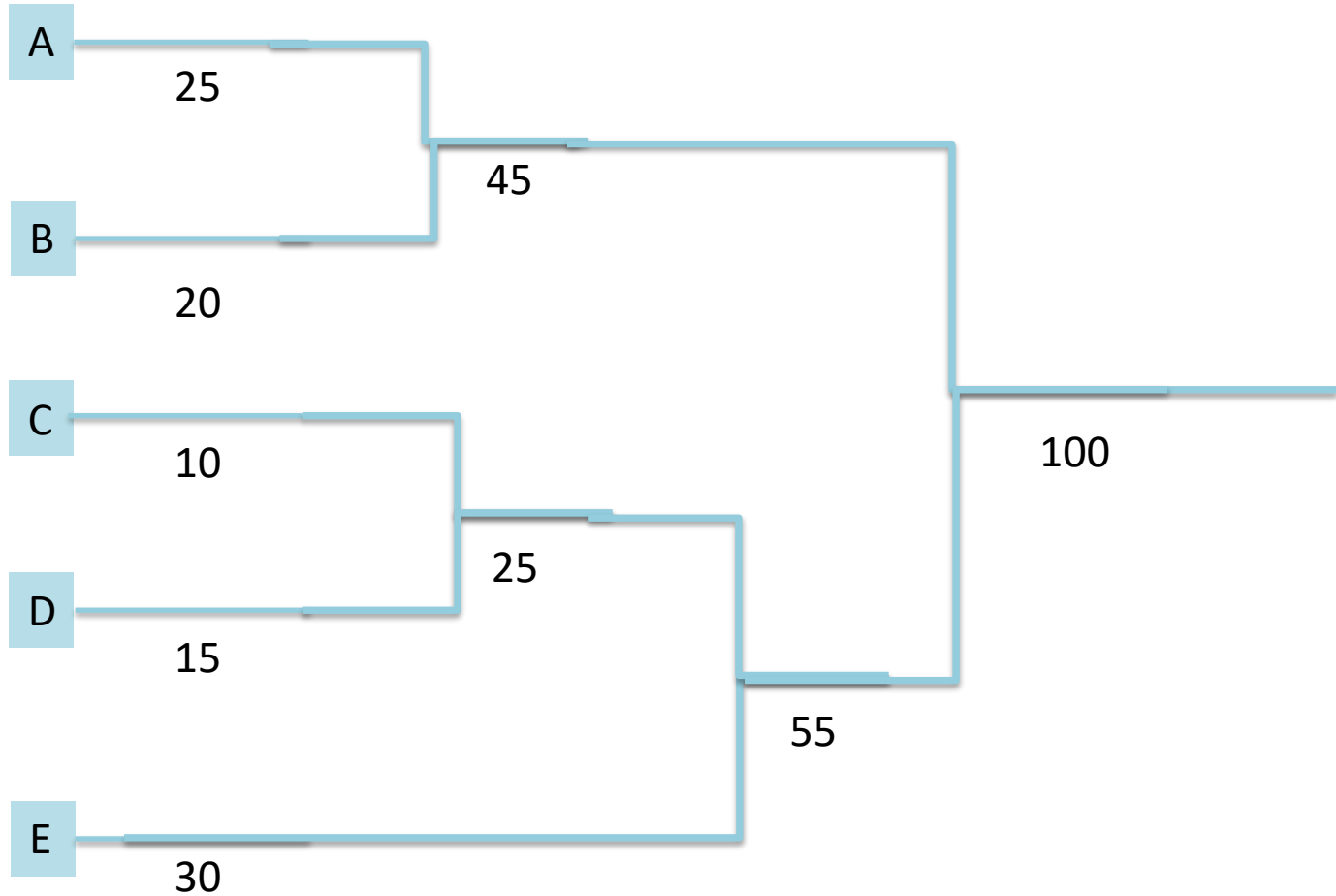
# Generate Codes



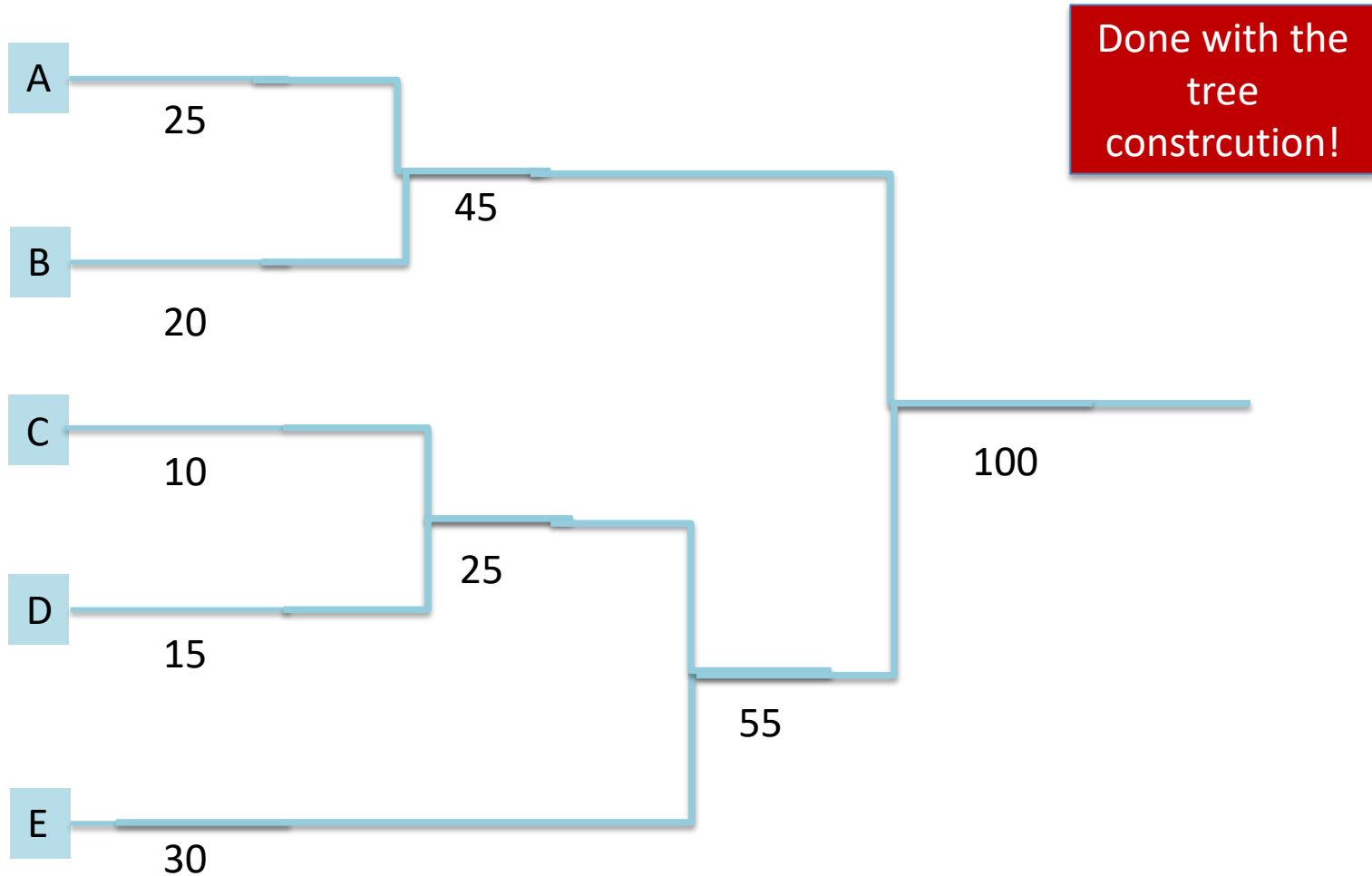
# Generate Codes



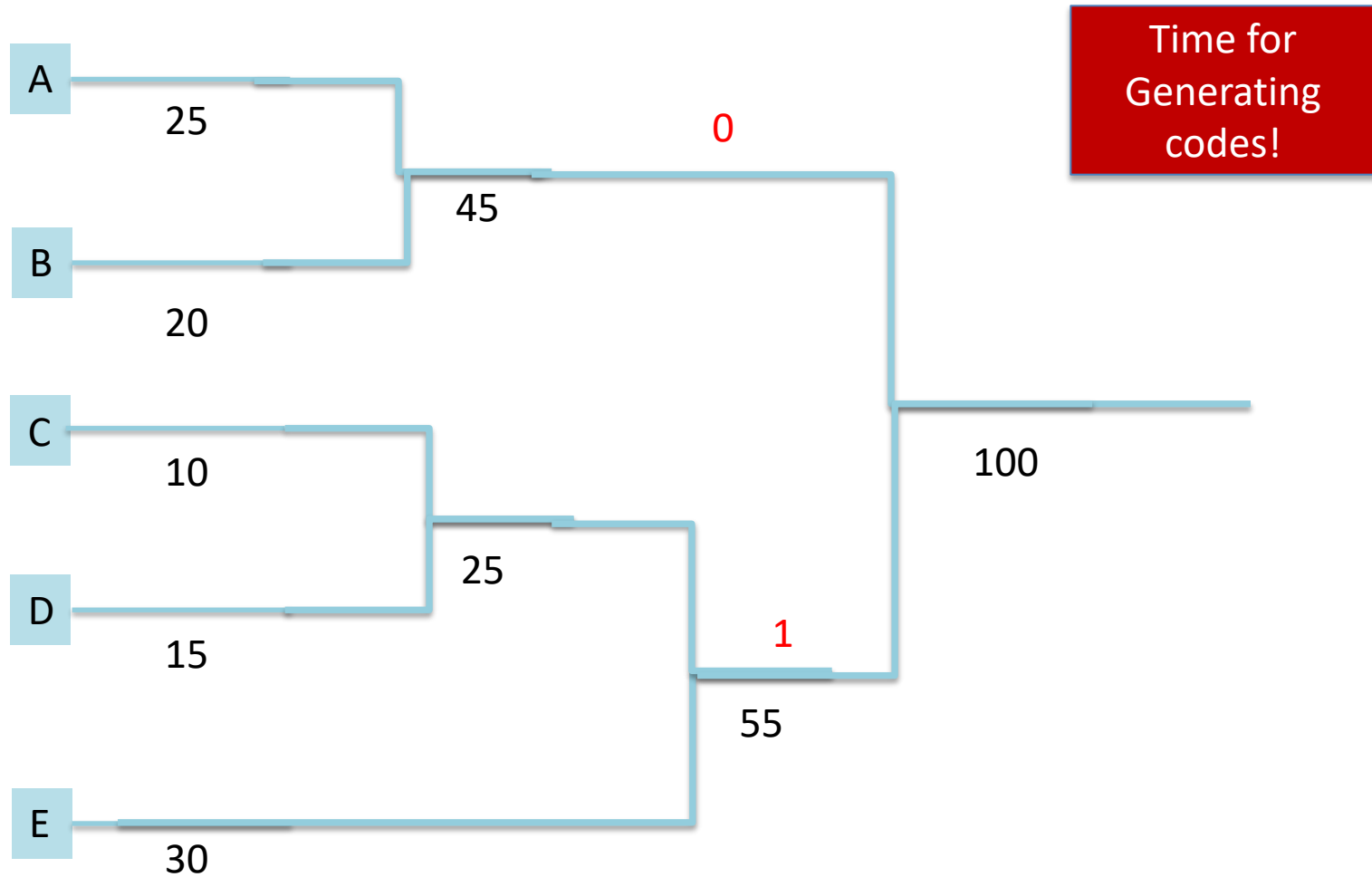
# Generate Codes



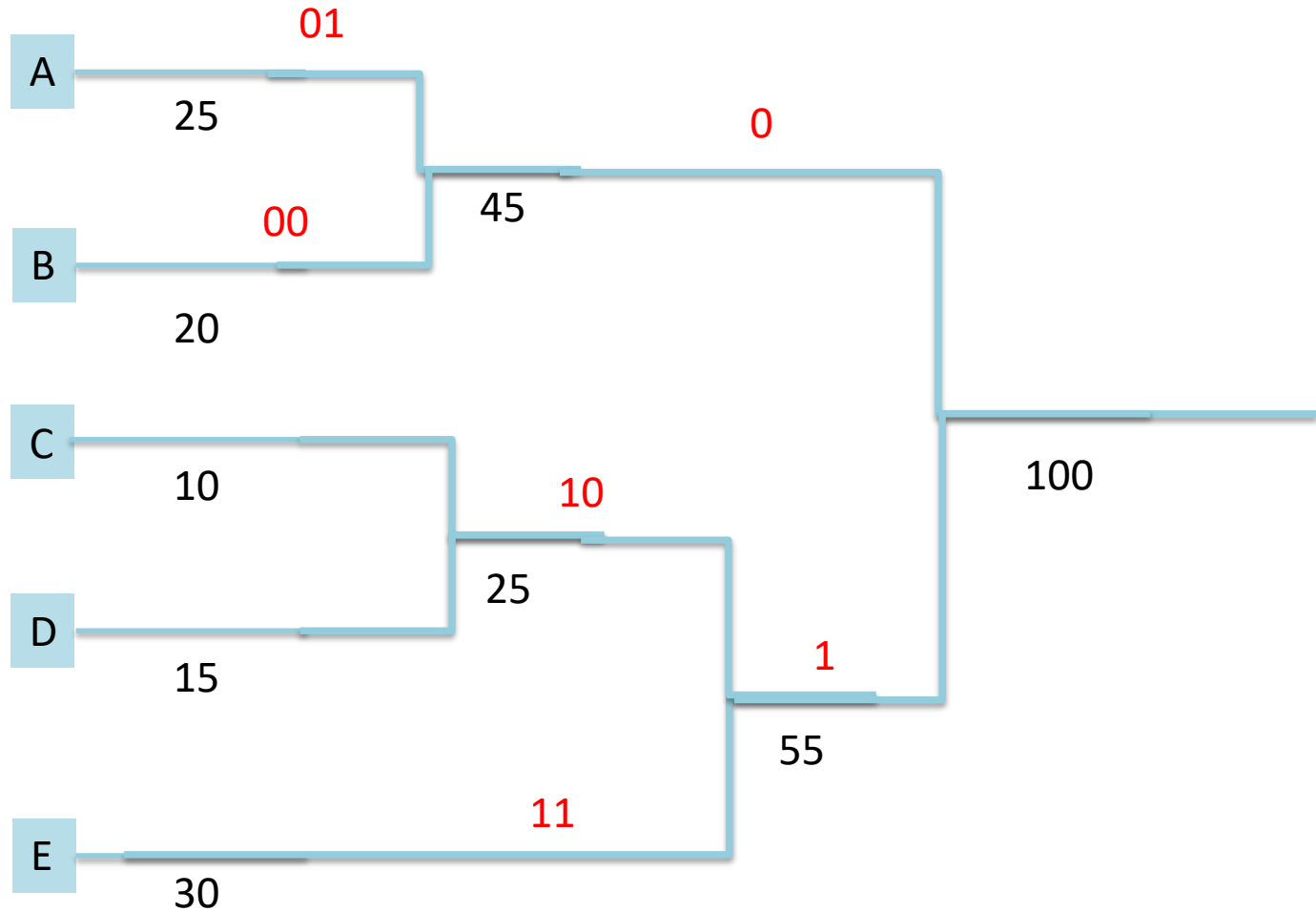
# Generate Codes



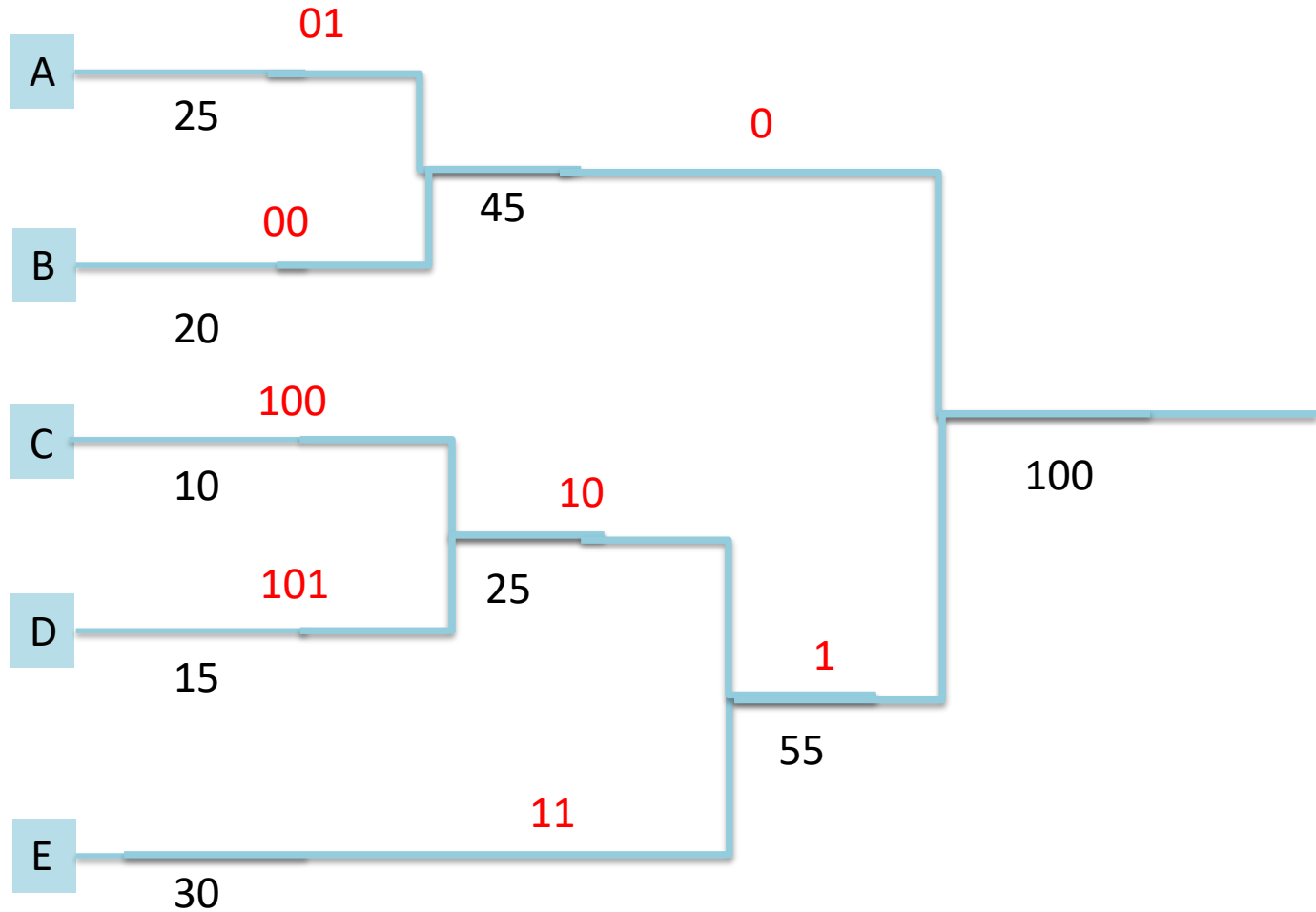
# Generate Codes



# Generate Codes



# Generate Codes



# Huffman Coding

| Letters | Frequency | Code |
|---------|-----------|------|
| A       | 25        | 01   |
| B       | 20        | 00   |
| C       | 10        | 100  |
| D       | 15        | 101  |
| E       | 30        | 11   |

00011011000100

BADCAB

# Let's do another

| Letters | Frequency | Code |
|---------|-----------|------|
| A       |           |      |
| B       |           |      |
| C       |           |      |
| D       |           |      |
| E       |           |      |

# How to implement in Java

- Priority Queue and Tree Node

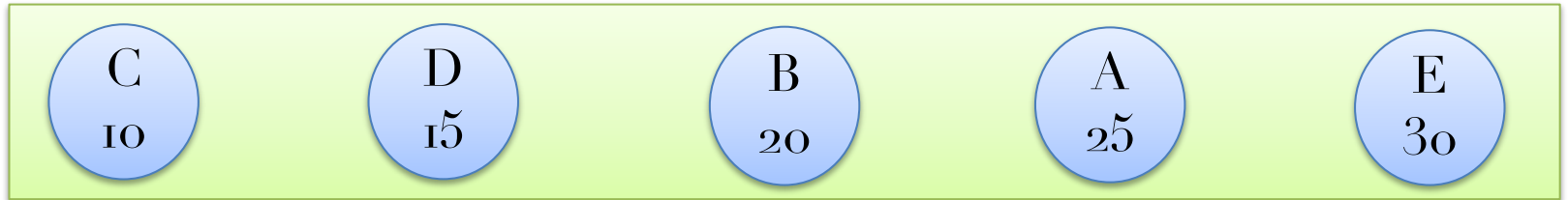
# Recall: How to construct Expression Trees?

4 3 2 + \* 6 3 - 5 \* 3 / -



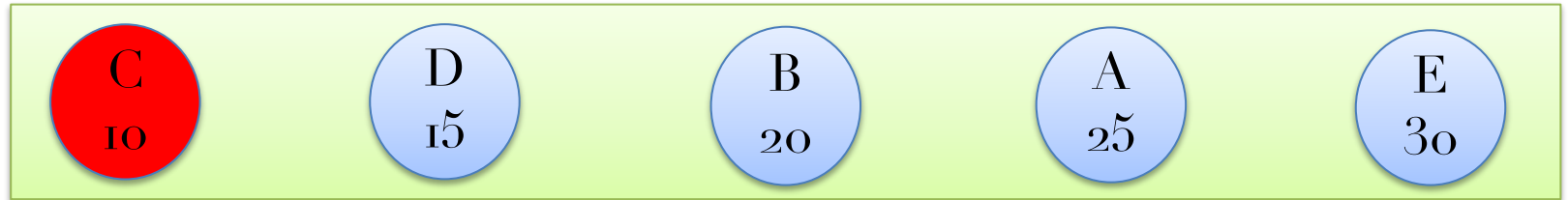
Similar Idea. Instead of using a Stack we will use a  
Priority Queue

# Huffman Code in Java

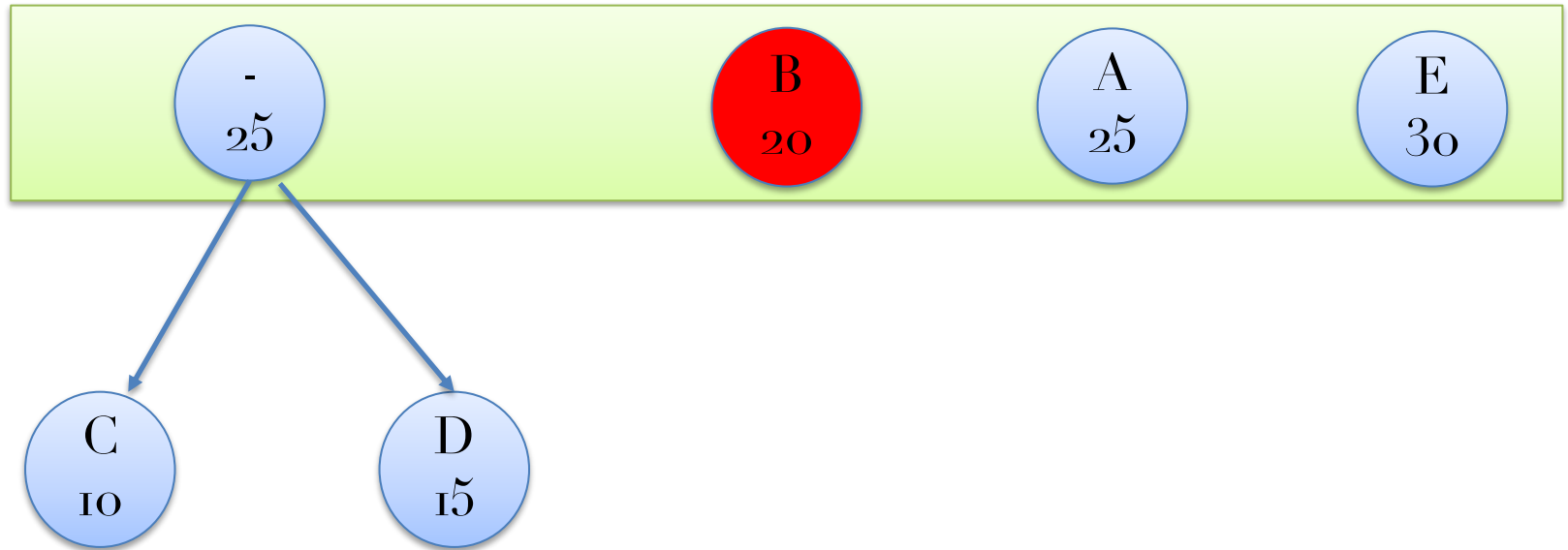


Similar Idea. Instead of using a Stack we will use a  
Priority Queue

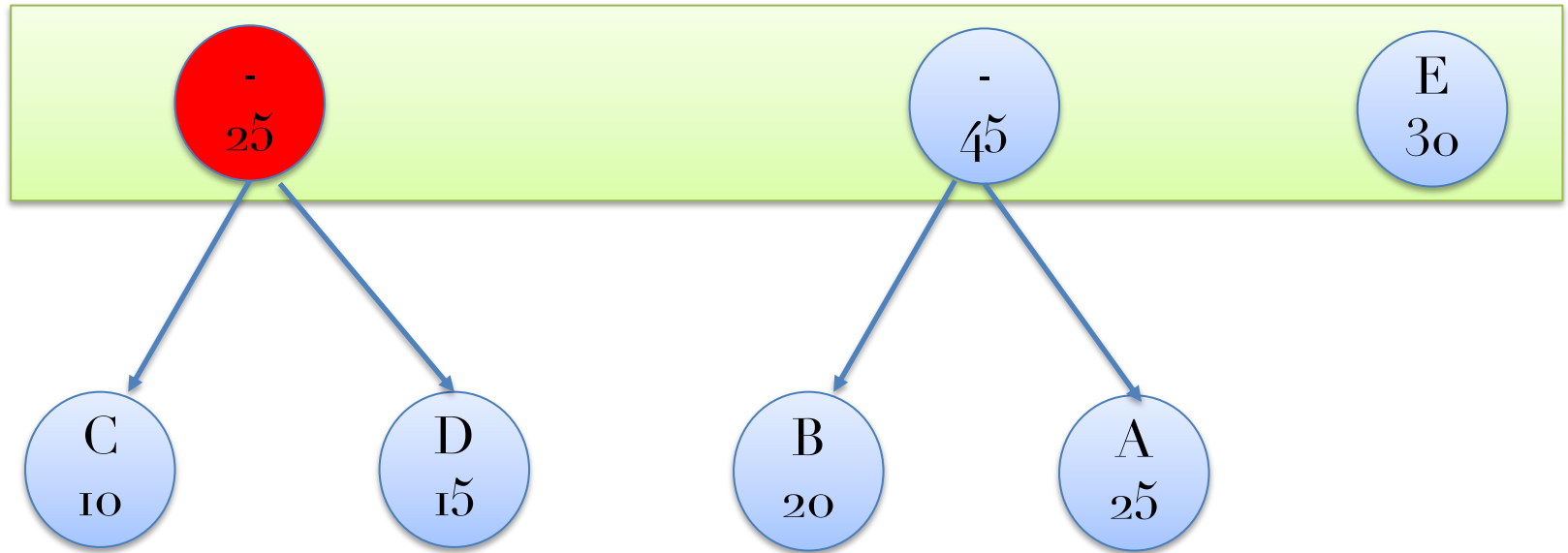
# Huffman Code in Java



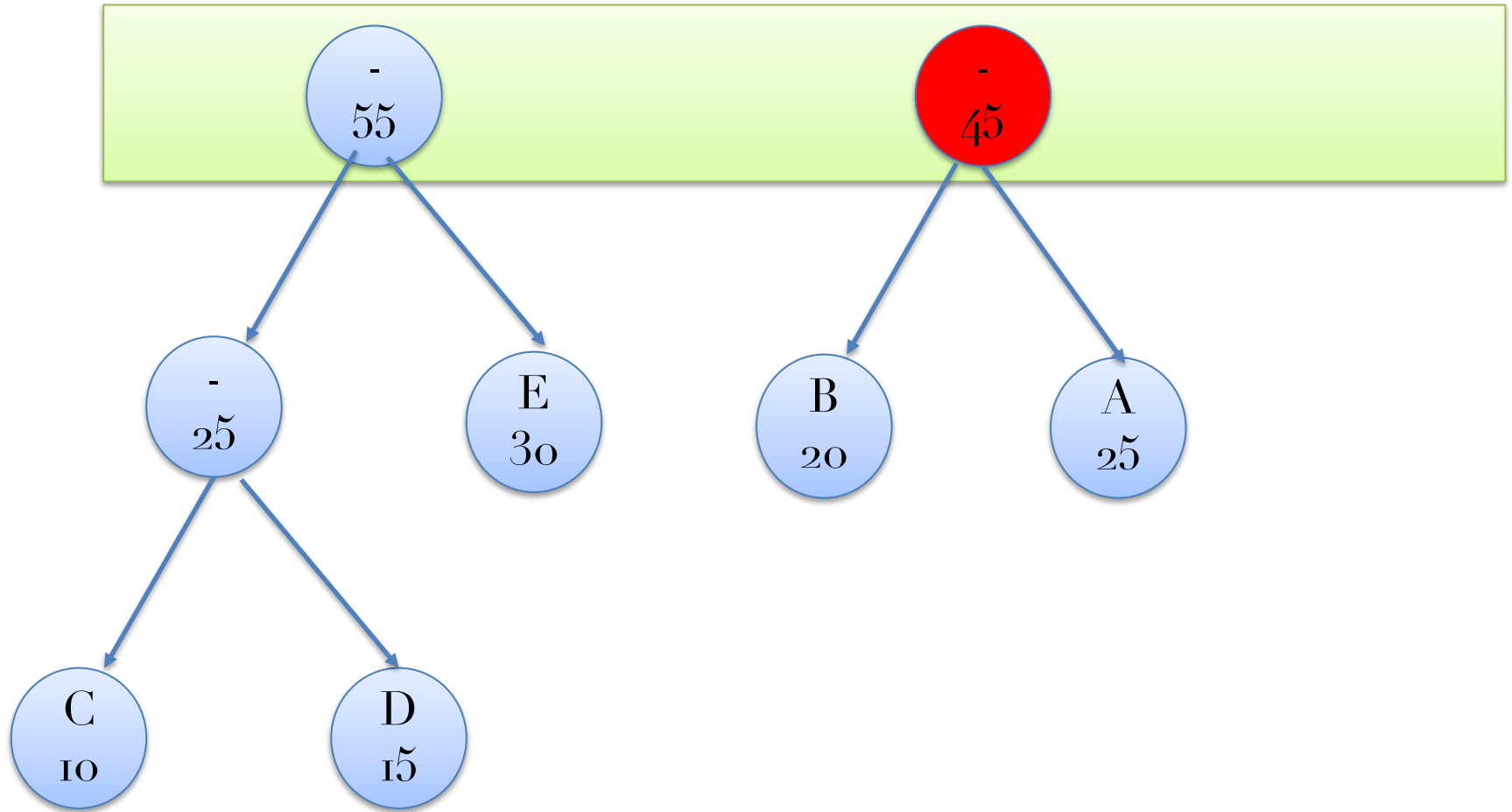
# Huffman Code in Java



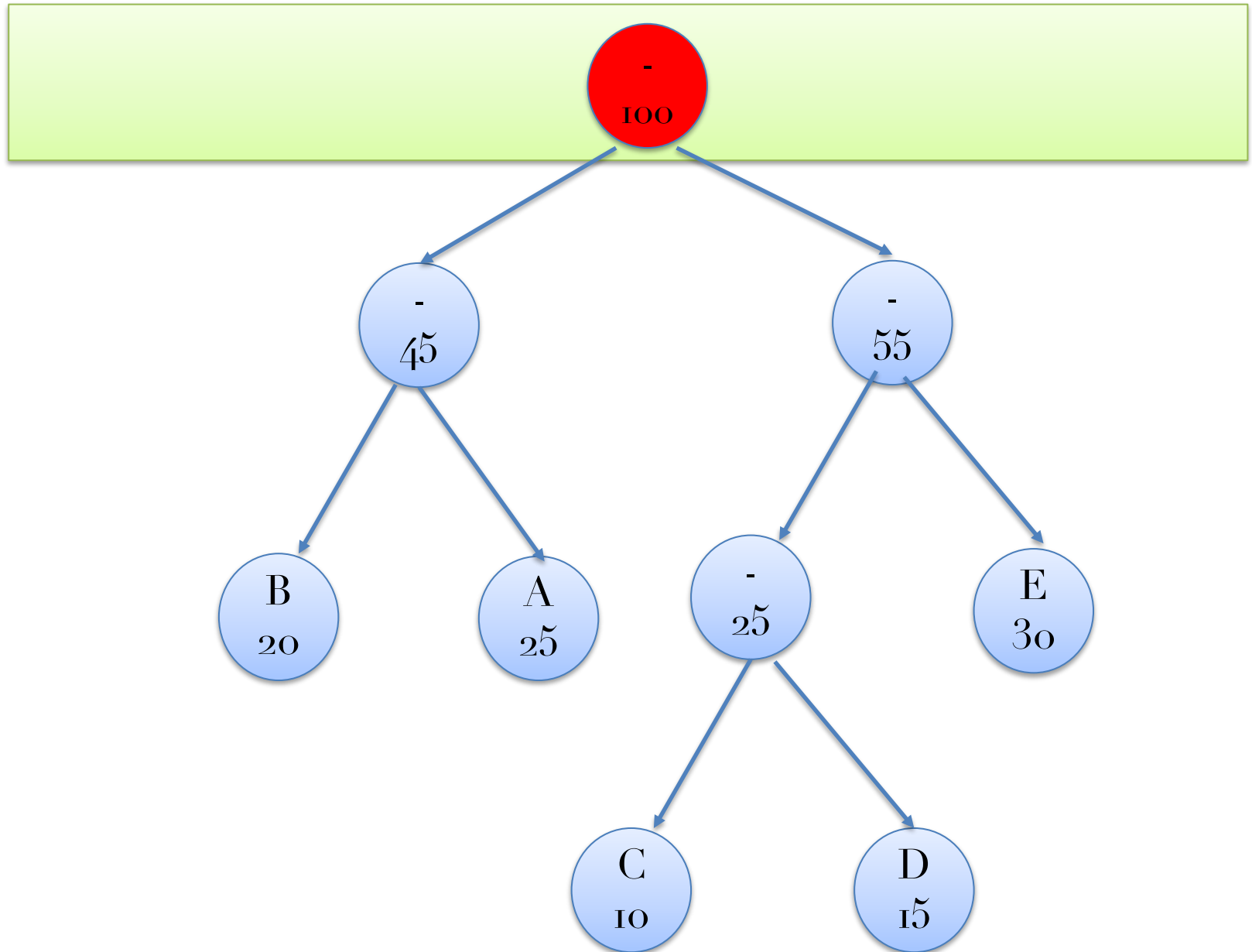
# Huffman Code in Java



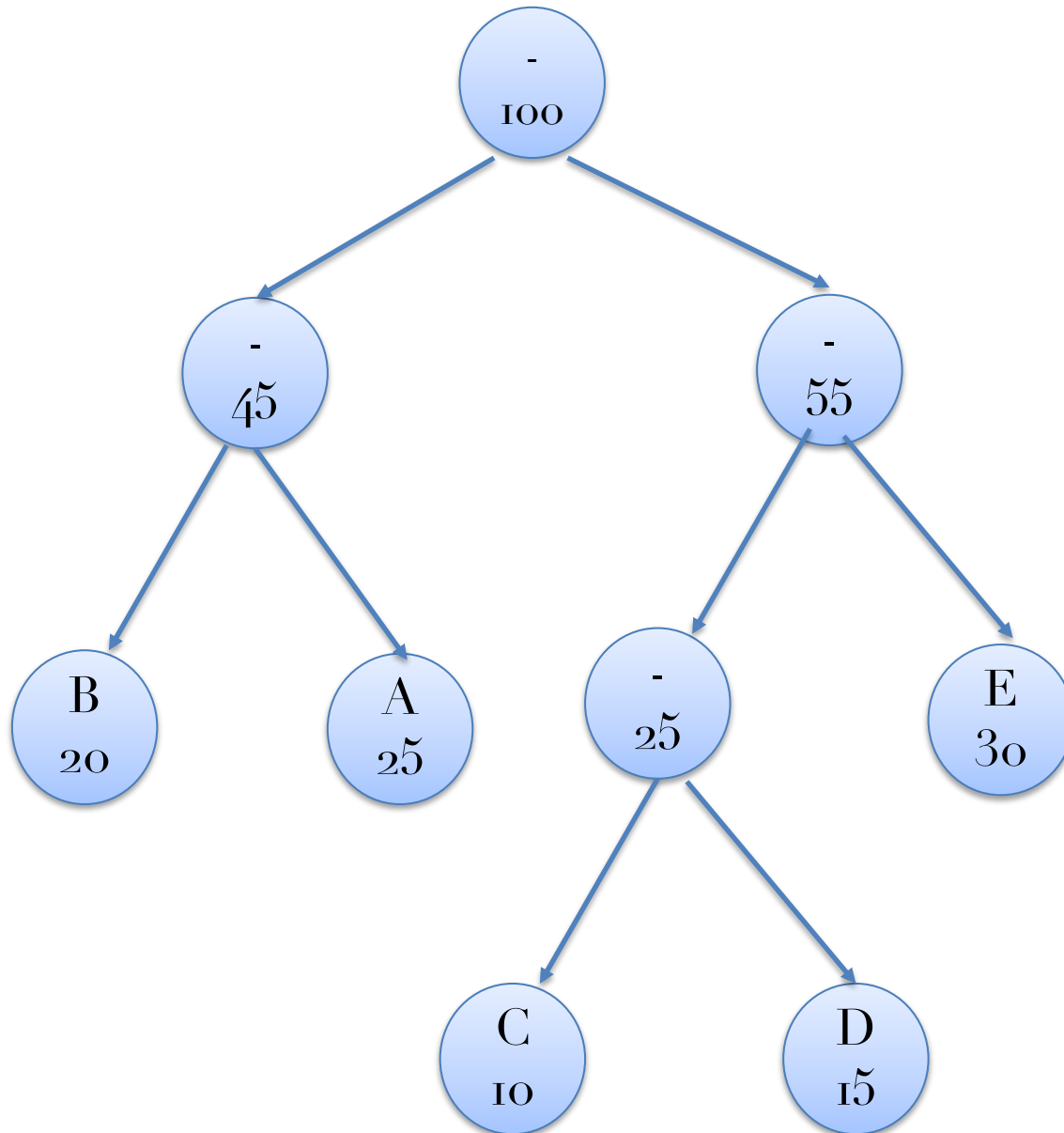
# Huffman Code in Java



# Huffman Code in Java

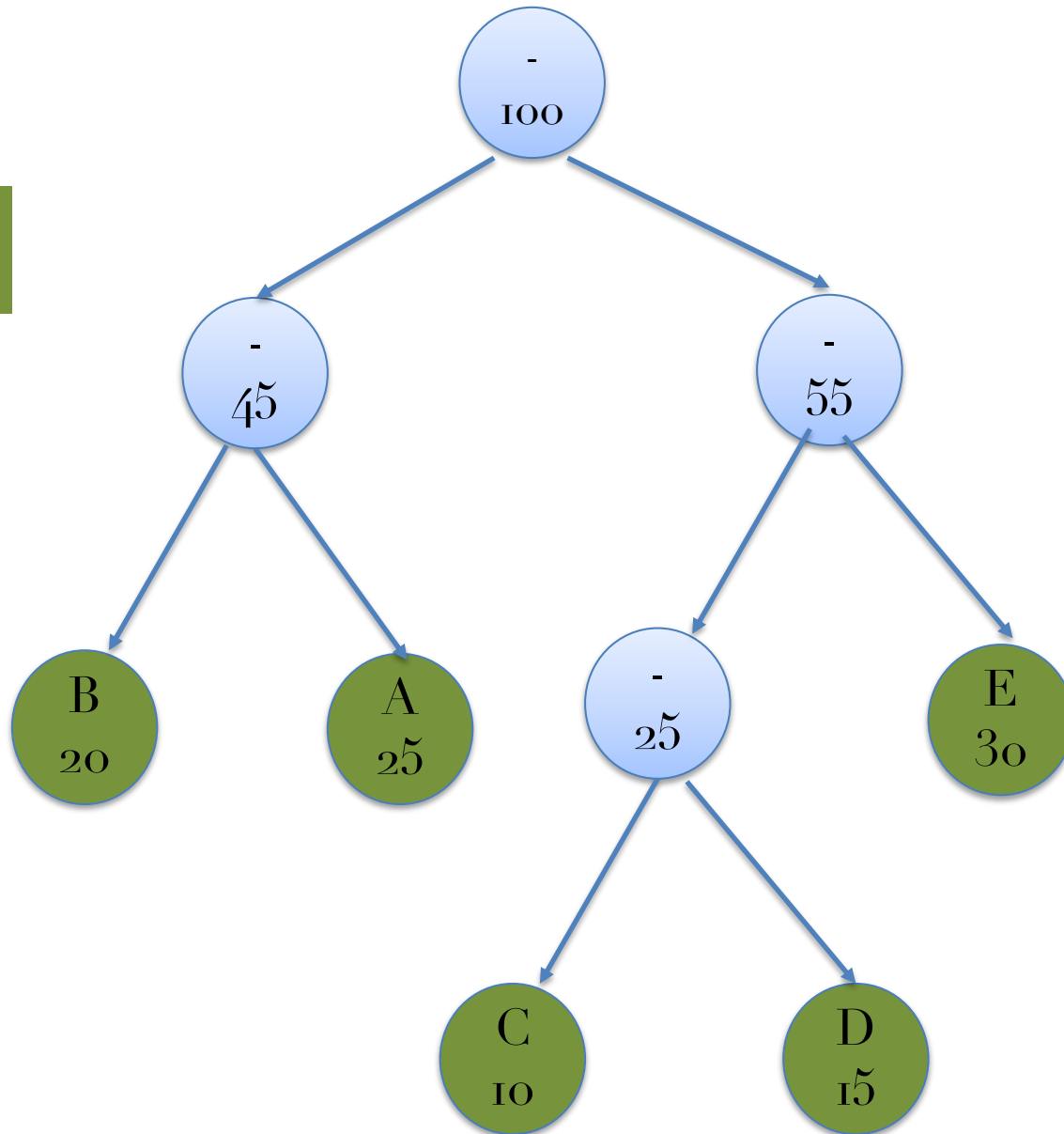


# Huffman Code in Java



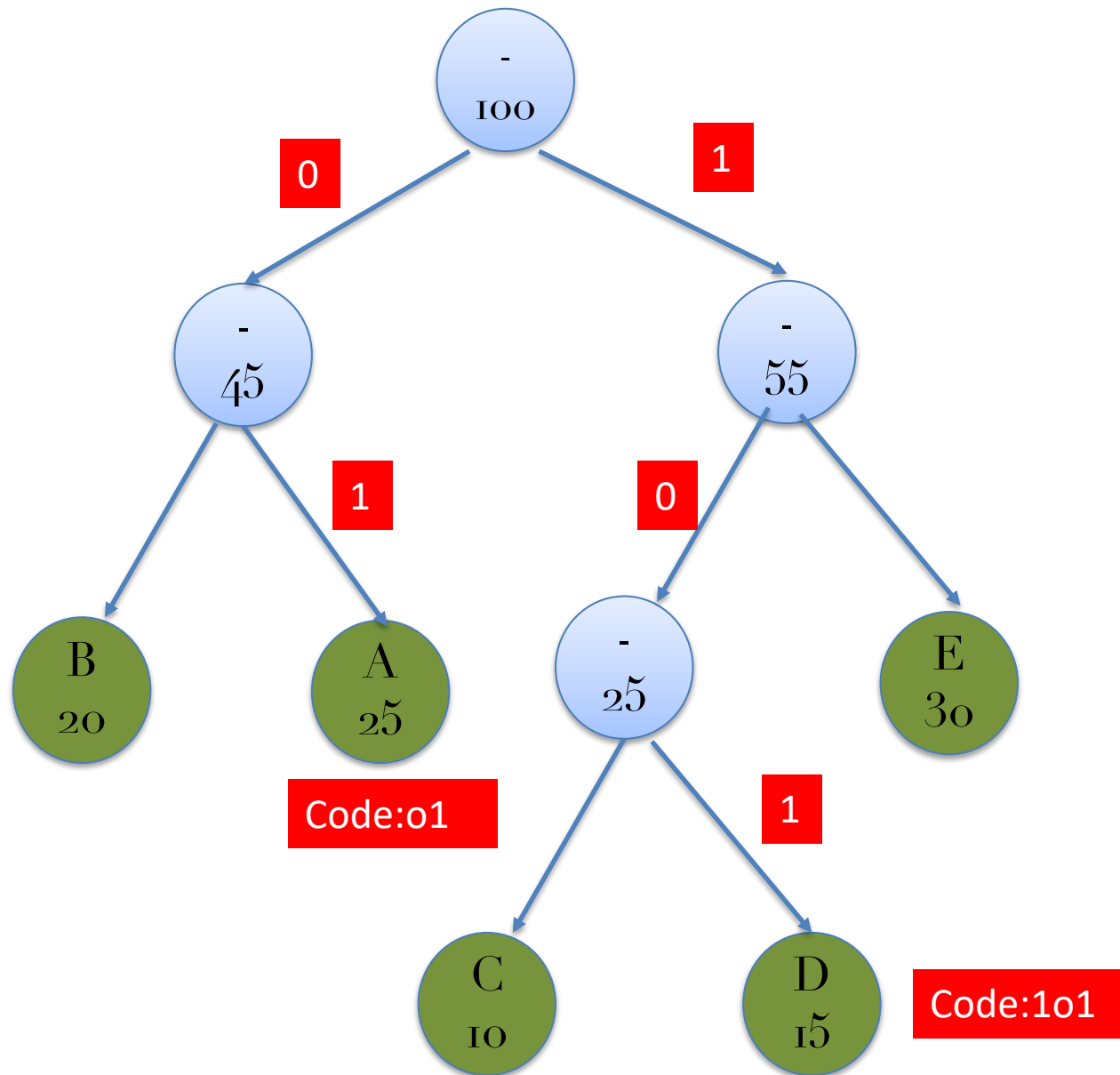
# Huffman Code in Java

We care about  
only the leaves



# Huffman Code in Java

Left 0  
Right 1



# Huffman Coding

| Letters | Frequency | Code |
|---------|-----------|------|
| A       | 25        | 01   |
| B       | 20        | 00   |
| C       | 10        | 100  |
| D       | 15        | 101  |
| E       | 30        | 11   |

00011011000100

BADCAB

# Huffman Coding and Project 3

- Please go through:
- [http://lti.cs.vt.edu/LTI\\_ruby/Books/CS172/html/Huffman.html](http://lti.cs.vt.edu/LTI_ruby/Books/CS172/html/Huffman.html)