

Some Rules of Reasoning

The reasoning example we saw for “Robbie’s self-model” showed particular logical reasoning examples (Robbie is not a person, Robbie is located somewhere, there is a dog), but without explicitly listing the mechanical rules we can use for such reasoning. Here are 4 very common inference rules, followed by another example:

$$\begin{array}{c}
 \frac{\Phi, \Phi \Rightarrow \Psi}{\Psi} \quad \frac{\forall x. \Phi}{\Phi_{x/C}} \quad \frac{\Phi, \neg \Phi \vee \Psi}{\Psi} \quad \frac{\Phi[C]}{\exists x. \Phi[x]} \sim \text{premises} \\
 \sim \text{conclusion} \\
 \nwarrow \\
 \text{C is some constant}
 \end{array}$$

Can you see which rules we used for the Robbie examples?

An inference using 2 steps: $\frac{\text{Dog}(\text{Snoopy}), \forall x. \text{Dog}(x) \Rightarrow \text{Has-Tail}(x)}{\text{Has-Tail}(\text{Snoopy})}$

Can you see which 2 rules have been used?

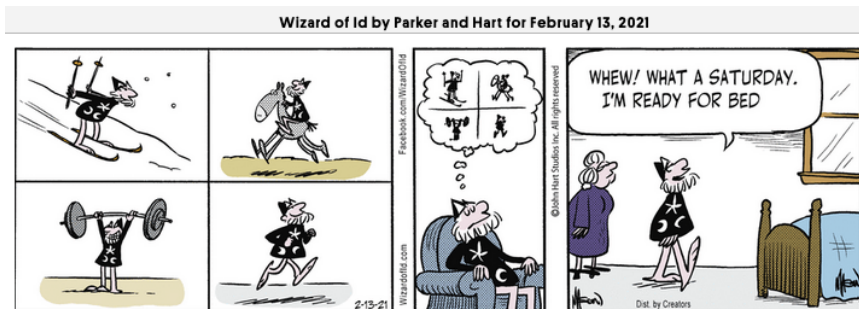
Horn clause form would use just one step (free variables are implicitly universal):

$\text{Dog}(\text{Snoopy})$
 $\text{Dog}(x) \Rightarrow \text{Has-Tail}(x)$
 ----- We unify variable x with constant **Snoopy**
 $\text{Has-Tail}(\text{Snoopy})$

Similarly, using clause form, a single resolution (cancellation) step suffices:

$\frac{\text{Dog}(\text{Snoopy}), \neg \text{Dog}(x) \vee \text{Has-Tail}(x)}{\text{Has-Tail}(\text{Snoopy})}$ Again, we unify as above (cf. rule 3, and the “Robbie” QA example)

These are *deductive rules* (as such completely reliable -- “sound”). But keep in mind that not all reasoning is deduction: We saw various ways of “jumping to conclusions” – in unsound, but generally useful ways; and recall special “analogue methods”, for example for “conjuring up” images in the mind (and in computers, we can use computer graphics to store and manipulated such images).



Faulty self-modeling ...