A smorgasbord of types

scalar types -- one or two-dimensional  
  discrete -- one-dimensional and countable  
    integer, boolean, char, enumeration, subrange  
  rational  
  real  
  complex

composite types  
  records/structs/tuples  
  variants/unions  
  arrays  
    strings  
  sets  
  pointers  
  lists  
  files  

  mappings       // common in scripting languages

-------------------------------
Records
  usually laid out contiguously  
  possible holes for alignment reasons  
    permits copying but not comparison with simple block operations

example:

    struct element {  
      char name[2];  
      int atomic_number;  
      double atomic_weight;  
      bool metallic;  
    }
layout on a 32-bit machine:

<table>
<thead>
<tr>
<th>4 bytes/32 bits</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td></td>
</tr>
<tr>
<td>atomic_number</td>
<td></td>
</tr>
<tr>
<td>atomic_weight</td>
<td></td>
</tr>
<tr>
<td>metallic</td>
<td></td>
</tr>
</tbody>
</table>

A few languages allow the programmer to specify that a record is **packed**, meaning there are no (internal) holds, but fields may be unaligned. Less space, but significant run-time access penalty.

<table>
<thead>
<tr>
<th>4 bytes/32 bits</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>atomic_</td>
</tr>
<tr>
<td>number</td>
<td></td>
</tr>
<tr>
<td>atomic_weight</td>
<td></td>
</tr>
<tr>
<td>metallic</td>
<td></td>
</tr>
</tbody>
</table>

Smart compilers may re-arrange fields to minimize holes largest first or smallest first. Latter maximizes # of fields with a small offset from the beginning.

<table>
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</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>metallic</td>
</tr>
<tr>
<td>atomic_number</td>
<td></td>
</tr>
<tr>
<td>atomic_weight</td>
<td></td>
</tr>
</tbody>
</table>

C compilers promise not to rearrange.
**Unions** (variant records)

overlay space

w/ tag: *discriminated* union (as in OCaml or Rust)
w/out tag: nondiscriminated union (as in C)

cause problems for type checking -- you don’t know what is there
ability to change tag and then access fields hardly any better (as in Pascal)
- modern languages typically require assignment of entire variant (w/ tag),
as in OCaml, Rust, or Ada

Several languages (including Algol68, Ada, and ML) require access to variant
portions of a record to be confined to a “conformity clause” (e.g., OCaml’s match)
that ensures type safety.

If structs and unions are independent, declarations can be quite ugly, as in this legacy C:

```c
struct employee {
...
  union {
    struct { // hourly employee
      double hourly_pay;
      ...
    } S1;
    struct { // salaried employee
      double annual_salary;
      ...
    } S2;
  } U1;
};
...
this_employee.U1.S1.hourly_pay       // yuk!
```

Pascal unified records and variants:

```pascal
type employee = record
...
  case boolean of   (* hourly? *)
    true:
      hourly_pay : real;
    ...
    false:
      annual_salary: real;
    ...
```
end;
...
this_employee.hourly_pay  // better

Recent versions of C and C++ achieve a similar effect with *anonymous* structs and unions. Strike out the S1, S2, U1 names above.

Note that the problem of uninitialized variables is more general than variant records. Some languages say variables start out with certain values (e.g. 0 for globals [but not locals!] in C). Many just say it’s erroneous to use an uninitialized variable. A few actually try to prevent you from accessing one. In general, the only ways to do this are (1) restrict the language, e.g., as Java and C# do to ensure *definite assignment*; (2) initialize variables automatically with a special “uninitialized” value and check most references at run time.

========================================

**Arrays**

Two layout strategies for arrays:

- **contiguous elements**
  - *column major* -- basically used only in Fortran  
    probably an historical accident
  - *row major* -- used by everybody else; makes array [a..b, c..d]  
    the same as array [a..b] of array [c..d].

---

Row-major order

Column-major order
**row pointers**

an option in C; only option in Java and some scripting languages
allows rows to be put anywhere -- nice for big arrays on
legacy machines with segmentation problems
avoids multiplication -- nice for legacy machines with slow multiply
nice for matrices whose rows are of different lengths
e.g. an array of strings
requires extra space for the pointers

---

**Descriptors (dope vectors)** required when bounds not known at compile time.

When bounds *are* known, much of the arithmetic can be done at compile time.

Given

\[
A : \text{array } [L1..U1] \text{ of array } [L2..U2] \text{ of array } [L3..U3] \text{ of glarch};
\]

Let

\[
D1 = U1-L1+1 \\
D2 = U2-L2+1 \\
D3 = U3-L3+1
\]

Let

\[
S3 = \text{sizeof \ glarch} \\
S2 = D3 \times S3 \\
S1 = D2 \times S2
\]

The address of \(A[i][j][k]\) is

\[
(i - L1) \times S1 \\
+ (j - L2) \times S2 \\
+ (k - L3) \times S3 + \text{address of } A
\]

We could compute all that at run time, but we can make do with fewer subtractions:
$$== (i \times S1) + (j \times S2) + (k \times S3)$$
+ address of A
− [(L1 \times S1) + (L2 \times S2) + (L3 \times S3)]$$

The stuff in square brackets is a compile-time constant that depends only on the type of A. We can combine easily with records:

Another example: Suppose A is a messy local variable.
The address of A[i].B[3][j] is
i \times S1
− L1 \times S1
+ B’s field offset
+ (3−L2) \times S2
+ j \times S3
− L3 \times S3
+ fp
+ A’s offset in frame

Some languages assume that all array indexing starts at zero. A few assume it starts at one. This is not a performance issue: the lower bound can be factored out at compile time.

**Lifetime** (how long object exists)
and **shape** (bounds and possibly dimensions)

common options:
- global lifetime, static shape
  globals in C
- local lifetime, static shape
  subroutine locals in many classic imperative languages, including historical C
- local lifetime, shape bound at elaboration
  subroutine locals in Ada or modern C
- arbitrary lifetime, shape bound at elaboration
  Java arrays
- arbitrary lifetime, dynamic shape
  most scripting languages, APL, Icon
The first two categories are just familiar global and local variables. With dynamic shape you need dope vectors. The fourth and fifth categories have to be allocated off a heap. The third category can still be put in a subroutine’s stack frame; Dope vector and a pointer go at a fixed offset from the FP; the data itself is higher up in the frame. This divides the frame into fixed-size and variable-sized parts; also requires a frame pointer.

-- Ada:
procedure foo(size : integer) is
  M : array (1..size, 1..size) of long_float;
  ... begin
  ... end foo;

// C99:
void foo(int size) {
  double M[size][size];
  ...
}

Note that deallocating a fully dynamic array on subroutine exit requires some extra code -- doesn’t happen automatically via pop of stack frame. Cf: C++ destructors, Rust drop
Slices (Fortran 90, APL, MATLAB, others)

\[
\begin{align*}
\text{matrix}(3:6, 4:7) & \quad \text{columns 3-6, rows 4-7} \\
\text{matrix}(6:;, 5) & \quad \text{columns 6-end, row 5} \\
\text{matrix}(;, 2:8:2) & \quad \text{columns 1-4, every other row from 2-8} \\
\text{matrix}(;, /2, 5, 9/) & \quad \text{all columns, rows 2, 5, and 9}
\end{align*}
\]

can assign into each other as if they were smaller arrays.

Vectors

Supported by container libraries in many languages.
Built into a few — esp. scripting languages.

Basically just arrays that automatically resize when you run off the end.

May also support operations like push_back (which extends the underlying array) or delete (which removes an element and moves all remaining elements down to fill the gap).

Strings

Basically arrays of characters.
But often special-cased, to give them flexibility (e.g., dynamic sizing)
and operators not available for arrays in general.

It’s easier to provide these things for strings than for arrays in general because strings are one-dimensional and non-circular (meaning you can garbage-collect them with reference counts; more later). Some languages make them all constant: you can create new strings, but not modify old ones.

Sets & mappings

You learned about a lot of possible implementations in 172.
Bit vectors are what usually get built into compiled programming languages. Things like intersection, union, membership, etc. can be implemented efficiently with bitwise logical instructions.
Scripting languages typically use hash tables. May use trees or skip lists for fast enumeration and range queries.

Pointers and recursive types

Pointers serve two purposes:
- efficient (and sometimes intuitive) access to elaborated objects (as in C)
- dynamic creation of linked data structures, in conjunction with a heap storage manager

Note that pointers are not the same thing as addresses. Pointers are an abstraction. Addresses are an implementation. Pointers are not always implemented as addresses:
- machines with segments
- error checks (e.g. locks and keys -- see below)
- swizzling
- cursors
- C++ overloading of *, -> (e.g., for smart pointers)

Many languages restrict pointers to accessing things in the heap: the only way to get a pointer is by calling new. Others (e.g., C) allow you to create a pointer to any existing object.

Pointers are used with a value model of variables. They aren’t needed with a reference model.

Good implementations of languages with a reference model of variables represent primitive (immutable) types the same way you would for a language with a value model of variables -- you think of your variable x as a reference to “the” 3 (the Platonic ideal), but the compiler implements it as a box with a copy of “the” 3 in it.

\[
\text{mental model:} \quad y := x \\
\text{implementation:} \quad x \rightarrow 3
\]

Problems:
- syntax of pointer dereferencing
typically explicit, as in C
a few languages dereference automatically, depending on context
  Ada, for example, does implicit dereferencing for record field references,
  and has special syntax to name the entire referenced object

```plaintext
type foo is record ...
type fp is access foo
f : xp := new foo;
...
y := f.field1;  -- implicit dereference
g : foo := f.all;  -- whole object
```
dangling pointers due to
  explicit deallocation of heap objects
    only in languages that have explicit deallocation
  implicit deallocation of elaborated objects
    only in languages that let you create pointers to these
  two implementation mechanisms to catch:

```plaintext
new(my_ptr);
```

**locks and keys**

```plaintext
ptr2 := my_ptr;
```
not an option for pointers
to elaborated objects

```plaintext
delete(my_ptr);
```

(Potentially reused)
tombstones

new(my_ptr);

ptr2 := my_ptr;

delete(my_ptr);

tombstones themselves live a long time, but can be garbage collected using reference counts; more later

Garbage collection

Many languages leave it up to the programmer to design without garbage creation. This is very hard.

C++ increasingly regularizing automatic collection via smart pointers. Rust supports manual reclamation via ownership and borrowing, but this significantly complicates the creation of linked structures.

Increasingly, languages arrange for automatic garbage collection objects are reclaimed when the runtime can prove they are no longer accessible. (Note: this is not the same as no longer needed -- may be overly conservative.)

Two common implementations: reference counting and tracing
reference counting

works great for strings; does not work for circular structures

Stack | Heap

stooges := nil;

Does work for tombstones, though you have to make sure that when you delete a struct containing pointers (or allow it to go out of scope) the compiler decrements the reference counts of the tombstones for those pointers. Key observation is that tombstones are used with explicit object deletion: ref. counts fail to reclaim tombstone only when user fails to reclaim object.

tracing

generally requires strong typing

(but see conservative collection below)

used routinely in Java, C#, Scala, Swift, Kotlin, Go, Lisp, ML/OCaml/Haskell, scripting languages, ...

variants
**mark-and-sweep**
- Takes time proportional to total heap size
  (would prefer proportional to amount of garbage collected, but we don’t know how to do that)
- Can use *pointer reversal* for space-efficient tracing

**stop-and-copy**
- Takes time proportional to amount of space currently in use
- Performs compaction, to cure external fragmentation
- Might be expected to double space requirements, but doesn’t really, given virtual memory

**generational** (used in most production systems)
- Avoids, heuristically, wasting time on memory that is unlikely to be unused
- Has to be able to fall back to previous techniques
- Requires “write barriers” in program code to track old-to-new pointers
  (we also need write barriers -- for different reasons -- with reference counts)

Conservative approximation possible in almost any language:

Assume any pointer-sized aligned value is a pointer if its bit pattern is the address of (the beginning of) a block in the heap.

Limitations:
- Pointers to *interior* of objects not generally supported
- Pointers must not be hidden (stored in any way other than a full-word aligned address)
- Can leak storage when the address of an unneeded block happens to match the bit pattern of some non-pointer object.

Hybrids also possible: e.g., reference count most of the time, do a mark-and-sweep once in a while to catch circular structures.
The basic idea: an array variable is (in most respects) treated like a pointer to the array’s first element; subscripting is defined in terms of pointer arithmetic:

\[ E1[E2] == \star((E1)+(E2)) = \star((E2)+(E1))! \]

So given
\[
\begin{align*}
\text{int } & n, *p; \\
& \text{You can say not only} \\
& n = p[3]; \\
& \text{but also} \\
& n = 3[p]; & // \text{surprise!}
\end{align*}
\]

Subscripting scales to the size of array elements in C precisely because pointer arithmetic does.

When is an array not a pointer?

(a) in a variable definition, where the array allocates space

(b) in a sizeof, where the array represents the whole thing

\[
\begin{align*}
\text{double } & A[10]; \\
\text{double } & \star p = A; \\
& \text{sizeof}(A) == 80 & // \text{the whole array} \\
& \text{sizeof}(A[0]) == 8 & // \text{one element} \\
& \text{sizeof}(\star p) == 4 & // \text{a pointer (on a 32-bit machine)}
\end{align*}
\]

Variable definitions:
\[
\begin{align*}
& \text{int } *a[n] & // \text{n-element array of row pointers} \\
& \text{int } a[n][m] & // 2-D array
\end{align*}
\]

Beware the difference between definitions, which allocate space, and declarations, which merely introduce names.

Since function prototypes (headers) are just declarations, and don’t allocate space, and since arrays are passed as pointers, the following parameter declarations are equivalent:
int *a == int a[] // pointer to int
int **a == int *a[] // pointer to pointer to int

Note that these equivalences do not hold for definitions.

Compiler has to be able to tell the size of the things to which you point. So the following aren’t valid, even as parameter declarations:

    int a[][] // bad
    int (*a)[] // bad

But a[][10] is ok, even as a parameter, and the compiler will do the right thing. (*a)[10] is equivalent as a parameter.

You can pass contiguous arrays to subroutines, but you have to specify the size of all inner dimensions:

    int a[][10] // ok (as declaration, not definition)
    int (*a)[10] // " ; does the same thing
    int a[10][10] // also ok, but first 10 is unnecessary

**C declaration rule:** read right as far as you can (subject to parentheses), then left, then out a level and repeat.

    int *a[n] // n-element array of pointers to integers
    int (*a)[n] // pointer to n-element array of integers

    int (*f)(int *) // pointer to function taking pointer to
                    // integer as argument, and returning integer

Choice between pointer arithmetic & subscripts is largely a matter of taste. Pointer arithmetic used to be faster with stupid compilers. With modern compilers it’s often the other way around, particularly given the tendency of aliases to inhibit optimization.

Cf. choice between row-pointer and contiguous layout: tradeoff has reversed with time.