1 Introduction

The labs in CSC172 will follow a pair programming paradigm. Every student is encouraged (but not strictly required) to have a lab partner. Labs will typically have an even number of components. The two partners in a pair programming environment take turns at the keyboard. This paradigm facilitates code improvement through collaborative efforts, and exercises the programmers cognitive ability to understand and discuss concepts fundamental to computer programming. The use of pair programming is optional in CSC172. It is not a requirement. You can learn more about the pair programming paradigm, its history, methods, practical benefits, philosophical underpinnings, and scientific validation at http://en.wikipedia.org/wiki/Pair_programming.

Every student must hand in his own work, but every student must list the name of the lab partner (if any) on all labs.

This lab has six parts. You and your partner(s) should switch off typing each part, as explained by your lab TA. As one person types the lab, the other should be watching over the code and offering suggestions. Each part should be in addition to the previous parts, so do not erase any previous work when you switch.

The textbook should present examples of the code necessary to complete this lab. However, collaboration is allowed. You and your lab partner may discuss the lab with other pairs in the lab. It is acceptable to write code on the white board for the benefit of other lab pairs, but you are not allowed to electronically copy and/or transfer files between groups.
1. Since this is a course in data structures, let's look at structuring some data in lisp (scheme). The fundamental concept of data aggregation in this language is the list. (You never would have guessed that, right?) We can construct lists in lisp (say that 5 times, fast) with the list operator. Let's try this, just for fun. Type in the following and examine the results.

(list 1 2 3)
(list 1 2 3 5 6 7 8)
(define list1 (list 0 1 2 3 4 5 6 7 8 9))
(display list1)
(list “abe” “bea” “cal” “deb”)
(define bintree (list (list 1 2) (list 3 4)))
(display bintree)
(display list3)
(define arry3x3 (list (list 1 2 3) (list 4 5 6) (list 7 8 9))
(display arry3x3)
()
(list)
(null? ())
(null? (list))
(null? (list 1 2 3))

So, it should be clear from the above that we can make lists. We can even make empty (a.k.a. “null”) lists if we like. We can define variables to refer to lists. We can also make lists of lists. Perhaps you might have noticed that lists of lists could look like arrays and that more complex nested list structures look like binary trees? (Don't worry if you don't - it should become apparent later.)

2. OK, We can construct a list. Once we have a list how do we get stuff out of it? In Lisp, there are two commands of fundamental importance. The first is the car operator\(^1\). The second is the cdr operator (pronounced “could-er”)\(^2\). The car operator gives us the head of a list. The cdr operator gives us everything but the head. Type the following:

(car (list 1 2 3))
(cdr (list 1 2 3))
(define list3 (list 0 1 2 3 4 5 6 7 8 9))
(display list3)

---

1 Once upon a time, this stood for “Contents of Address part of Register”, on an IBM 704 computer.
2 Similarly, “Contents of Decrement part of Register”.

(car list3)
(cdr list3)
(cdr (cdr list3))
(cdr (cdr (cdr list3)))
(car (cdr (cdr (cdr list3))))

It turns out that there is a nice abbreviation syntax to make the code a bit more compact. Instead of typing `(cdr (cdr someList))` we can use `(cddr someList)`. It works with the “a” in car as well. Type in and observe the following:

(display list3)
(cdr list3)
(cddr list3)
(cdddr list3)
(car (cdddr list3))
(cadddr list3)

(define list4 (list
    (list (list 1 2) (list 3 4) (list 5 6) )
    (list (list 7 8) (list 9 10) (list 11 12) )
    (list (list 13 14) (list 15 16) (list 17 18 ))
)
(display list4)
(car list4)
(caar list4)
(caaar list4)
(cadr list4)
(cdadr list4)
(cddr list4)
(cddadr list4)
(cadadr list4)

3. One more simple operation. We can construct a pair (sometimes referred to as a dotted-pair)
with the **cons** operation\(^3\). It's just a bit more complex than the list operation, but it helps us to build lists a little bit at a time. Again, type and observe.

```
(cons 1 2)
(car (cons 1 2))
(cdr (cons 1 2))
(define list6 (cons (cons 1 2) (cons 3 4)))
(display list6)
(car list6)
(cdr list6)
(caar list6)
(cadr list6)
(cdar list6)
(cddr list6)
(cons 1 ())
(cons () 1)
(cons 1 (cons 2 ()))
(cons 1 (cons 2 (cons 3 ())))
(cons 1 (cons 2 (cons 3 (cons 4 ()))))
```

4. So, now that we can construct data items like pairs and list. Let's make some functions that process data. Consider making a **rational number** processing system. As you know, rational numbers have an integer numerator and denominator – perfect for a pair operation. Just like in Java we can think in terms of constructor and accessor operations.

```
(define (make-rat n d) (cons n d))
(define (numer rat) (car rat))
(define (denom rat) (cdr rat))
(define (print-rat rat)
   (newline) (display (numer rat))
   (display "/") (display (denom rat)))
(define one-half (make-rat 1 2))
(define one-third (make-rat 1 3))
(display one-half)
```

---

\(^3\) **cons**, from **construct** - pretty clever, eh?
5. Now, let's implement the five basic arithmetic operations (addition, subtraction, multiplication, division and test for equality), on the “rational number type”. What you need to do is to write function definitions for (add-rat rat1 rat2), (sub-rat rat1 rat2), (mul-rat rat1 rat2) and (div-rat rat1 rat2). In the body of each of these you should make a call to the make-rat constructor, passing in the appropriately extracted values for the new numerator and denominator. The (equal-rat rat1 rat2) doesn't need to construct a new rational number. Instead, it uses a call to the “=” operator with the appropriate values. To implement these methods, use the formulas shown. The definition of add-rat is given as a template.

\[
\frac{n_1 + n_2}{d_1} = \frac{n_1 d_2 + n_2 d_1}{d_1 d_2}
\]

\[
\frac{n_1 - n_2}{d_1} = \frac{n_1 d_2 - n_2 d_1}{d_1 d_2}
\]

\[
\frac{n_1 \times n_2}{d_1 d_2} = \frac{n_1 n_2}{d_1 d_2}
\]

\[
\frac{n_1}{d_1} = \frac{n_2}{d_2} \text{ if and only if } n_1 d_2 = n_2 d_1
\]

(define (add-rat rat1 rat2)
  (make-rat (+ (* (numer rat1) (denom rat2))
              (* (numer rat2) (denom rat1)))
              (* (denom rat1) (denom rat2))))

6. Compete this lab constructing at least 10 different rational numbers. Demonstrate that the functions you defined in the previous section work by performing operations on the rationals you define.

2 Hand In

Hand in the source code from this lab at the appropriate location on the blackboard system at my.rochester.edu. You should hand in a single compressed/archived (i.e. “zipped” file that contains the
1. A README that includes your contact information, your partner's name, a brief explanation of the lab (A one paragraph synopsis. Include information identifying what class and lab number your files represent.).

2. The source code files representing the work accomplished for this lab. All source code files should contain author and partner identification in the comments at the top of the file.

3. A plain text file named OUTPUT that includes author information at the beginning and shows the compile and run steps of your code. The best way to generate this file is to cut and paste from the command line.

3 Grading

172/grading.html

Each section (1-6) accounts for 15% of the lab grade (total 90%)

(README file counts for 10%)