CSC2/455 Software Analysis and Improvement Dominators and SSA Form - II

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URCS

Dominance Frontiers and Dominator Trees

Emitting code for SSA form

Dominance Frontiers and Dominator Trees

Emitting code for SSA form

- A node *n* in the CFG dominates a node *m* iff:
 - *n* is on all paths from entry to *m*
 - by definition, a node *n* always dominates itself
 - if $n \neq m$, then *n* strictly dominates *m*
- Computed using a dataflow-style analysis
 - Each node annotated with a set of its dominators

- Simple algorithm to generate SSA form
 - Introduce ϕ functions
 - Rename variables using Reaching Definitions
- Algorithm can generate excessive ϕ functions
 - TODAY: Use *dominance frontiers* to place the minimal number of ϕ functions
- Also today: Removing ϕ functions
 - Machines don't support ϕ functions, so we must emulate them

- $\bullet\,$ Insert ϕ nodes for each definition at every join node
- Rename LHS
- Rename RHS using reaching definitions

- Why insert ϕ nodes at only join nodes?
- Can we skip inserting ϕ nodes for a definition at some join node?

Dominance Frontiers and Dominator Trees

Emitting code for SSA form

- The dominance frontier of a node n (DF(n)) is a set of nodes
- A node $m \in DF(n)$ iff:
 - *n* does not strictly dominate *m*
 - *n* dominates *q* where $q \in \text{pred}(m)$
- Note that dominance frontiers only contain join nodes
 - I.e. nodes with multiple predecessors
- Computing the dominance frontier of each node:
 - Iterative Data-flow analysis?

Direct calculation of dominance frontiers using *dominator trees*.

Immediate Dominators

- The *immediate* dominator of a node *m* (IDOM(*m*)) is the node *n*:
 - such that *n* strictly dominates *m*, and
 - n does not strictly dominate o where o ∈ (DOM(m) - {m})
 - in some sense, *n* is the "closest" dominator in the CFG to *m*.
- By definition, ENTRY has no immediate dominator



- *n* strictly dominates *m*
 - $SDOM(n,m) = n \in DOM(m) \land n \neq m$
- *n* does not strictly dominate *m*

•
$$\neg SDOM(n, m) = n \notin DOM(m) \lor n = m$$

Dominator Tree

- Note that each node in the CFG can have only one immediate dominator
 - Can you see why?
- Create a graph G = (V, E), where:
 - V is the set of basic blocks
 - There is an edge (n, m) in *E* if n is the immediate dominator of m (i.e. IDOM(m) = n)



Example: CFG and its dominator tree



- Find all join nodes in CFG, e.g. j
- For all nodes *n* that dominate predecessors of *j* (in the CFG)
 - If *n* does not strictly dominate *j*, add *j* to DF(*n*)
- This last step can be operationalized over all predecessors *p* of *j* in the CFG:
 - Start traversing the dominator tree *p*
 - If p is IDOM(j), stop. Otherwise add j to DF(p)
 - Repeat by moving up the dominator tree until you reach IDOM(*j*)

Example: Non-redundant ϕ functions



- For each definition *d* in basic block *n*:
 - Place a ϕ function for d in all nodes m where $m \in DF(n)$
 - Note that each ϕ function is also a definition!
 - Repeat, until no more $\boldsymbol{\phi}$ functions need to be inserted
- This is the minimal number of ϕ functions for a definition d structurally
 - Can we further reduce the overall number of ϕ functions?
- (Figure 9.9 in Cooper and Turczon)

- Dead definitions
 - Definitions that are not read (i.e. overwritten) do not need ϕ functions
- Two forms:
 - *Semi-pruned* SSA form, using "globals" names (those variables that are live in to a block)
 - Pruned SSA form, using LIVEOUT information

Dominance Frontiers and Dominator Trees

Emitting code for SSA form

- SSA form introduced "subscripts" for each variable
- Should we drop them when generating code?

```
a_0 = x_0 + y_0
b_0 = a_0
a_1 = 17
c_0 = a_0
```

Problem with dropping subscripts

a = x + y b = a a = 17c = a # WRONG!

- Each definition becomes a new variable
 - I.e. Do NOT drop subscripts
- Preserves data dependences
 - Esp. important when we aggressively move code from basic blocks (e.g. very busy expressions, loop invariant code motion, etc.)

• Introduce copies along each incoming edge to a join node



Inserting appropriate copies along incoming edges



- Executing ϕ functions by inserting copies into predecessor blocks is not always correct
- If such a predecessor block has multiple successors, then the ϕ function may execute when it shouldn't
 - This *may* be harmless, but not always
- Edges connecting such predecessors to the block containing the ϕ function are called *critical* edges

Critical Edges: Example



Splitting critical edges



- Such edges need to be *split* by inserting a block on that edge
- See the discussion in Cooper and Turczon for more details and an example

Dominance Frontiers and Dominator Trees

Emitting code for SSA form

• Chapter 9 of Cooper and Turczon

- Section 9.2.1
- Section 9.3