Outline

Cache Performance Recap

Data Layout

Reuse Distance

Besides the Cache
Cache Performance Recap

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Reuse Distance

Besides the Cache
Memory vs CPU

tiny bandwidth == HUGE BOTTLENECK

CPU Speed
DRAM Speed

Performance

1000
100
10
1
0.1


Year

from STREAM
Misses (Recap)

- Compulsory/Cold
- Capacity
- Conflict
- Our Goal: Reduce Misses
Outline

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Reuse Distance

Besides the Cache
Caches are optimized for:
  - Spatial locality
  - Temporal locality
Caches store lines, 64 to 128 bytes from contiguous locations
  - Memory is partitioned into lines
Important considerations:
  - Footprint (total size of data)
  - Working set (total size of data accessed in a given period of time)
Data Layout for Arrays

- **Row Major**
  - C
  - Array elements in same row are next to each other
  - Memory: \[
  \begin{bmatrix}
  0 & 1 & 2 & 3 & 4 \\
  5 & 6 & 7 & 8 & 9
  \end{bmatrix}
  \]

- **Column Major**
  - FORTRAN
  - Array elements in same column are next to each other
  - Memory: \[
  \begin{bmatrix}
  0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9
  \end{bmatrix}
  \]
What is the size in bytes of each of the structures below?

```
struct pt {
    char ptvalid;
    int x;
    char xvalid;
    int y;
    char yvalid;
} lines[100];

struct pt2 {
    char ptvalid;
    char xvalid;
    char yvalid;
    int x;
    int y;
} lines[100];
```
Packing in Structures

```c
struct pt {
    char ptvalid;
    int x;
    char xvalid;
    int y;
    char yvalid;
} lines[100];

• Uses 20 bytes per element, padding/packing (3 bytes) inserted after ptvalid, xvalid, yvalid

struct pt2 {
    char ptvalid;
    char xvalid;
    char yvalid;
    int x;
    int y;
} lines[100];

• Uses 12 bytes per element, padding/packing (1 byte) inserted
Dynamic data structures and “Pointer-chasing” code

```c
struct node {
    struct node *next;
    int data;
};

n = list->head;
while(n) {
    ...
    n = n->next;
};
```
• Most dynamic data structures (i.e. allocated dynamically)
• Members keeps links (pointers) to other members of the structure
  • Linked lists
  • Trees
• Code to traverse these data structures can hinder some processor optimizations
  • Sometimes called “irregular” code
  • Memory equivalent of indirect/conditional branches
Summary of Data Layout

- Understand how data is laid out in memory
  - Contiguous memory accesses are the fastest (due to spatial locality)
  - Aligned memory accesses are the fastest
- Check for excessive packing
  - May cause poor utilization
- Dynamically allocated structures can perform poorly
  - Use sparingly in high-performance code
  - Consider using custom memory allocators that are backed by contiguous memory
Outline

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Data Layout

Reuse Distance

Besides the Cache
Reuse distance for a cache line (or address) is the number of intervening *unique* references to other lines between any two consecutive references to the same line.

\[ \text{A B C C D B F A} \]

- Reuse distance for second B is 2
- Reuse distance for last A is 4
- Reuse distance for second C is 0
- Reuse distance for others is $\infty$
Interpreting Reuse Distance

- A miss with reuse distance $\infty$ implies cold miss
- A miss with reuse distance $< \text{cache size (in lines)}$ implies conflict miss
- A miss with reuse distance $> \text{cache size (in lines)}$ implies capacity miss
- Note: these assume LRU is the replacement algorithm
- P.S.: these are not exact rules
- P.P.S: the only takeaway is that changing (specifically, reducing) reuse distance can result in better cache behaviour.
Goal: Reduce misses by decreasing reuse distance

How can you reduce reuse distance?
• \( y = \alpha x + y \)

.. code-block::

    for(int j = 0; j < N; j++) {
        y[i] = y[i] + alpha * x[j];
    }
• \( y = \alpha x + y \)

```java
    temp = y[i];
    for(int j = 0; j < N; j++) {
        temp = temp + alpha * x[j];
    }
    y[i] = temp;
```

• Automatically by any compiler that can determine that \( y \) and \( x \) do not alias
min = minimum(y, 0, N);
max = maximum(y, 0, N);

- where minimum and maximum may be implemented as:

```c
int minimum(int *a, int start, int end) {
    int tmp = a[start];
    for(int i = start + 1; i < end; i++) {
        if(a[i] < tmp) tmp = a[i];
    }
    return tmp;
}
```
min = y[0];
max = y[0];

for(int j = 0; j < N; j+=WIDTH) {
    end = j + WIDTH;
    if(end > N) end = N;

    tmp_min = minimum(y, j, end);
    tmp_max = maximum(y, j, end);

    if(tmp_min < min) min = tmp_min;
    if(tmp_max > max) max = tmp_max;
}
for(int i = 0; i < m; i++)
    for(int j = 0; i < n; j++)
        A_out[j * m + i] = A_in[i * n + j];
After one full inner iteration ($i$)

- $A_{in}$ has good cache reuse
- $A_{out}$ has poor cache reuse (reuse distance = $n$)
for(int i = 0; i < m; i+=WIDTH)
    for(int j = 0; i < n; j+=HEIGHT)
        for(int ii=0; ii < WIDTH && (i+ii) < m; ii++)
            for(int jj=0; jj < HEIGHT && (j+jj) < n; jj++)
                A_out[(j+jj) * m + (i+ii)] = A_in[(i+ii) * n + (j+jj)]
After one full tile iteration \((ii\text{ and } jj)\)

- \(A_{in}\) has good cache reuse
- \(A_{out}\) has good cache reuse (reuse distance = \(WIDTH\))
Determining blocking parameters

- Which cache must the block fit?
  - L1?
  - L2?
  - LLC?

- How to determine best performing values of WIDTH and HEIGHT?
  - "Auto-tuning"
  - Search through space of all possible values
Other loop transformations to improve cache behaviour

- Loop interchange
  - $IJK$ vs $IKJ$ (previous lecture)
  - Analyze that loop for reuse distance
- Loop fusion
  - merge two loops together if reuse can be improved
  - check dependencies are not violated!
- Many more
  - need to verify legality when applying
  - check dependencies are not violated
Outline

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Data Layout

Reuse Distance

Besides the Cache
Other components in the memory subsystem

The following play an important role in the memory subsystem:

- Prefetcher
- Virtual Memory Manager/Pager
To avoid compulsory misses, we can prefetch data.

- **Software techniques (programmer)**
  - issue loads in advance of reading
  - use software prefetch instructions
  - useful when no hardware prefetcher present

- **Hardware techniques (automatic)**
  - automatically detect a “stream” and fetch from it
  - limited in what it can do

- **Fundamental performance concerns**
  - Timeliness (is prefetch just-in-time?)
  - Usefulness (was data from prefetch read?)
  - Cache Pollution (prefetches displaces useful lines from cache space)
  - Bandwidth (prefetches compete with “actual” loads)
The Hardware Prefetcher

- “Next line prefetcher” (L1)
  - Fetch next cache line on multiple accesses to a line
- “Stream/Stride prefetcher” (L2/LLC)
  - Triggered by multiple misses
  - Detects stride
  - Fetches cache lines that match the stride
  - Does not fetch past 4096 bytes (x86)
Why did the memory request read from disk?
Virtual Memory

- Every process has its own address space
  - for protection, isolation, etc.
  - Two different processes may store data at the same virtual address
- Data may exist:
  - Physical RAM
  - Disk (Swapped out)
- Virtual to Physical address mappings are handled by the OS
  - stored in page tables
  - which may also be swapped out!
- Every [why?] memory reference by a program must be:
  - translated into its physical equivalent
  - involves reading the page table
Translation Look-aside Buffer (TLB)

- Small cache (what else?)
- Caches page table entries (about 64 or so)
- Fully-associative
- Consulted on every memory request
- Miss in TLB implies walking the page table
  - OSes are lazy, may only create a page on a miss!
- One solution to lower TLB misses: “Huge Pages”
  - 4MB vs 4KB
  - Requires OS and programmer support
Software Managed Caches

- On-chip memory managed by programmer
- Separate address space
- Prevalent on DSPs, GPUs
- Will deal with these when studying GPUs
Conclusion

- Memory accesses will remain primary bottleneck for most applications
  - Big data ...

- Compilers can help with regular, array-based code
  - Especially if you use FORTRAN to write it
  - Situation getting better for C
  - What about other programming languages?

- Irregular, dynamic data-structure based code must be optimized by programmer
  - Few general and automatic solutions
  - Ideas similar to strip-mining/blocking may still be applicable