

GAN-EM: GAN Based EM Learning Framework Wentian Zhao¹ Shaojie Wang¹ Zhihuai Xie² Jing Shi¹ Chenliang Xu¹ ¹University of Rochester ²Tsinghua University

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Introduction

- Expectation maximization (EM) algorithm is to find the maximum likelihood solution for models having latent variables. A typical example is the Gaussian mixture model (GMM), which requires a Gaussian assumption. However, natural images are highly non-Gaussian so that GMM is not ideal for performing image clustering task on pixel space.
- Generative adversarial network (GAN) has been proved to be powerful in learning data distribution. Previous work has shown that GAN can be modified to perform maximum likelihood estimation (MLE).

Methodology



- Instead of applying GMM on the image clustering task, we propose a GAN based EM learning framework that can maximize the likelihood of images and estimate the latent variables. We call this model GAN-EM, which is a framework for image clustering, semi-supervised classification, and dimensionality reduction. In M-step, we design a novel loss function for discriminator of GAN to perform MLE on data with soft class label assignments.
- The GAN-EM model outperforms most other popular clustering methods. In the meantime, the quality of the generated images is also comparable to different GAN variants. Examples of generated images:



M-step: We design a novel loss function for GAN discriminator to perform MLE on data with soft class label assignments. Specifically, a conditional generator captures data distribution for K classes, and a discriminator tells whether a sample is real or fake for each class.

$$L_G = -\frac{1}{2} \mathop{\mathbb{E}}_{c \sim U} \mathop{\mathbb{E}}_{z \sim \mathcal{N}} \exp\{\sigma^{-1}[D_c(G(z,c))]\}$$
$$L_D = \mathop{\mathbb{E}}_{c \sim U} \mathop{\mathbb{E}}_{z \sim \mathcal{N}} \sum_{i=1}^K \log(1 - D_i(G(z,c))) + \mathop{\mathbb{E}}_{x \sim P_r} \sum_{i=1}^K w_i \log(D_i(x))$$

E-step: We introduce another neural network, called E-net, to fit the data distribution. The E-net is trained on the data generated by the generator, acting as a reversed generator.

 $L_E = \mathop{\mathbb{E}}_{z \sim \mathcal{N}} \mathop{\mathbb{E}}_{c \sim \phi} \operatorname{CE}\{E(G(z,c)), u\}$

Experiments

| | MNIST | MNIST | MNIST | SVHN | CelebA | CelebA |
|--------------|---------------------|------------------|------------------|-------------------|----------------|--------------|
| | (Unsupervised) | (100 labels) | (1000 labels) | (1000 labels) | (Unsupervised) | (100 labels) |
| K-means | 46.51 ¹ | - | - | - | - | - |
| GMM | $32.61(\pm 0.06)^1$ | - | - | - | - | - |
| DEC | 15.7 ¹ | - | - | - | - | - |
| VAE | - | $3.33(\pm 0.14)$ | $2.40(\pm 0.02)$ | $36.02(\pm 0.10)$ | - | 45.38 |
| AAE | $4.10(\pm 1.13)^3$ | $1.90(\pm 0.10)$ | $1.60(\pm 0.08)$ | $17.70(\pm 0.30)$ | 42.88 | 31.03 |
| CatGAN | 4.27^{2} | $1.91(\pm 0.10)$ | $1.73(\pm 0.28)$ | - | 44.57 | 34.78 |
| InfoGAN | 5.004 | - | - | - | - | - |
| Improved GAN | - | 0.93(±0.06) | - | 8.11(±1.30) | - | - |
| VaDE | 5.54 ¹ | - | - | - | 43.64 | - |
| PixelGAN | $5.27(\pm 1.81)^3$ | $1.08(\pm 0.15)$ | - | 6.96(±0.55) | 44.27 | 32.54 |
| GANMM | $35.70(\pm 0.45)^1$ | - | - | - | 49.32 | - |
| GAN-EM | $4.20(\pm 0.51)^1$ | $1.09(\pm 0.18)$ | $1.03(\pm 0.15)$ | 6.05(±0.26) | 42.09 | 28.82 |
| | $4.04(\pm 0.42)^2$ | - | - | - | - | - |
| | $3.97(\pm 0.37)^3$ | - | - | - | - | - |



Convergence of test error rate of GAN-EM on MNIST.



Clustering: We perform unsupervised clustering on MNIST and CelebA datasets. GAN-EM achieves SOTA results on MNIST with 10, 20, and 30 clusters.

Semi-supervised classification: We extend our model to semi-supervised classification tasks where only a small part of samples' labels are known. We use almost the same training strategies as the clustering task except that we add the supervision to the E-net in every E-step. We evaluate the performance on MNIST, SVHN, and CelebA.

Dimensionality reduction: We add a new layer to the E-net before the output layer. After convergence of training, we take the output of this newly added layer as extracted features after dimensionality reduction.

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Representation of unsupervised dimensionality reduction on MNIST. Each color denotes one class of digit.