#### **SCANNING**

Scanner is responsible for tokenizing source removing comments saving text of identifiers, numbers, strings saving source locations (file, line, column) for error messages

## a DFA for identifiers:



Can be built by hand (ad hoc) or automatically from regular expressions (REs) ad-hoc generally yields the fastest, most compact code by doing lots of special-purpose things automatically-generated scanners can come close, though and are easy to develop and change

A scanner generator builds a DFA automatically from a set of REs Specifically, it constructs a machine that accepts the "language"

identifier | int const | real const | comment | symbol | ...

In other words, a real scanner accepts the alternation of a language's tokens, with a separate final state for each.

We run the scanner over and over to get one token after another.

(Note that theoreticians use "language" to mean a set of strings -- not nec. the valid programs of a programming language.)

Nearly universal rule:

always take the longest possible token from the input thus foobar is foobar and never f or foo or foob more to the point, 3.14159 is a real const and never 3, ., and 14159

An RE generates a regular language; a DFA recognizes it.

The standard Unix lex (flex) outputs C code.

Some other tools produce numeric tables that are read by a separate driver.

The table is the transition function

two-dimensional array indexed by current state and input character entries specify

next state

whether to keep scanning, return a token, or announce an error

Longest-possible token rule means we return only when the next character can't be used to continue the current token.

That next character must generally be saved for the next token.

In some cases you may need to peek at more than one character of lookahead in order to know whether to proceed.

In Pascal, when you had a 3 and you a saw a dot, did you proceed (in hopes of getting 3.14) or did you stop (in fear of getting 3..5)?

In messier cases, you may not be able to get by with any fixed amount of lookahead. In Fortran IV (c. 1962), for example, one had

```
D0 5 I = 1,25 loop
D0 5 I = 1.25 assignment
D0 5,I = 1,25 alternate syntax for loop, f77
```

For most languages it suffices to remember we were in a potentially final state, and save enough information that we can back up to it if we get stuck later.

For some languages (famously, Fortran), that isn't enough.

Sometimes need semantic information in order to scan (yuck).

-----

## Building a scanner from regular expressions

## multi-step process

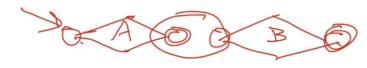
- 1) write REs by hand, including for whitespace and comments, but with identifiers and reserve words (keywords) combined
- 2) build NFA from REs
- 3) build DFA from NFA
- 4) minimize DFA
- 5) add extra logic to
  - o implement the longest-possible-token rule, with backup
  - discard white space and comments (i.e., start over when you realize that's what you found)
  - o distinguish reserve words from identifiers
  - o save text of "interesting" tokens
  - o tag returned tokens with location and text
  - o return an extra \$\$ token at end-of-file

Step (2) is inductive. It starts with a trivial DFA to accept a single character:

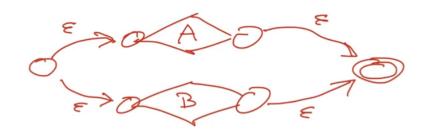


Note that this machine has a single start state, a single final state, no transitions into the start state, and no transitions out of the final state. We'll maintain these invariants in three inductive steps:

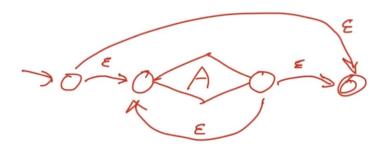
Concatenation (A B):



Alternation (A | B):



Kleene closure (A\*):



Step (3) uses what's called a "set of subsets" construction. Step (4) divides the states of an initial DFA into progressively finer equivalences classes, until it can prove that additional refinement makes no difference.

Example 1 (in the book): real numbers (no exponential notation)

 $RN = d^*(.d|d.)d^*$ 

14-state NFA results from construction

5-state subset DFA

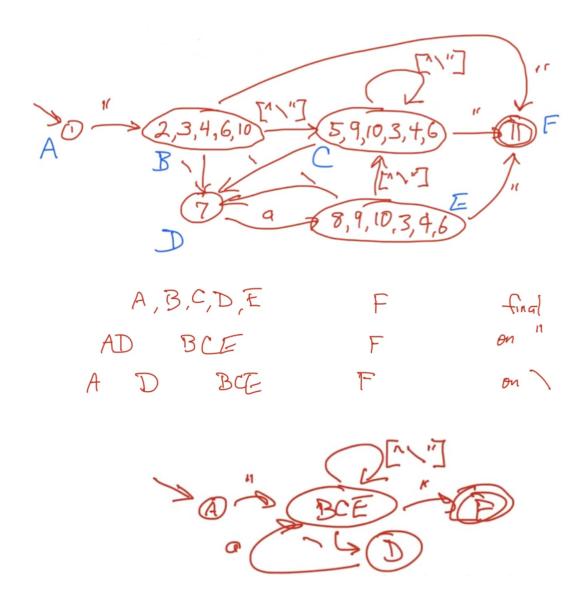
4-state minimal DFA

Example 2: character strings with optional backslash-escaped quotes

11-state NFA results from construction

6-state subset DFA

4-state minimal DFA



In these two examples, the DFA was smaller than the original NFA. Is that always the case?

No! Quite the contrary.

Example 3: subset of  $(a|b|c)^*$  in which some letter appears at least 3 times.

```
RE (one possibility):

(a|b|c)* ( (a|b)*c(a|b)*c(a|b)*c(a|b)*

| (c|b)*a(c|b)*a(c|b)*a(c|b)*

| (a|c)*b(a|c)*b(a|c)*b(a|c)* ) (a|b|c)*
```

## exists an 8-state NFA minimal DFA has 28 states

See the PLP Companion Site, Sec. 2.4.1

That NFA, of course, doesn't come from the standard construction. Are there any that *do*, and for which the DFA is bigger yet? Absolutely!

Example 4: subset of  $(0|1|2|3|4|5|6|7|8|9)^*$  in which some digit appears at least 10 times.

minimal DFA has 10,000,000,001 states one RE is

```
(0|1|2|3|4|5|6|7|8|9)*
   ((1|2|3|4|5|6|7|8|9)*0(1|2|3|4|5|6|7|8|9)*0
    (1|2|3|4|5|6|7|8|9)*0 (1|2|3|4|5|6|7|8|9)*0
    (1|2|3|4|5|6|7|8|9)*0 (1|2|3|4|5|6|7|8|9)*0
   (1|2|3|4|5|6|7|8|9)*0 (1|2|3|4|5|6|7|8|9)*0
   (1|2|3|4|5|6|7|8|9)* 0 (1|2|3|4|5|6|7|8|9)* 0 (1|2|3|4|5|6|7|8|9)*)
   ((0|2|3|4|5|6|7|8|9)*1(0|2|3|4|5|6|7|8|9)*1
    (0|2|3|4|5|6|7|8|9)*1 (0|2|3|4|5|6|7|8|9)*1
    (0|2|3|4|5|6|7|8|9)*1 (0|2|3|4|5|6|7|8|9)*1
    (0|2|3|4|5|6|7|8|9)*1 (0|2|3|4|5|6|7|8|9)*1
    (0|2|3|4|5|6|7|8|9)*1(0|2|3|4|5|6|7|8|9)*1(0|2|3|4|5|6|7|8|9)*)
   ((0|1|2|3|4|5|6|7|8)*9 (0|1|2|3|4|5|6|7|8)*9
    (0|1|2|3|4|5|6|7|8)*9 (0|1|2|3|4|5|6|7|8)*9
    (0|1|2|3|4|5|6|7|8)*9 (0|1|2|3|4|5|6|7|8)*9
    (0|1|2|3|4|5|6|7|8)*9 (0|1|2|3|4|5|6|7|8)*9
    (0|1|2|3|4|5|6|7|8)*9 (0|1|2|3|4|5|6|7|8)*9 (0|1|2|3|4|5|6|7|8)*)
(0|1|2|3|4|5|6|7|8|9)*
```

anybody believe the automatically constructed NFA for that has 10 billion states?

-----

Recall that real scanner accepts alternation of tokens, with a separate final state for each. Scanner generator

- starts with NFAs for all the separate tokens
- creates a new start state with an E-transition to the start state of each token NFA
- turns that into a DFA
- runs the minimization algorithm starting not with two classes (final and non-final) but with K+1: non-final, final for token T1, final for token T2, ..., final for token TK.

Try Exercise 2.5 in the book!

In most compilers, the parser drives the front end. The scanner is a subroutine (function) called by the parser.

-----

We can also build a RE from a DFA (as shown in Section 2.4.1 on the PLP companion site). This completes a proof that the two notations are equally powerful. Nobody does this in practice, however; it amounts to converting the computer-friendly notation into a human-friendly notation, and we usually want to go the other way.

-----

In a real compiler, the input may have errors, including lexical errors. Consider, in Java or C, the input

int myVaria\$ble

That dollar sign isn't supposed to be there.

What should a scanner do?

Generally suffices to

return the longest token that starts at the beginning of the

remaining part of the input program

(after deleting white space and comments)

or, if there isn't a valid token starting there, delete characters until there is, print an error message reporting the deletion, and return the token found

Pseudocode for a table-driver scanner can be found in the text.

## **CONTEXT FREE GRAMMARS**

Here's a grammar for a simple desk calculator language (from the intro lecture notes):

```
1 pgm
                \rightarrow stmt list $$
2 stmt list
               \rightarrow stmt list stmt | \epsilon
                \rightarrow id := expr | read id | write expr
3 stmt
               \rightarrow term | expr add op term
4 expr
               → factor | term mult_op factor
5 term
6 factor
               \rightarrow (expr) | id | lit
               \rightarrow + | -
7 add op
               \rightarrow * \mid /
8 mult_op
```

[This happens to be a "bottom-up" grammar -- one of the two kinds that are easy to parse.]

```
Terminology:
    CF grammar
    symbols
        terminals (tokens)
        non-terminals
    start symbol
    production
    derivation (see example below)
    left-most
    right-most (canonical)
    sentential form
```

[ Useless symbols: non-terminals that can't derive a token string, or tokens that can't be derived. We will assume we have none of these. They can be detected and removed automatically and efficiently. ]

.....

```
Consider the program
  read A
  read B
  sum := A + B
  write sum
  write sum / 2
```

Derivation using the above grammar:

```
program
stmt list $$
stmt list stmt $$
stmt list write expr $$
stmt list write term $$
stmt list write term mult_op factor $$
stmt list write term mult_op lit $$
stmt list write term / lit $$
stmt list write factor / lit $$
stmt_list write id / lit $$
stmt list stmt write id / lit $$
stmt list write expr write id / lit $$
stmt list write term write id / lit $$
stmt list write factor write id / lit $$
stmt list write id write id / lit $$
stmt list stmt write id write id / lit $$
stmt list id := expr write id write id / lit $$
stmt_list id := expr add_op term write id write id / lit $$
stmt_list id := expr add_op factor write id write id / lit $$
stmt list id := expr add op id write id write id / lit $$
stmt list id := expr + id write id write id / lit $$
stmt list id := term + id write id write id / lit $$
stmt list id := factor + id write id write id / lit $$
stmt_list id := id + id write id write id / lit $$
stmt_list stmt id := id + id write id write id / lit $$
stmt list read id id := id + id write id write id / lit $$
stmt list stmt read id id := id + id write id write id / lit $$
stmt list read id read id id := id + id write id write id / lit $$
read id read id id := id + id write id write id / lit $$
```

Each line is a sentential form. By definition that's a string of grammar symbols that occurs in the derivation of some string of terminals from the start symbol.

This is a "canonical" (right-most) derivation: at each step we have expanded the right-most non-terminal in the current sentential form. So each line is a "right sentential form."

Bottom-up parsers that read their input left-to-right to discover right-most derivations.

Top-down parsers that read their input left-to-right discover left-most derivations.

-----

A Little Theory

A context-free grammar (CFG) is a *generator* for a CF language. A parser is a language *recognizer*.

There is an infinite number of grammars for every context-free language. But not all grammars are equal!

For any CFG we can create a parser that runs in O(n^3) time. Early's algorithm (~emulation of an NPDA) Cocke-Younger-Kasami (CYK) algorithm (dynamic programming)

 $O(n^3)$  time is clearly unacceptable for a parser in a compiler.

There are large classes of grammars for which we can build parsers that run in linear time. The two most important classes are called LL and LR.

LL stands for 'Left-to-right, Leftmost derivation'. LR stands for 'Left-to-right, Rightmost derivation'.

We'll focus on LL parsing, which is what you're going to be using in your next assignment. The LR class is larger, but

- most programming languages have LL grammars
   (or something close enough to use with a couple hacks)
- LL parsing is generally simpler and easier to understand.

You commonly see LL or LR (or whatever) written with a number in

parentheses after it. This number indicates how many tokens of look-ahead are required in order to parse. Most but not all real compilers use one token of lookahead.

Some compilers (e.g., for Fortran) have hacks to get more lookahead in special cases.

The open-source compiler-compiler ANTLR is LL(k).

LL parsers are also called 'top-down', or 'predictive' parsers. LR parsers are also called 'bottom-up', or 'shift-reduce' parsers. More on this in the next lecture.

There are several important sub-classes of LR parsers, including SLR and LALR. See Sec. 2.3.4 in the text (unassigned) if you're curious.

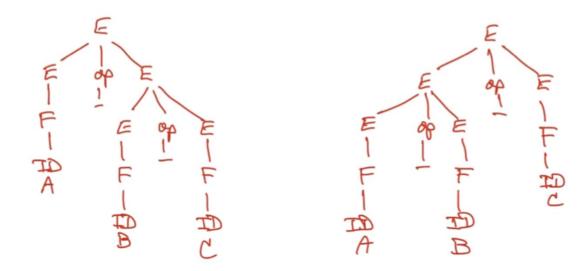
- Every LL(1) grammar is also LR(1), though right recursion in productions (analogous to left recursion, discussed in more detail in the next lecture) tends to require very deep stacks and complicates semantic analysis.
- Most but not all LL(1) grammars are also LALR(1).
- Every CF \*language\* that can be parsed deterministically has an SLR(1) grammar (which is automatically LALR(1) and LR(1)).
- Every deterministic CFL with the "prefix property" (no valid string is a prefix of another valid string -- every language augmented with an end-of-file marker fits the bill) has an LR(0) grammar, but it's almost certainly too ugly to use.

What makes a grammar "nice"?

It's particularly important that it be UNAMBIGUOUS -- no two parse trees for the same string. Consider what would have happened if bottom-up productions 4 and 5 were

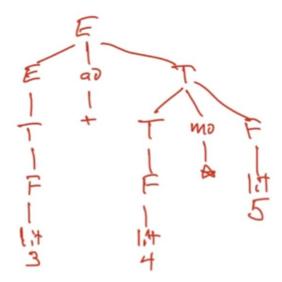
expr o factor | expr op expr

This gives us two parse trees for A - B - C:



Also nice if the parse trees reflect semantic structure, but that's not essential. Our bottom-up calculator grammar nicely captures the notion of precedence:

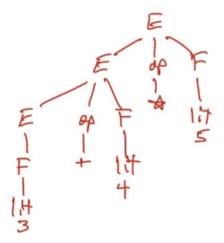
Here's a bottom-up parse tree for 3 + 4 \* 5:



Consider what would have happened if productions 4 and 5 in the bottom-up grammar were

$$expr o factor \mid expr op factor$$

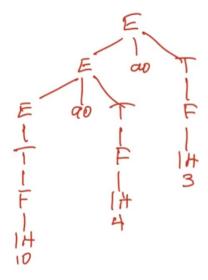
This gives us a different parse tree for 3 + 4 \* 5:



There is nothing *wrong* with this grammar or this tree, but you can see why the first one might be easier to translate into a syntax tree.

Our grammar also captures the notion of left associativity:

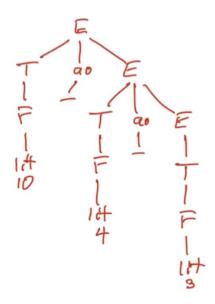
Here's a bottom-up parse tree for 10 - 4 - 3:



Consider what would have happened if production 4 was

$$expr \longrightarrow term \mid term \ add\_op \ expr$$

This gives us a different parse tree for 10 - 4 - 3:



Again, there is nothing *wrong* with this grammar or this tree, but you can see why the first one might be easier to translate into a syntax tree.

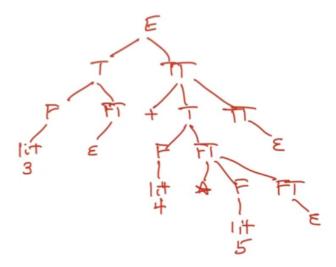
-----

Here is an LL(1) (top-down) grammar for the same language:

```
1
  pgm
               \rightarrow stmt_list $$
               \rightarrow stmt stmt_list | \epsilon
2
  stmt list
               \rightarrow id := expr | read id | write expr
3
  stmt
               → term term_tail
4
  expr
               → add_op term term_tail | ε
5
  term_tail
               → factor fact_tail
6
  term
               → mult_op factor fact_tail | ε
7
  fact tail
  factor
               \rightarrow (expr) | id | lit
8
  add_op
9
10 mult_op
```

Like the bottom-up grammar, the top-down one captures precedence, but most people don't find it as pretty. Operands of a given operator aren't in a RHS together, and the resulting parse trees look a bit strange.

Here's a top-down parse tree for 3 + 4 \* 5:



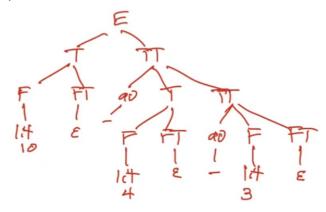
It still seems to suggest that multiplication groups more tightly than addition, but in a lopsided sort of way.

The simplicity of the parsing algorithm makes up for this weakness, in my opinion. As we'll see later, top-down parsing also makes it easier to handle special cases and to produce good error messages when the input program has syntax errors.

gcc switched from bottom-up to top-down parsing around 2005 LLVM's clang front end also uses top-down parsing

Also note that the top-down grammar doesn't capture associativity: in order to parse top-down left-to-right, we end up with a tree that tends to associate to the right.

Here's a top-down parse tree for 10 - 4 - 3:



There's no getting around this in the parser.

Have to take care (by hand) to make sure that the *syntax tree* reflects associativity correctly.

Next lecture: algorithms for top-down v bottom-up parsing.

\_\_\_\_\_\_

## TOP-DOWN AND BOTTOM-UP PARSING

- \*\*\* A LL family parser builds a leftmost derivation from the top down.
- \*\*\* A LR family parser builds a rightmost derivation from the bottom up.

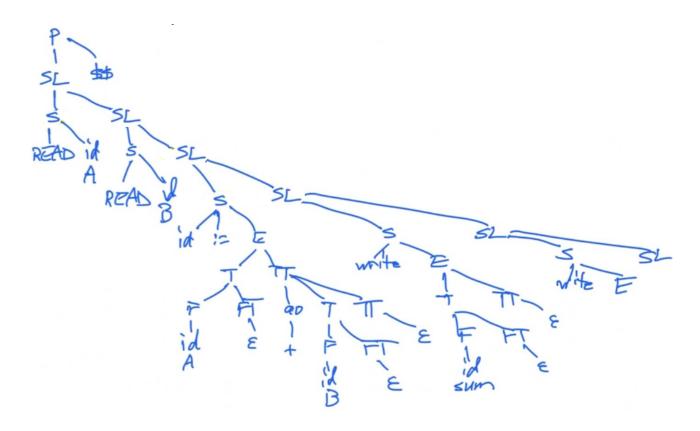
How do we parse a string with the top-down grammar? You can get the general idea by building the parse tree incrementally by hand:

Start at the top and \*predict\* needed productions on the basis of the current left-most non-terminal in the tree and the current input token.

Consider our example program again, together w/ the top-down grammar:

$$P \longrightarrow SL \$\$$$
 $SL \longrightarrow S SL \mid \epsilon$ 
 $S \longrightarrow id := E \mid read id \mid write E$ 
 $E \longrightarrow T TT$ 
 $TT \longrightarrow ao T TT \mid \epsilon$ 
 $read A$ 
 $T \longrightarrow F FT$ 
 $read B$ 
 $SUM := A + B$ 
 $SUM$ 

Let's build a parse tree:



Notice that at every step along the way, it was clear (unambiguous) what to do.

We can also get a sense of the bottom-up case with an example, but it won't be as obvious what's going on.

Just as a scanner is based on a finite automaton, a parser is based on a *pushdown* automaton

- basically a finte automaton with a stack
- makes a decision based on input, state, and top-of-stack symbol
- chooses a new state and may push or pop the stack

A top-down parser has a trivial state machine.

 makes all decisions based on input and top-of-stack symbol until it sees end-of-file, at which point it switches to a final state if the stack looks right (more on this later)

A bottom-up parser has a complex state machine.

- uses current state to make decisions

- I won't be showing you the state machine in this example

Consider our example program again, together w/ the bottom-up grammar:

$$P \longrightarrow SL \$\$$$

$$SL \longrightarrow SL S \mid \epsilon$$

$$S \longrightarrow \text{id} := E \mid \text{read id} \mid \text{write E}$$

$$\text{read A} \qquad E \longrightarrow T \mid E \text{ ao } T$$

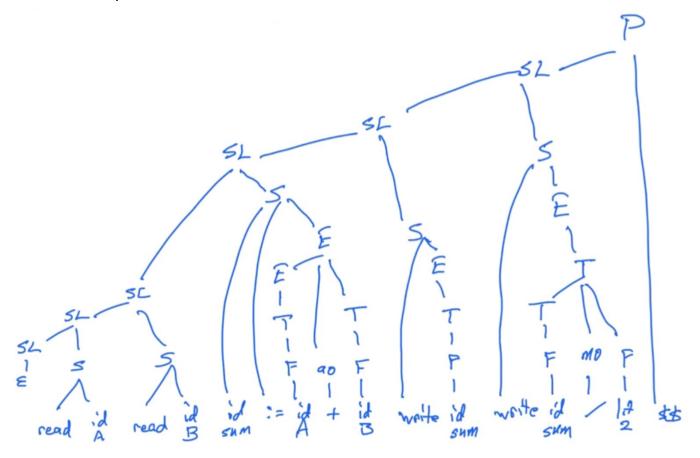
$$\text{read B} \qquad T \longrightarrow F \mid T \text{ mo } F$$

$$\text{sum} := A + B \qquad F \longrightarrow (E) \mid \text{id} \mid \text{lit}$$

$$\text{write sum} \qquad ao \longrightarrow + \mid -$$

$$\text{write sum} / 2 \qquad mo \longrightarrow * \mid /$$

Let's build a parse tree:



The power of bottom-up parsing comes from its ability to recognize things "after the fact," rather than predicting them up front.

This same power explains why error messages and special-case hacks are harder to implement in the bottom-up-case: the parser isn't always sure what's going on until after it's finished.

\_\_\_\_\_

## LL PARSING and RECURSIVE DESCENT

We can implement top-down parsing in two ways:

- recursive descent parser
  - written by hand or automatically
- parse table and a driver
  - written automatically

We'll consider the table-driven option more in a bit. If you took 173 you probably saw recursive descent; this is a review.

Key idea: set of mutually recursive subroutine, one for each nonterminal. Each such routine is responsible for discovering a subtree of the parse tree, rooted at the symbol for which it is named.

Also need a *match* routine:

takes a token name as argument and reads a matching token from the input stream, or announces an error if it can't.

(How to handle errors comes in the next lecture. For now, let's assume we just quit.)

Consider recursive descent routines for the calculator language:

The parser begins by calling the following subroutine:

Other subroutine include:

```
procedure stmt_list
    case input_token of
    id, read, write : stmt; stmt_list
    $$ : skip // epsilon
    else error
```

```
procedure stmt
      case input_token of
          id : match(id); match(:=); expr
          read : match(read); match(id)
          write : match(write); expr
          else error
  procedure expr
      case input token of
          id, literal, ( : term; term_tail
          else
                           error
  procedure term
      case input token of
          id, literal, ( : factor; fact_tail
          else
  procedure term tail
      case input_token of
                                : add_op; term; term_tail
          ), id, read, write, $$ : skip // epsilon
          else
                                   error
etc.
```

Each routine knows that it's expecting to see

- the *yield* of the symbol for which it is named It needs to

- (1) choose a production with which to generate the symbol's children in the parse tree
  - makes this choice based on the upcoming token from the scanner
- (2) parse those children one by one
  - match any that are terminals
  - call the appropriate RD routine to parse any that are nonterminals

So how exactly do we know (in a complicated grammar) which production to use, given an expected nonterminal (root of to-be-fleshed-out subtree) and upcoming token?

That is, how to label the arms of the switch statements?

-----

#### **PREDICT Sets**

If a RHS can start with a given token (directly or indirectly), the appearance of that token *predicts* its rhs.

If the rhs is epsilon (or something that can derive epsilon), any token that can follow the LHS anywhere in the grammar predicts the epsilon production.

An LL(1) parser generator constructs these "predict sets" for you. We'll consider the algorithm in a future lecture. It depends on the following definitions:

```
FIRST(\alpha) \equiv {c : \alpha \Rightarrow * c \beta}

FOLLOW(A) \equiv {c : S \Rightarrow * \alpha A c \beta}

PREDICT(A \rightarrow \alpha) \equiv FIRST(\alpha) U (if \alpha \Rightarrow * \epsilon then FOLLOW(A) else \emptyset)
```

Here  $\rightarrow$  is the familiar "goes to" symbol used in productions.

- → means "derives" can be replaced by. Note that its LHS doesn't have to be a single symbol.
- ⇒\* means "derives in zero or more steps"
- ⇒+ means "derives in one or more steps"

FIRST sets capture the "RHS can start with 'c'" case. FOLLOW sets capture the "RHS can generate  $\epsilon$ " case.

#### NB: conventional notation uses

lower case letters near the beginning of the alphabet for terminals lower case letters near the end of the alphabet for *strings* of terminals upper case letters near the beginning of the alphabet for non-terminals upper case letters near the end of the alphabet for arbitrary symbols Greek letters for arbitrary *strings* of symbols

\*\*\* In a recursive descent parser, if  $c \in PREDICT(A \rightarrow \alpha)$ , then the RD routine for A will predict  $A \rightarrow \alpha$  when it sees c on the input.

The calculator language is simple enough that one can figure these out

more or less by inspection. "Real" languages are too complex for that to be a reasonable task. We need an algorithm (stay tuned).

-----

#### MAKING A GRAMMAR LL

is in FOLLOW(A)?

Note the implicit assumption that the choice among productions  $A \to \alpha \ \ \text{and} \ A \to \beta \ \ \text{is always uniquely determined}.$  What if there is more than one production w/ a LHS of A and a RHSs that can start w/ the same nonterminal? Or two RHSs than can generate epsilon? Or a RHS that can start with c and a RHS that generate  $\epsilon$ , when c

In this case the grammar is not LL(1) — by definition.

If you're trying to write an LL(1) grammar, you probably want to avoid left recursion and common prefixes

```
left recursion
  example
  id_list → ID | id_list , ID
  convert this to
  id_list → ID id_list_tail
  id_list_tail → , ID id_list_tail | ε

common prefixes
  example
  stmt → ID := expr | ID ( arg_list )
  convert this to
  stmt → ID id_stmt_tail
  id_stmt_tail → := expr | ( arg_list )
```

Both left recursion and common prefixes can be removed mechanically. Note, however, that there are infinitely many non-LL *languages*, and the mechanical transformations work on them just fine, so removing these is necessary but not sufficient to make a grammar LL(1).

Fortunately, the cases that arise in practice, however, can generally be handled with kludges.

A famous example was the if-then-else statements of Algol-60 and Pascal. Does

```
if A < B then if C < D then X := 1 else X := 2
```

mean

The hack for top-down parsers was to force the first interpretation with a bit of special-case code. If the programmer wanted the second interpretation they needed to type

```
if A < B then begin
    if C < D then
        X := 1
end
else
    X := 2</pre>
```

Languages since 1970 have fixed this with 'elsif' and 'endif'/'fi'.

```
if A < B then
    if C < D then
        X := 1
    fi
else
    X := 2
fi</pre>
```

\_\_\_\_\_

#### SYNTAX ERROR RECOVERY

Not ok to announce a single syntax error and stop parsing. Have to recover and continue, to find additional errors.

"Phrase-level" recovery defines a *set* of well-defined places to back out to: e.g. end of current expression, statement, or declaration.

Wirth's formalization for recursive descent

- On a token mismatch, insert what you expect and print an error message
- On a null prediction in the RD routine for nonterminal A (no matching label in switch)

delete tokens until you see something in FIRST(A) or FOLLOW(A)

(also stop if you see \$\$)

if the FIRST case, restart the current routine

- assume what we saw was garbage and can be ignored if the FOLLOW case, return
- assume what we saw was the desired nonterminal, garbled

So the RD routine for statements might be

```
procedure stmt
  if not (input_token ∈ FIRST(stmt)) // NB: stmt cannot derive ε
    report_error()
    repeat
        get_next_token()
    until input_token ∈ (FIRST(stmt) U FOLLOW(stmt) U {$$})
  case input_token of
    id : match(id); match(:=); expr()
    read : match(read); match(id)
    write : match(write); expr()
    // no else clause needed
```

That initial if clause can of course be abstracted out into a routine that is then called at the top of each RD routine:

```
procedure check_for_error(sym)

if not (input_token \in FIRST(sym) or sym \Rightarrow+ \epsilon)
```

```
report_error()
repeat
    get_next_token()
until input_token ∈ (FIRST(sym) U FOLLOW(sym) U {$$})
```

Simpler strategies are possible.

Here's one based on exceptions that avoids need for error handling logic in all RD routines:

- On a token mismatch we still insert what we expect (and print an error message)
- On a null prediction, we throw a syntax\_error exception.
- Exceptions are caught by handlers in some subset of RD routines -- "phrases" in the grammar -- statement, declaration, block, function, etc.

## E.g.: replace

```
procedure stmt
        case input_token of
                : match(id); match(:=); expr()
            id
            read : match(read); match(id)
           write : match(write); expr()
                  error()
            else
with
    procedure stmt
        try
            case input_token of
                    : match(id); match(:=); expr()
                read : match(read): match(id)
               write : match(write); expr()
                else
                       throw syntax_error
        except when syntax_error ⇒
            loop
                if input_token ∈ FIRST(stmt)
                    stmt()
                            -- try again
                    return
                elsif input token ∈ (FOLLOW(stmt) U {$$})
                               -- caller can probably make progress
                else get_next_token()
                    -- get_next_token normally called only in match()
```

NB: accepting a token in FIRST(stmt) and restarting may or may not be a good idea. It's always a good idea in Wirth's algorithm, because we detect errors only at the beginning of the RD routine. But with exceptions we may land in the handler halfway through the construct (in this case, stmt). At that point we may have already accepted a big chunk of the statement. Starting over implicitly means silently ignoring what we've seen of the statement so far. It may be better just to delete to what we hope is the end -- that is, to write the simpler

Fancier strategies are also possible. Fischer, Milton, and Quiring developed a particularly pretty "tunable", locally-least-cost recovery mechanism for table-driven LL(1) (see the book).

\_\_\_\_\_

The immediate error detection problem and context-sensitive follow sets

Several error-recovery mechanisms, including the version of Wirth's described above, will sometimes predict an epsilon production when calling routines are doomed to discover an error.

Arguably, we should detect the error before generating epsilon. That way we have more context with which to craft recovery.

Example from the book, in the calculator language:

```
Y:= (A * X X*X) + (B * X*X) + (C * X)

^ There's a problem here (missing '*' in polynomial).

Can we tell?
```

When we're at the point shown in the parse, what recursive descent

#### routines are active?

(dot shows where we are inside)

program	$P \rightarrow . SL \$\$$
stmt_list	$SL \rightarrow . S SL$
stmt	$S \rightarrow id := . E$
expr	E   o <b>.</b> T   TT
term	T   o <b>.</b> F   FT
factor	F   o  ( . $E  )$
expr	E   o <b>.</b> T   TT
term	T   o  F . FT
factor_tail	$FT \to * \; F \; . \; \; FT$
factor_tail	FT   o  ?

Now ID can follow expr in some programs (e.g. A := B C := D), and an expr can end with a factor\_tail, so ID is in FOLLOW of factor\_tail. And since factor\_tail and term\_tail can generate epsilon, the "obvious" thing is to return from FT twice, return from T (which thinks it's done); call from E to TT; return from TT; and return to F all without detecting an error of any kind. At this point we'll (finally) get a mismatch between ID and ). Unfortunately we won't have much information to work with at that point, and won't be able to make as good a recovery as we would have liked.

Specifically: match will insert a right paren, allowing F to complete and return. T will call FT, which will see X on the input, which is in FOLLOW(FT), so it will predict and epsilon production and return, allowing T to return. E will likewise call TT, which predicts epsilon and returns, allowing E to return, at which point S will complete and return, allowing SL to make a recursive call. Now we have

$$X*X) + (B * X*X) + (C * X)$$

on the input, but we've left the context in which we could continue to parse more pieces of an expression.

SL will predict S  $\rightarrow$  id := E. We'll match id (X), insert :=, call E, T, and then F. F will predict F  $\rightarrow$  id, match X, then return

all the way back to

$$SL \rightarrow S \cdot SL$$

at which point we'll make another recursive call to SL and run into trouble with ) on the input. We'll delete the ), predict  $S \rightarrow id := E$ , and soon run into trouble again when we see \* instead of := on the input. When the dust settles, our final "correction" will be

$$Y := (A * X) X := X B := X * X C := X$$

If we were smarter, when FT saw X way back at the beginning it would know that an ID can't follow a factor\_tail *in this particular context* (where we're inside a parenthesized expression, not at the end of an assignment). Good error recovery algorithms take this into account. Wirth showed how to do it in the (better version of) his error-recovery algorithm for recursive descent. He adds a *context-sensitive follow set* parameter to every R.D. subroutine, and uses these, rather than global FOLLOW, to predict epsilon productions.

So, for example, when F calls E in the example above, it would pass as E's follow set only { ')' }. When E calls T it would pass that same set, plus FIRST(TT) -- i.e., { ')', '+', '-' }. When T calls FT it would pass what it, itself, was given, namely { ')', '+', '-' }. When FT calls itself recursively it would pass this same set yet again. When the nested FT sees 'id' on the input, it would know there was a problem. It would delete the id. The subsequent \* is in FIRST(FT), so all would be well at that point. Recognizing the problem early allows the parser to, effectively, "correct" the input into

$$Y := (A * X*X) + (B * X*X) + (C * X)$$

Not "right", but certainly better.

Generalizing, our top-of-routine error checker now looks like this:

```
procedure check_for_error(sym, LAset)
  if not (input_token ∈ FIRST(sym)
```

```
or (sym ⇒+ ε and input_token ∈ LAset)
report_error()
repeat
    get_next_token()
until input_token ∈ (FIRST(sym) U LAset U {$$})
```

We can do something very similar with exception-based recovery, if we pass context-sensitive FOLLOW sets into appropriate RD routines.

One can also do something similar in table-driven parsers, but for these there's an even easier alternative: go ahead and do the epsilon productions, but remember one did so, and when a problem arises, restore the stack to where it was when the error *should* have been noticed, and recover from there instead. There isn't a good analogue of this approach for the recursive descent case: we can't "undo" having returned from a bunch of R.D. routines the way we can restore the explicit stack of the T.D. parser.

ANTLR, by default, uses global FOLLOW sets and Java/C++/C# exception handlers, but the compiler writer can (by hand) write smarter handlers.

FMQ (a parser generator developed at the Univ. of Wisc., which we used many years ago) buffered epsilon productions and then undid them, putting context back on the stack. FMQ also implements tunable "locally least cost" repair.

\_\_\_\_\_

#### TABLE-DRIVEN LL PARSING

ID stmt\_list \$\$

Table-driven LL parsing is essentially a different way to think about recursive descent. You have a big loop in which you repeatedly look up an action in a two-dimensional table based on current leftmost non-terminal and current input token. The actions are (1) match a terminal, (2) predict a production, or (3) announce a syntax error.

- When you predict a production, you replace its LHS (currently at top of stack) with the symbols of the RHS, so the new TOS is the first symbol of the RHS.
- This means the stack always contains what you expect to see in the future.

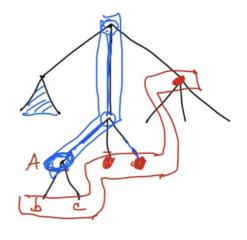
```
grammar:
                                      → stmt_list $$
                        program
                        stmt_list → stmt stmt_list | E
                                      → ID := expr | READ ID | WRITE
                        stmt
expr
                                      → term term_tail
                        expr
program:
                        term_tail
                                      → add_op term term_tail | E
                                      → factor fact_tail
    read A
                        term
    read B
                        fact_tail
                                      → mult_op factor fact_tail | E
    sum := A + B
                        factor
                                      → ( expr ) | ID | LITERAL
    write sum
                        add_op
                                      → + | -
    write sum / 2
                        mult_op
                                      → * | /
stack
                                            remaining input
____
                                            read A read B sum ...
pgm
stmt_list $$
                                            read A read B sum ...
                                            read A read B sum ...
stmt stmt_list $$
READ ID stmt_list $$
                                            A read B sum := A \dots
ID stmt_list $$
                                            read B sum := A + ...
stmt_list $$
                                            read B sum := A + \dots
stmt stmt_list $$
                                            read B sum := A + \dots
READ ID stmt_list $$
                                            B sum := A + B \dots
```

sum := A + B write ...

```
stmt_list $$
                                             sum := A + B write \dots
stmt stmt_list $$
                                             sum := A + B write ...
                                             := A + B write sum ...
ID := expr stmt_list $$
:= expr stmt_list $$
                                             A + B write sum ...
expr stmt_list $$
                                             A + B write sum ...
term term_tail stmt_list $$
                                             A + B write sum ...
factor fact_tail term_tail stmt_list $$
                                             A + B write sum ...
ID fact_tail term_tail stmt_list $$
                                             + B write sum / 2 $$
fact_tail term_tail stmt_list $$
                                             + B write sum / 2 $$
term_tail stmt_list $$
                                             + B write sum / 2 $$
add_op term term_tail stmt_list $$
                                             + B write sum / 2 $$
+ term term_tail stmt_list $$
                                             B write sum / 2 $$
term term_tail stmt_list $$
                                             B write sum / 2 $$
factor fact_tail term_tail stmt_list $$
                                             B write sum / 2 $$
ID fact_tail term_tail stmt_list $$
                                             write sum / 2 $$
                                             write sum / 2 $$
fact_tail term_tail stmt_list $$
term_tail stmt_list $$
                                             write sum / 2 $$
stmt_list $$
                                             write sum / 2 $$
stmt stmt_list $$
                                             write sum / 2 $$
WRITE expr stmt_list $$
                                             sum / 2 $$
        etc
stmt_list $$
                                             $$
$$
```

Remember: the stack contains all the stuff you expect to see between now and the end of the program -- what you *predict* you will see.

These correspond in a recursive descent parser to the concatenation of the remainders of the current case arm in all the RD routines on the current call chain.



-----

#### LL PARSER GENERATORS

The algorithm to build PREDICT sets is tedious (for a "real" sized grammar), but relatively simple.

- (1) compute FIRST sets and EPS values for symbols
- (2) compute FOLLOW sets for non-terminals (this requires computing FIRST sets for some *strings*)
- (3) compute PREDICT sets for productions (this requires computing EPS for some *strings*)

where

```
EPS(\alpha) == if \alpha \Rightarrow^* E then true else false

FIRST(\alpha) == {c : \alpha \Rightarrow^* c \beta}

FOLLOW(A) == {c : S \Rightarrow^+ \alpha A c \beta}

PREDICT(A \rightarrow \alpha) == FIRST(\alpha) U (if EPS(\alpha) then FOLLOW(A) ELSE \emptyset)
```

Steps (1), (2), and (3) begin with "obvious" facts, and use them to deduce more facts, until nothing new is learned in a full pass through the grammar.

What is obvious? At a minimum:

```
If A \rightarrow E, then EPS(A) = true c in FIRST(c)
```

How to deduce?

```
If EPS(\alpha) = true and A \rightarrow \alpha, then EPS(A) = true

If A \rightarrow B \beta, then FIRST(A) \supset FIRST(B)

If A \rightarrow \alpha B \beta, then FOLLOW(B) \supset FIRST(\beta)

If A \rightarrow \alpha B (or A \rightarrow \alpha B \beta and EPS(\beta) = true)

then FOLLOW(B) \supset FOLLOW(A)
```

This last one is tricky. It's *not* true the other way around. That is,  $A \to \alpha$  B does *not* imply that FOLLOW(A)  $\supset$  FOLLOW(B). Consider our calculator grammar.

```
')' is in FOLLOW(E), because F \rightarrow ( E ) $$ is in FOLLOW(S), because P \rightarrow SL $$, SL \rightarrow S SL, and SL \rightarrow \epsilon
```

Now consider the production  $S \to write E$ . The fact that \$\$ is in FOLLOW(S) means than \$\$ is in FOLLOW(E). But the fact that ')' is in FOLLOW(E) does *not* mean that ')' is in FOLLOW(S).

Put another way, ')' is in FOLLOW(E) in the context where E was generated from F, but *not* necessarily in the context where E was generated from S.

# If any token belongs to the PREDICT set of more than one production with the same lhs, then the grammar is not LL(1).

A conflict can arise because

some token c can begin more than one rhs, or c can begin one rhs and can also appear *after* the LHS in some valid program, and one possible RHS is epsilon.

Examples 2.33–2.35 in the book work through the generation of a table-driven parser for the calculator language.

- Fig. 2.22 shows the "obvious" facts in the calculator grammar
- Fig. 2.23 shows the generated FIRST, FOLLOW, and PREDICT sets
- Fig. 2.20 contains the resulting parse table
- Fig. 2.19 contains a parser driver that reads the parse table

Again, the algorithm to generate the parse table

- (1) computes FIRST sets and EPS values for symbols
- (2) computes FOLLOW sets for non-terminals (this requires computing FIRST sets for some *strings*)
- (3) computes PREDICT sets for productions (this requires computing EPS for some *strings*)

Here are the details:

-- EPS values and FIRST sets for all symbols:

```
for all terminals c
         EPS(c) := false: FIRST(c) := \{c\}
    for all non-terminals X
         EPS(X) := if X \rightarrow \varepsilon then true else false
         FIRST(X) := \emptyset
    repeat
         <outer> for all productions X \rightarrow Y1 Y2 ... Yk
              <inner> for i in 1..k
                  add FIRST(Yi) to FIRST(X)
                  if not EPS(Yi) (yet) then continue outer loop
              EPS(X) := true
    until no further progress
-- Subroutines for strings, similar to the inner loop above:
    function string_EPS(X1 X2 ... Xn):
         for i in 1...n
              if not EPS(Xi) then return false
         return true
    function string_FIRST(X1 X2 ... Xn):
         return value := Ø
         for i in 1..n
              add FIRST(Xi) to return value
              if not EPS(Xi) then return
-- FOLLOW sets for all symbols:
    for all symbols X, FOLLOW(X) := \emptyset
    repeat
         for all productions A \rightarrow \alpha B \beta
              add FIRST(\beta) to FOLLOW(B)
         for all productions A \rightarrow \alpha B
                  or A \rightarrow \alpha B \beta, where string EPS(\beta) = true
              add FOLLOW(A) to FOLLOW(B)
    until no further progress
-- PREDICT sets for all productions:
    for all productions A \rightarrow \alpha
         PREDICT(A \rightarrow \alpha) := string FIRST(\alpha)
              U (if string EPS(\alpha) then FOLLOW(A) else \emptyset)
```

At the end, the grammar is LL(1) iff all the PREDICT sets for productions with the same LHS are disjoint

-----

## SYNTAX ERROR RECOVERY (reprise)

Natural adaptation of phrase-level recovery to table-driven top-down parsing:

- When we encounter an error in match (TOS is a token that doesn't match the input), we print a message and pop the stack (pretend to have seen the desired token).
- When we encounter an error entry in the table (non-terminal A at TOS), we delete tokens until we find something in FIRST(A) or FOLLOW(A). If in FIRST(A), we continue the main loop of the driver. If in FOLLOW(A), we pop the stack first.

(\$\$ is a special case: if we see that, we pop the stack and continue the main loop.)

More generally, we may define a set of "starter symbols" that are too dangerous to delete (begin, left paren, procedure, ...), because they are likely to presage subsequent structure. Treat them like \$\$. Hopefully they'll be in FIRST of something deeper in the stack. If not, we'll eventually end up with \$\$ on the stack and remaining input, at which point we print a message and die.

As in the recursive descent case, we probably want to consider the immediate error detection problem.

Adding context-sensitive follow sets to the stack is a nuisance, however.

Much easier, when we predict an epsilon production, to remember that we did so, and buffer what we popped off the stack.

- If we accept a new token of real input, we can toss the buffer.
- If we run into an error before then, we put the buffered symbols back on the stack and initiate error recovery as shown above.