Midterm Exam
CSC 252
25 October 2021
Computer Science Department
University of Rochester

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Name: ____________________________________

Problem 0 (2 points): ______________________
Problem 1 (15 points): _____________________
Problem 2 (12 points): _____________________
Problem 3 (15 points): _____________________
Problem 4 (17 points): _____________________
Problem 5 (14 points) _____________________
Total (75 points): _________________________
Extra Credit (4 points) _____________________

Remember “I don’t know” is given 15% partial credit, but you must erase or cross out everything else. This does not apply to extra credit questions.

Your answers to all questions must be contained in the given boxes. Use spare space to show all supporting work to earn partial credit.

You have until the end of the class to work (~75 minutes).

Please sign the following. I have not given nor received any unauthorized help on this exam.

Signature: ____________________________________

GOOD LUCK!!!
Problem 0: Warm-up (2 Points)
What aspect of how computers work do you want to learn more about most of all?
(all answers accepted)

Problem 1: Fixed-point Arithmetic (15 points)
Part a) (4 points) Convert the decimal number 108 to hexadecimal.

Part b) (4 points) What is the decimal representation of the base 3 number 120?

Part c) (4 points) What is the two’s complement representation of the decimal number -43? Assume an 8-bit representation. Express the answer in hexadecimal.

Part d) (3 points) If 4-bit registers R1 and R2 contain 1100 and 0100 respectively, what are the values of the carry, overflow, and sign flags after the operation “add R1 R2”? 
Problem 2: Floating-Point Arithmetics (12 points)

Part a) (4 points) Put $\frac{9}{8}$ into the binary normalized form.

Part b) The IEEE has decided to introduce a 11-bit floating-point standard, whose main characteristics are consistent with existing floating-point number representations that we discussed in the class.

The following bit sequence contains the exact encoding of $\frac{33}{256}$ in this new standard:
00100000010

(2 points) How many bits are used for the fraction in this new standard?

(3 points) How many bits are used for the exponent in this new standard, and what is the bias?

(3 points) What is the smallest positive value that can be represented in this new standard? (Write your answer in decimal. You may use an exponent.)
(2 points extra credit) How would positive infinity be represented in this new float type? (write your answer in binary)

Problem 3: Data types and Assembly (15 points + 2 points extra credit)
Part a) Consider the following C struct:

```c
struct rec {
    char c;
    int i;
    char d;
    unsigned long id;
};
```

(3 points) Memory alignment requirements of variable types mean that there may be extra padding in a struct. How many bytes would the above struct use on the CS department machines?

(3 points) Reorder the variables in the above struct to use the least possible space. Write your answer as a C struct definition (like the example).
(2 points) How much space does your improved struct use?

Part b) Consider the following objdump output, produced from a C function which has been compiled with gcc:

```
000000000001141 <foo>:
  1141: 89 7c 24 ec    mov    %edi,-0x14(%rsp)
  1145: c7 44 24 fc 00 00 00  movl   $0x0,-0x4(%rsp)
  114c: 00
  114d: c7 44 24 f8 00 00 00  movl   $0x0,-0x8(%rsp)
  1154: 00
  1155: eb 13    jmp    116a <foo+0x29>
  1157: 8b 54 24 fc    mov    -0x4(%rsp),%edx
  115b: 8b 44 24 ec    mov    -0x14(%rsp),%eax
  115f: 01 d0    add    %edx,%eax
  1161: 89 44 24 fc    mov    %eax,-0x4(%rsp)
  1165: 83 44 24 f8 01  addl   $0x1,-0x8(%rsp)
  116a: 8b 44 24 f8    mov    -0x8(%rsp),%eax
  116e: 39 44 24 ec    cmp    %eax,-0x14(%rsp)
  1172: 77 e3    ja     1157 <foo+0x16>
  1174: 8b 44 24 fc    mov    -0x4(%rsp),%eax
  1178: c3    retq
```

(1 point) Where is the return value stored when retq is executed?

(2 points) If the C program calls foo(3), what value is returned?
(4 points) Write a C function “foo” that does the same thing as the assembly code above, in the same way. Be sure to show any loops and local variables needed. **Makes sure that your variable/argument types make sense given the assembly code above.**

(2 points extra credit) The assembly code shown is not very efficient. What x86_64 instruction would achieve the same result without looping? (you do not need to specify registers, just the instruction name that would appear in objdump)
Problem 4: Logic Design (17 points)

Part a) bit-wise operations
(3 points) What is the result of a bit-wise XOR between 0101 and 0110?

(3 points) What is the result of a bit-wise NOR between 0101 and 0110?

Part b) NAND gates!
It is possible to build any other gate out of combinations of only NAND gates. (We therefore say that NAND is “complete”)

For example, if you connect the inputs of a NAND gate together to act as one input, it will behave as a NOT gate.

(3 points) Draw a NOR gate made entirely from 4 NAND gates.
(2 points) Assume that our NAND gates each have a maximum delay of 1ps. What is the maximum delay of the NOR gate you designed above?

(3 points) In class we looked at the S-R latch, a memory circuit that can store one bit. In our slides, it was made from 2 OR gates and 2 NOT gates. Draw one made from 8 NAND gates (hint: use your NOR gate from above)
Part c) The logic circuit below is missing one gate, marked with the rectangle "?". The output of the entire circuit should match the truth table shown below.

Truth table:

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
</tbody>
</table>

Circuit Diagram:

(3 points) What type of gate is missing?
Problem 5: Microarchitecture (14 points)

Part a) Pipeline question!

Consider the CPU pipeline shown below.

(2 points) What is the minimum cycle time of this CPU?

(2 points) What is the instruction latency of this CPU?

(3 points) Suppose that the hardware designer decided to improve the design above by splitting the slowest stage into two separate stages. It would be a 4-stage CPU. What is the best possible throughput of this new design?
Part b) Now imagine that the 3-stage pipeline from the diagram above has the following stages: First stage is fetch. Second stage is decode, and the third stage does everything else (execute, memory, writeback). Consider the following assembly code fragment:

```
.L1:
sub $0x01, %rax
cmpq %rax, $0x01
jge .L1
add $0x99, %rsi
mov %rsi, %rax
ret
```

(3 points) If the jump is not taken, but the CPU predicts taken, how many cycles will it take for this code to finish? Assume that all data dependencies are handled by data forwarding, and assume that the branch misprediction is detected in the execute stage.

**Hint:** Remember that the pipeline starts empty, and the program is not done until the last instruction has finished all stages.
Part c) Suppose that you have written an assembly program with one conditional jump in it which will be taken twice in a row and then not taken. Your CPU has a two-bit branch predictor which will initially predict “not taken”.

(2 points) How many mispredictions will there be?

(2 points) How many mispredictions would there be if it was a 1-bit branch predictor instead?