Compiler Correctness

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Compiler pipeline

- Front-end:
  - C
  - C++
  - Go
  - Rust
  - Toy
  - Clang
  - Gollvm
  - rustc

- Middle-end:
  - LLVM IR
  - LLVM optimizer

- Back-end:
  - LLVM IR
  - LLVM static compiler
  - x86
  - ARM
  - RISC-V
  - MIPS
  - PowerPC
  - ...
The compilation process [Leroy(2019)]

In general: any translation from a computer language to another one.

More specifically:

- automatic translation
- from a high-level language suitable for programming by humans
- to a low-level language executable by machines
- with a concern for efficiency ("optimizing" compilers)
- often used as a black-box and assume correctness
Compiler bugs [Sun et al.(2016)]

(a) GCC.

(b) LLVM
Source

```c
a = x * y
if (j == 1) {
    x = 1
    b = x * y
}
else {
    b = x * y
}
return b
```

Target

```c
a = x * y
if (j == 1) {
    x = 1
    b = a
}
else {
    b = a
}
return b
```
Bugs in the compiler can make it produce wrong executable code for a correct source program.

For low-assurance software:
- miscompilation is negligible compared with bugs in the program itself
- when happen, it is very hard to track down the cause

For high-assurance software:
- e.g. aircraft, vehicle, cardiac device
- source programs are often formally verified against its specification
- miscompilation can invalidate the guarantees obtained by the inspection to source program
We've claimed that compilers should "preserve semantics" or "produce code that executes in accordance with the semantics of the source program".

- What does this mean exactly?
- Should source and compiled code do exactly the same thing?
- What should be preserved?

The only thing that matters is the observable behavior.
Observable behavior

Source

```c
int sum_10() {
    int res = 0;
    for (int i = 1; i <= 10; i++) {
        res += i;
    }
    return res;
}
```

Target

```c
int sum_10() {
    return 55;
}
```
For realistic languages, observable behaviors include:

- termination
- divergence
- abnormal termination
- I/O operations

However, program contains nondeterminism:

- unspecified behavior e.g. evaluation order of $\text{foo}(\text{g}(), \text{k}())$
- undefined behavior e.g. use of uninitialized variable
Refinement relation (backward simulation) [Leroy(2019)]

Definition (refinement)

Every possible behavior of the compiled program $C$ is a possible behavior of the source program $S$. However, $C$ may have fewer behaviors than $S$.

Refinement suffices to show the preservation of properties established by source-level verification: If the behavior of $S$ satisfy a specification $Spec$, then the behavior of $C$ satisfy $Spec$ as well.
For simplicity, we assume determinism for source program and compiled program.

- $f_{\text{src}}/f_{\text{tgt}}$ are the source/target program, which can be regarded as functions
- $I_{\text{src}}/I_{\text{tgt}}$ are inputs to the source/target functions
- $O$ is the return value of functions
- $f(I, O)$ means function $f$ will output $O$ given input $I$

Then we have the simplified refinement as follows:

$$\forall I_{\text{src}}, I_{\text{tgt}}, O. (I_{\text{src}} = I_{\text{tgt}} \land f_{\text{tgt}}(I_{\text{tgt}}, O)) \implies f_{\text{src}}(I_{\text{src}}, O)$$
Some attempts to approach compiler correctness

Translations validation:
- avoid the need to inspect the complex logic inside compiler
- look at one transformation each time

Compiler testing/fuzzing:
- generate quality source programs for compiler
- check target program

Correct by construction:
- construct the whole compiler in proof assistant
- corresponding proof is done in proof assistant
The goal is to check whether this source program and this target program have the same observable behavior (same return value in our simplified case).

Source

```plaintext
foo(x, y, j):
  a = x * y
  if (j == 1){
    x = 1
    b = x * y
  }
  else{
    b = x * y
  }
return b
```

Target

```plaintext
foo(x, y, j):
  a = x * y
  if (j == 1){
    x = 1
    b = a
  }
  else{
    b = a
  }
return b
```
SAT stands for Boolean satisfiability problem. It is a problem of deciding the bool variable assignment that satisfies a given proposition formula.

\((x_1 \lor x_2 \lor \neg x_3) \land (\neg x_4 \lor x_5)\)

A SAT solver will output one of the following:

- A variable assignment e.g. \(x_1 = true, x_2 = false, x_3 = false, x_4 = false, x_5 = true\)
- UNSAT (there is no assignment that can make the formula true)
- Don’t know (due to intractability)
SAT solver tries to find a variable assignment such that the given proposition formula is true. For any valid proposition such as

\[ x \lor \neg x \]

The formula is true for any assignment. As a result, to prove its validity, we ask the SAT solver to find an assignment that will make its negation true, which is

\[ \neg x \land x \]

If the SAT solver returns UNSAT, we have proven the formula.
SAT/SMT solver

SMT stands for Satisfiability module theory. It is built based on SAT solver, with support for more complex variable type other than boolean.

\[(x + 2y = 10) \land (x + y = 7)\]

Similarly SMT solver will output one of the following:

- A variable assignment e.g. \(x = 4, y = 3\)
- UNSAT
- Don’t know
SMT for graph coloring problem

Fill in colors to nodes such that adjacent nodes have different colors.

\[
(A = 1 \lor A = 2 \lor A = 3 \lor A = 4) \land \\
(B = 1 \lor B = 2 \lor B = 3 \lor B = 4) \land \\
(C = 1 \lor C = 2 \lor C = 3 \lor C = 4) \land \\
(D = 1 \lor D = 2 \lor D = 3 \lor D = 4) \land \\
\neg(A = C) \land \neg(A = B) \land \neg(A = D) \land \\
\neg(B = C) \land \neg(B = D) \land \neg(C = D)
\]

Output: \( A = 1, B = 2, C = 3, D = 4 \)
SMT encoding for source program

Source

```python
foo(x1, y1, j1):
    a1 = x1 * y1
    if (j1 == 1):
        x1' = 1
        b1 = x1' * y1
    else:
        b1 = x1 * y1
    return b1
```

SMT encoding for Source:

\[(a1 = x1 \times y1) \wedge (x1' = 1) \wedge (b1 = ITE(j1 == 1, x2 \times y1, x1 \times y1))\]
Target

\text{foo}(x_2, y_2, j_2):\
  \begin{align*}
    a_2 &= x_2 \times y_2 \\
    \text{if } (j_2 == 1) &
      \begin{align*}
        x_2' &= 1 \\
        b_2 &= a_2
      \end{align*} \\
    \text{else } &
      \begin{align*}
        b_2 &= a_2
      \end{align*}
  \end{align*}
\text{return } b_2

SMT encoding for Target:

\[(a_2 = x_3 \times y_3) \land (x_2' = 1) \land (b_2 = \text{ITE}(j_2 == 1, a_2, a_2))\]
Recall the definition of refinement

$$\forall I_{src}, I_{tgt}, O. (I_{src} = I_{tgt} \land f_{tgt}(I_{tgt}, O)) \implies f_{src}(I_{src}, O)$$

Its negation is

$$\exists I_{src}, I_{tgt}, O. (I_{src} = I_{tgt} \land f_{tgt}(I_{tgt}, O)) \land \neg f_{src}(I_{src}, O)$$

The final formula passed to SMT solver is

$$(a_1 = x_1 \ast y_1) \land (x_1' = 1) \land (b_1 = ITE(j_1 == 1, x_2 \ast y_1, x_1 \ast y_1)) \land$$
$$(a_2 = x_3 \ast y_3) \land (x_2' = 1) \land (b_2 = ITE(j_2 == 1, a_2, a_2)) \land$$
$$(x_1 = x_2) \land (y_1 = y_2) \land (j_1 = j_2) \land$$
$$\neg(b_1 = b_2)$$

Output can be $x_1 = 2$, $y_1 = 1$, $j_1 = 1$. 
If you still remember..........

```
Executing 'lcm.py' on 'lcm_pre.c'... (0/3.3333333333333333)

PASS: lcm.py on 'lcm_pre.c'
PASS: compile output of lcm.py
FAIL: Correctness check #1 of 1
  SUCCESS: check d
  SUCCESS: check b
  SUCCESS: check c
  SUCCESS: check a (c > d)
  SUCCESS: check a (c <= d)
FAILURE: return value is d

==== OUTPUT ====
```
```c
int pre_test(int a, int b, int c, int d) {
    if(c > d) {
        a = b + c;
    }
    d = b + c;
    printf("a: %d, b: %d, c: %d, d: %d\n", a, b, c, d);
    return d;
}
```
A typical testing activity contains:
- generate test cases as inputs (manually or automatically)
- look at the outputs (testing oracle)

When it comes to compiler testing:
- generate source programs
- look at the target programs

But what properties to check?
Check for semantics preservation

For a transformation from a source program to a target program, it is correct when the semantics is preserved. Possibility for cheating?

Come up with source programs for testing (fuzzing):

- randomly generate complex source programs
- modify previous successful source programs
- reverse compiler execution for source programs that take certain path
Check for equivalence (Metamorphic testing)

I may not know what the output is, but I know what it should never be

Assume you have a $\sin$ function

$$\sin(x) = \sin(\pi - x)$$

The focus shifts from verifying to finding bugs. (less bug means more correct?)
Check for equivalence

When it comes to compiler testing:

- same source programs for a compiler with near versions
- unit source programs for "peer" compilers from different vendors
Compcert

The first formally verified realistic compiler. (which took more than 5 years)

- closer look to implementation logic
- focus on code-gen transformation
Execution of a program is a sequence of program state change.

$$\alpha_0 \rightarrow \alpha_1 \rightarrow \alpha_2 \rightarrow \cdots \rightarrow \alpha_n$$

Consider an interpreter with small-step semantics. Program states only contain variable assignment.

$$\{x : 0\} \xrightarrow{x=3} \{x : 3\} \xrightarrow{x=x-1} \{x : 2\} \rightarrow \ldots$$
Simulation

{x=0} \approx \{x'=0\}
\rightarrow \quad x = x + 2 \quad \rightarrow \quad x' = x' + 1
\downarrow \quad \downarrow
\{x=2\} \approx \{x'=2\}

Simulation diagram

\[ \begin{array}{c}
S_{\text{init}} \approx C_{\text{init}} \\
S_1 \approx C_1 \\
\vdots \\
S_n \approx C_n \\
\text{Final} \supseteq S_n \approx C_n \subseteq \text{Final}
\end{array} \]
Coq proof assistant

It is a proof assistant, that’s all I know.
What is compiler correctness?
- miscompilation
- observable equivalence (semantics preservation)

Why it is important?
- miscompilation is hard to track
- source-level correctness needs to be preserved

How can we approach it?
- translation validation
- compiler testing
- proof from construction
